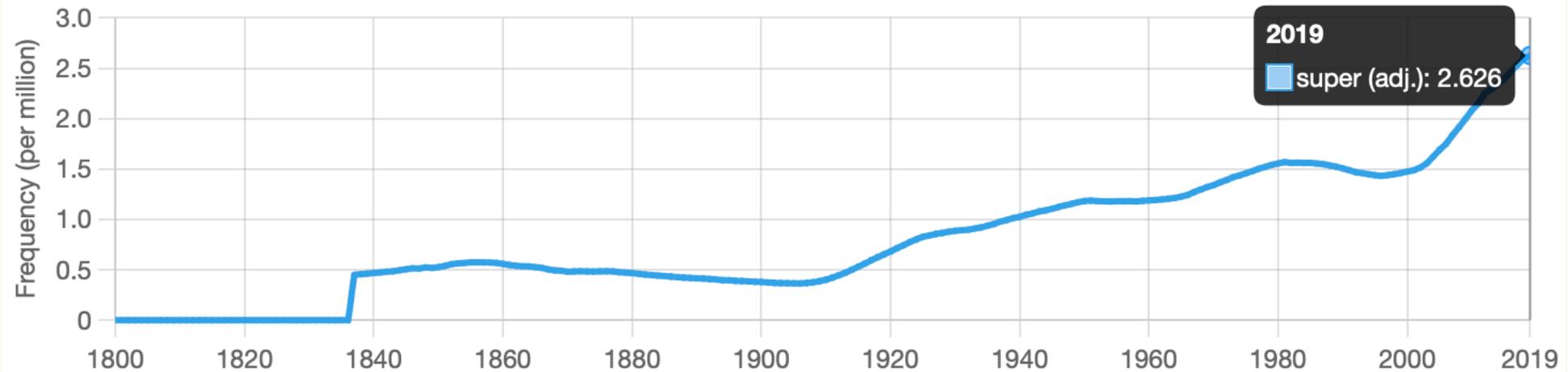


*“Super-”*

word-forming element of Latin origin meaning "above, over" in place or position; also in manner, degree, or measure, "over, beyond; ..."

Credit: [www.etymonline.com](http://www.etymonline.com)

### Trends of *super*





## **INTRODUCING CLEO:**

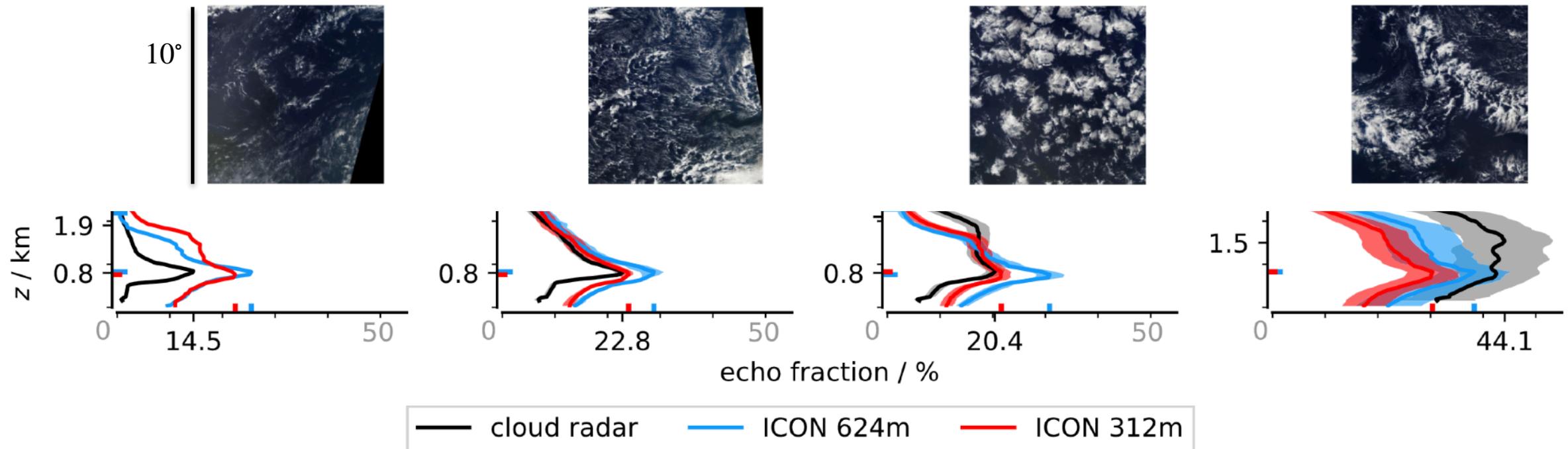
# **A NEW SUPER-DROPLET MODEL WITH COLLISIONAL BREAK-UP**

**Clara Bayley, T. Kölling, A. K. Naumann, R. Vogel, S. I. Shima, and  
B. Stevens**



# HIGHLY UNCERTAIN RAIN FROM SHALLOW CUMULI IN LES

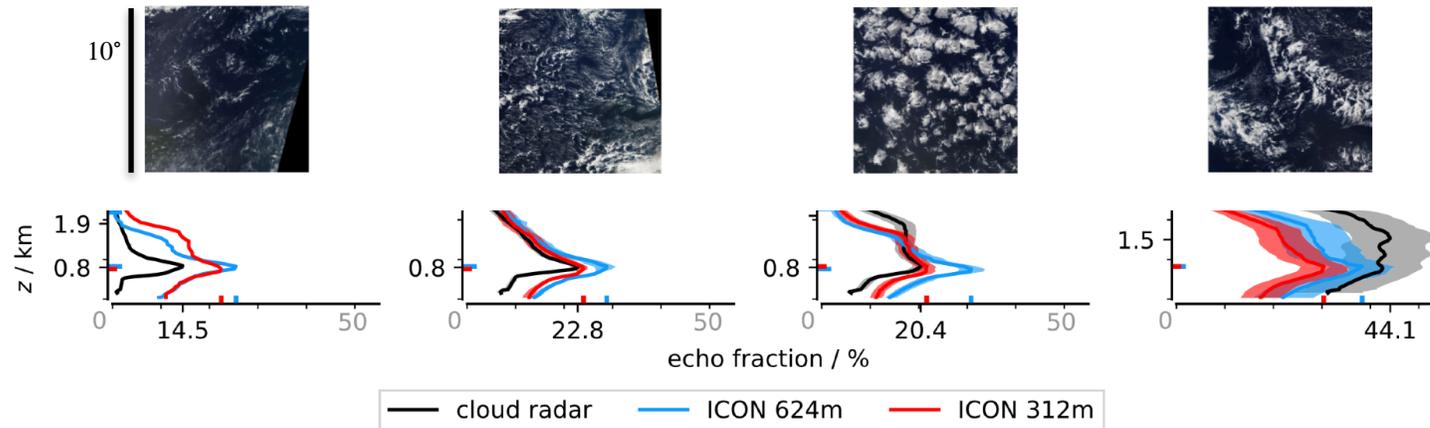
E.g. comparison of LES and EUREC4A observations:



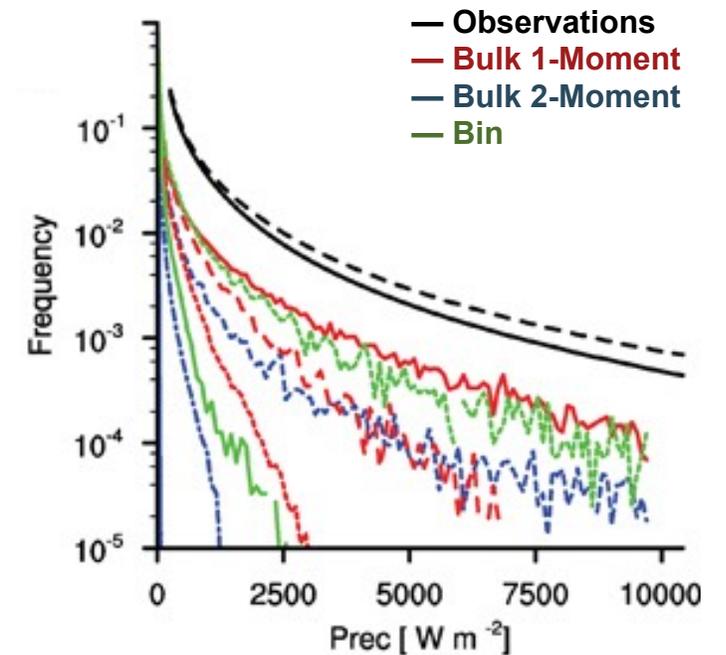


# HIGHLY UNCERTAIN RAIN FROM SHALLOW CUMULI IN LES IS PARTLY ATTRIBUTABLE TO MICROPHYSICS MODELS

E.g. comparison of LES and EUREC4A observations:



(Schulz and Stevens 2023) (Stevens et al. 2019)



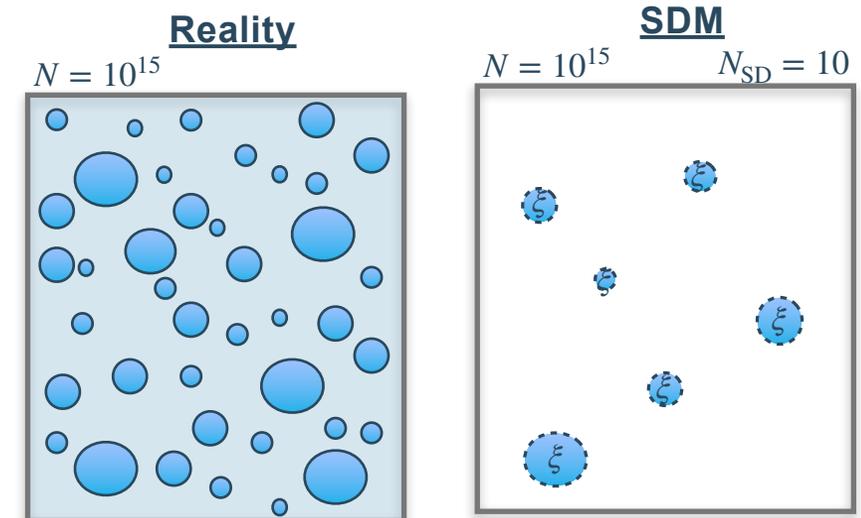
(van Zanten et al. 2011)



# THE SUPER-DROPLET MODEL (SDM) HAS SEVERAL MAJOR ADVANTAGES

Compared with conventional models for cloud microphysics, SDM...

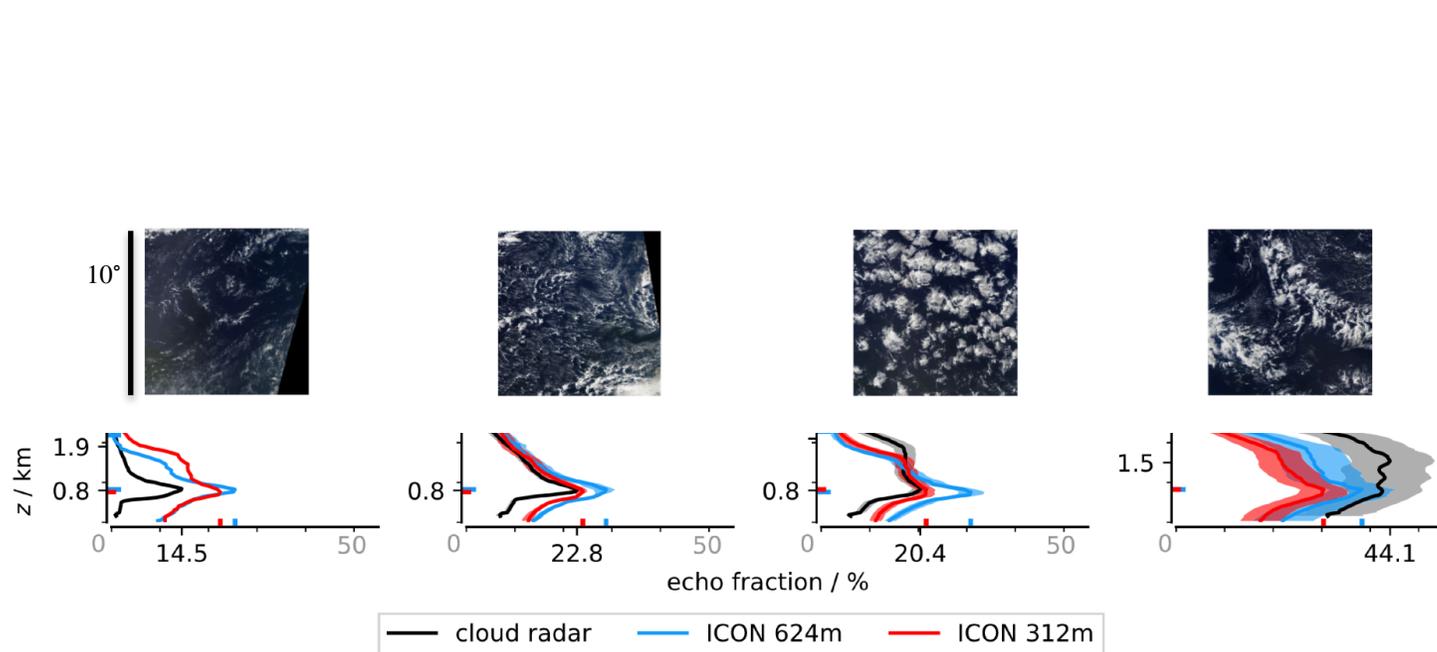
- has less numerical ambiguity
- is more suited to trends in High Performance Computing
- has insightful convergence properties



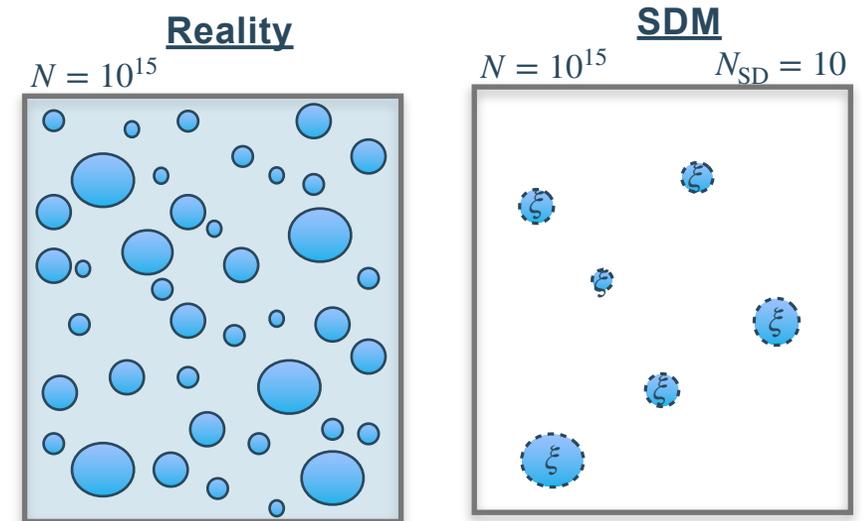
(Shima et al. 2009)



# CAN WE USE SDM TO BETTER REPRESENT RAIN FROM SHALLOW CUMULI AT THE MESOSCALE?



(Schulz and Stevens 2023) (Stevens et al. 2019)

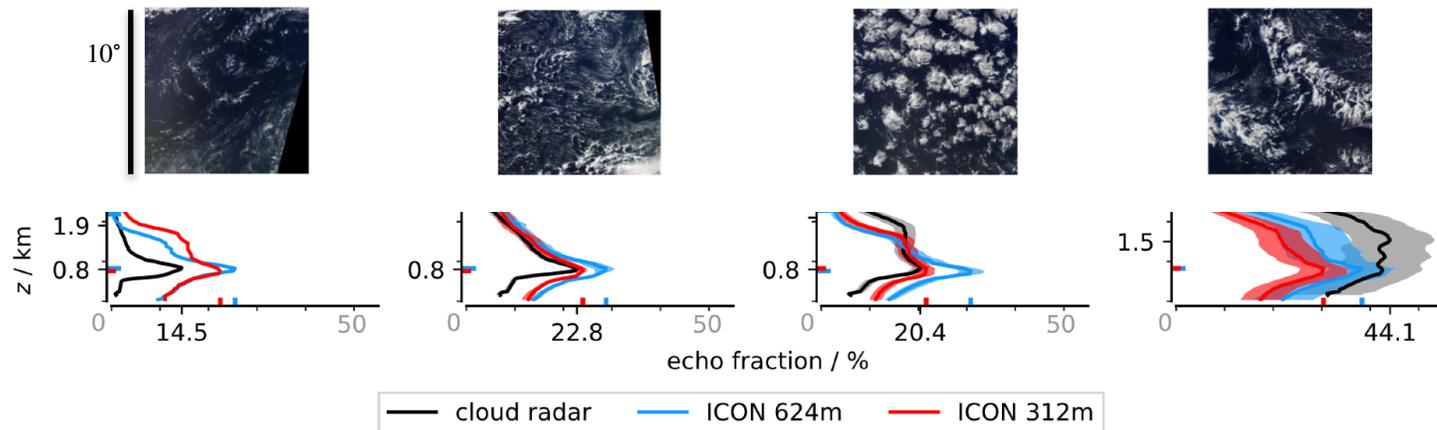


(Shima et al. 2009)

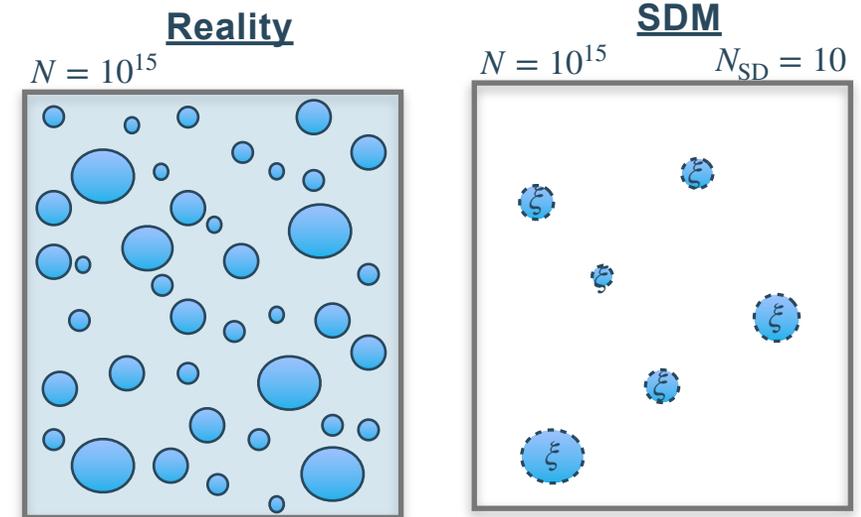


# CAN WE USE SDM TO BETTER REPRESENT RAIN FROM SHALLOW CUMULI AT THE MESOSCALE?

At the mesoscale we can study the interactions between precipitation and cloud organisation!



(Schulz and Stevens 2023) (Stevens et al. 2019)



(Shima et al. 2009)

SDM = Super-Droplet Model  
CLEO = this SDM implementation  
LES = Large Eddy Simulation

# CLEO: A SDM FOR WARM RAIN AIMING TO BE FEASIBLE IN O(100KM) DOMAINS AT HECTOMETER RESOLUTION

# CLEO: A SDM FOR WARM RAIN AIMING TO BE FEASIBLE IN O(100KM) DOMAINS AT HECTOMETER RESOLUTION

Purpose-built computational implementation

Extension of SDM collision algorithm to include rebound and breakup



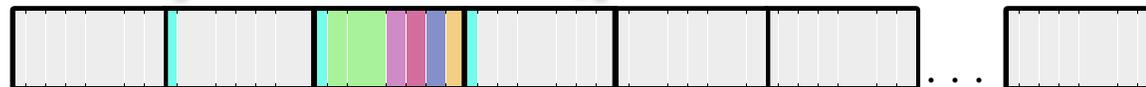
# CLEO: A SDM FOR WARM RAIN FEASIBLE IN $O(100\text{KM})$ LES

- Memory layout for **efficient data movement and cache loading**
- C++20 concepts constrain **compile-time determination** of microphysics and data output
- **Simplistic physics** from existing SDMs (mostly Shima et al. 2009)

Contiguous array of Gridboxes ordered by index



Dynamical core



Contiguous ordered array of super-droplets

**open source!**  
[yoctoyotta1024/CLEO](https://github.com/yoctoyotta1024/CLEO)





# CLEO: A SDM FOR WARM RAIN FEASIBLE IN $O(100\text{KM})$ LES

- Memory layout for **efficient data movement and cache loading**
- C++20 concepts constrain **compile-time determination** of microphysics and data output
- **Simplistic physics** from existing SDMs (mostly Shima et al. 2009)
  
- Need a framework for collisional breakup and rebound that:
  - Conserves super-droplet number (*c.f. Bringi et al. 2020*)
  - Is deterministic and non-iterative (*c.f. de Jong et al. 2023*)

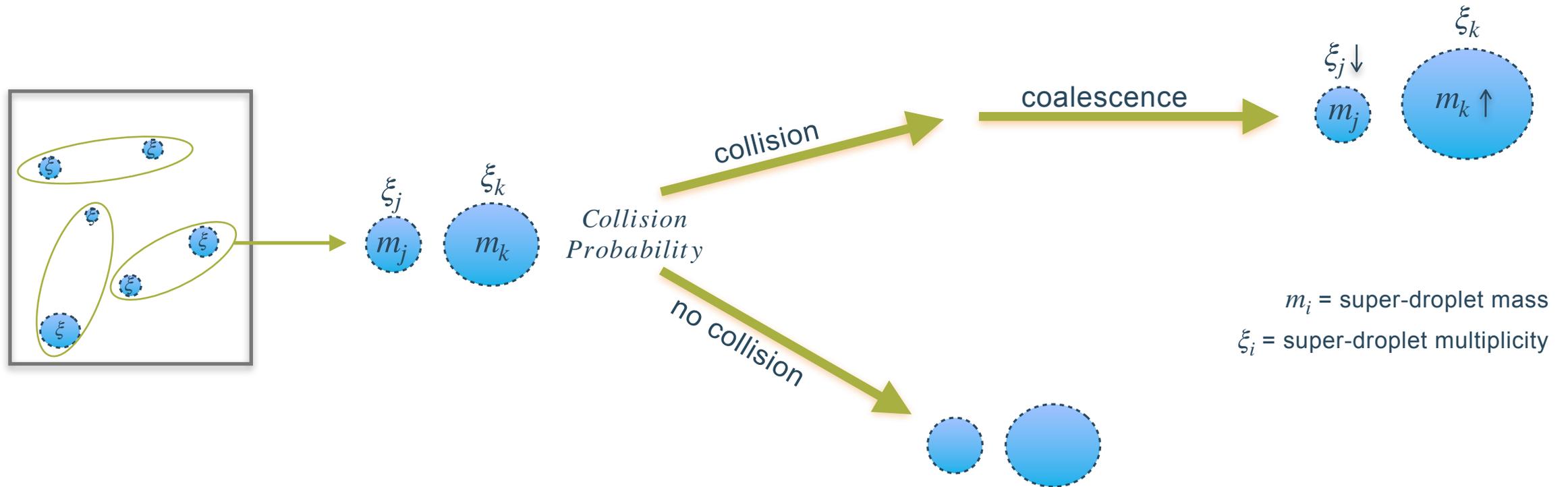
**open source!**  
**yoctoyotta1024/CLEO**



# EXTENSION OF SDM COLLISIONS TO INCLUDE REBOUND AND BREAKUP



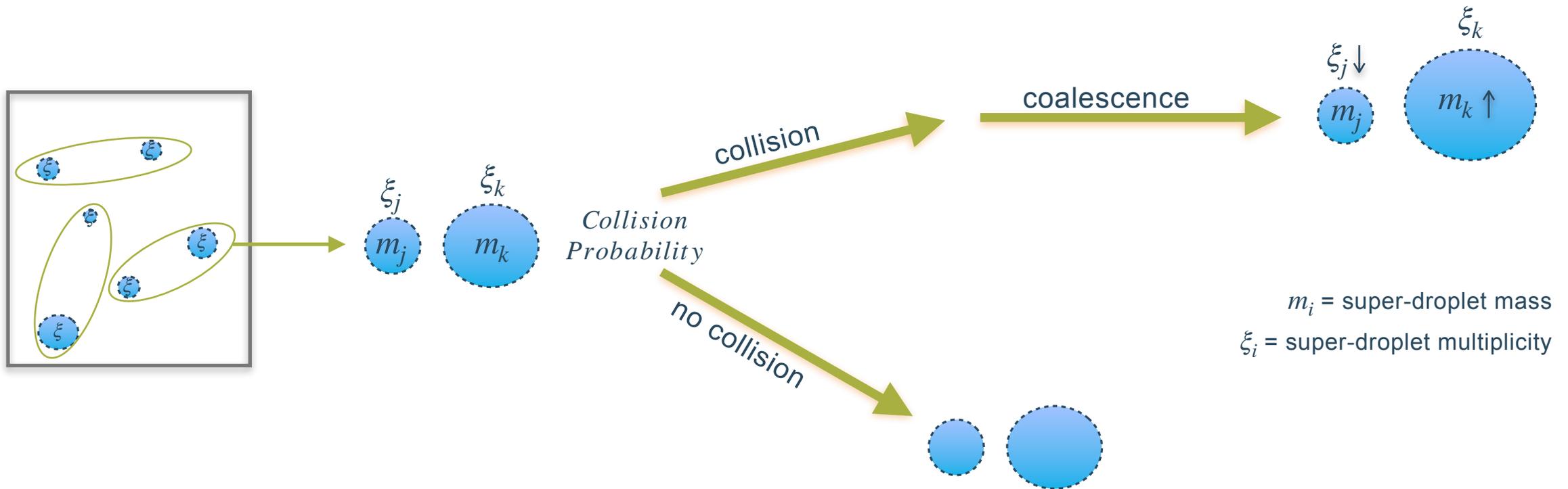
# ORIGINAL COLLISION-COALESCENCE ALGORITHM





# ORIGINAL COLLISION-COALESCENCE ALGORITHM

1. Randomly pair the super-droplets in a gridbox in a gridbox

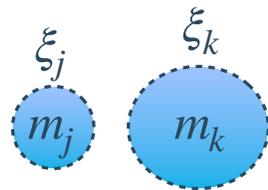
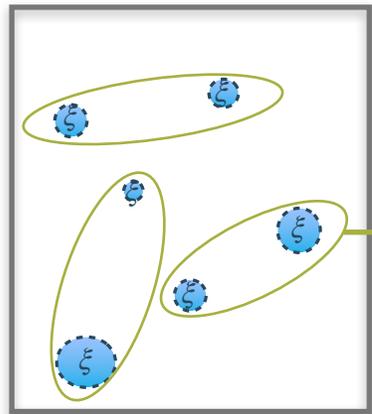




# ORIGINAL COLLISION-COALESCENCE ALGORITHM

1. Randomly pair the super-droplets in a gridbox

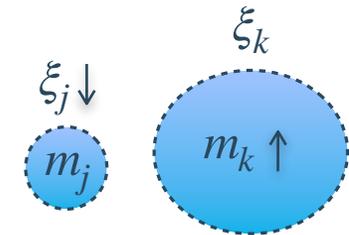
2. Calculate SDM collision probability



Collision Probability

collision

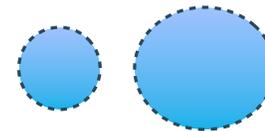
coalescence



$m_i$  = super-droplet mass

$\xi_i$  = super-droplet multiplicity

no collision



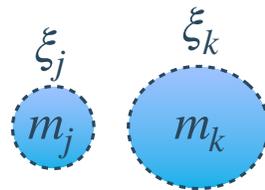
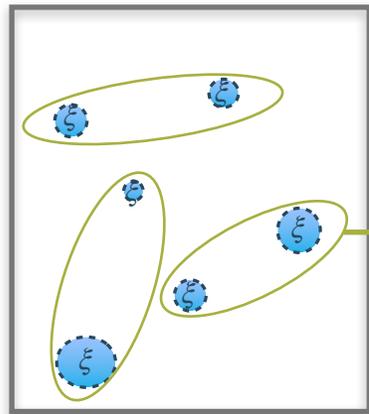


# ORIGINAL COLLISION-COALESCENCE ALGORITHM

1. Randomly pair the super-droplets in a gridbox

2. Calculate SDM collision probability

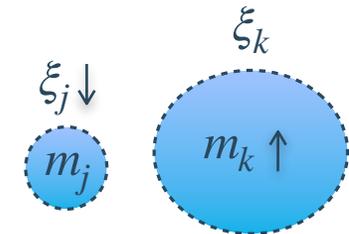
3. Random number to determine collision or not



*Collision Probability*

collision

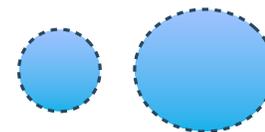
coalescence



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no collision





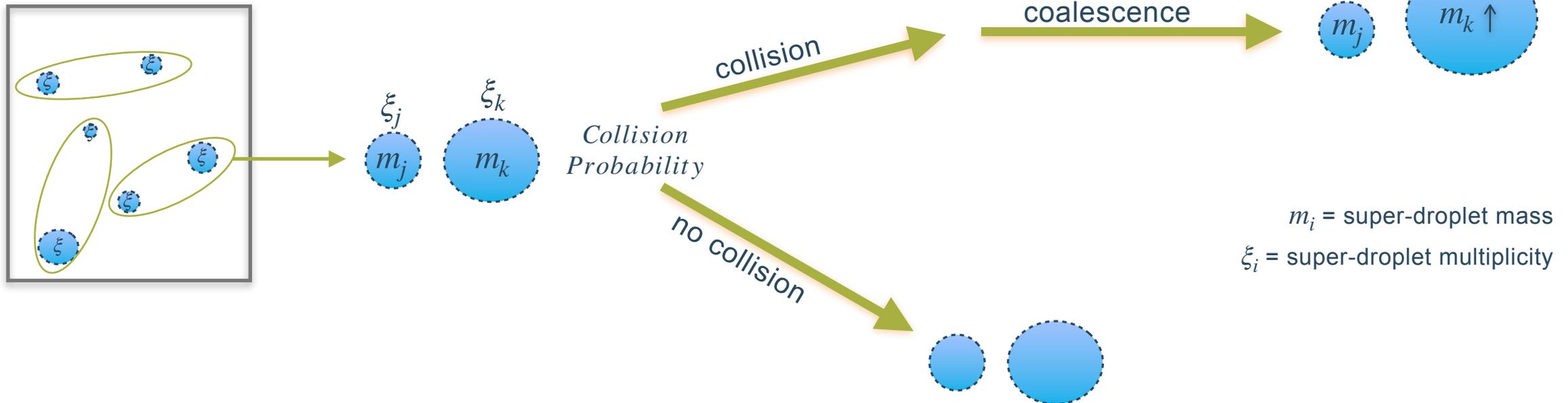
# ORIGINAL COLLISION-COALESCENCE ALGORITHM

1. Randomly pair the super-droplets in a gridbox

2. Calculate SDM collision probability

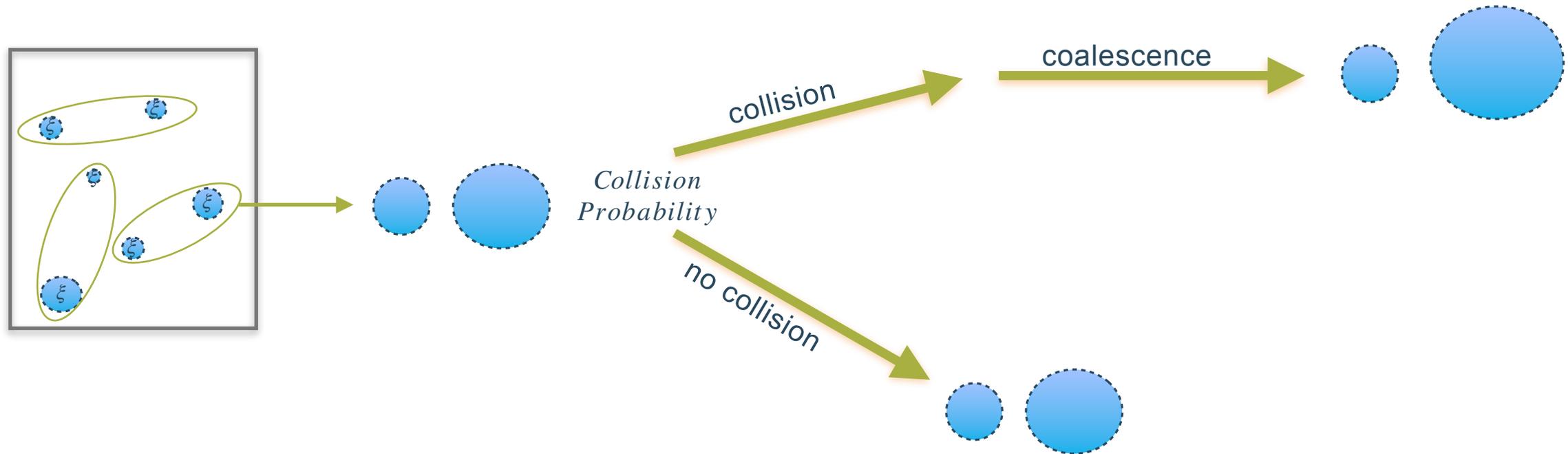
3. Random number to determine collision or not

4. Update super-droplet properties accordingly



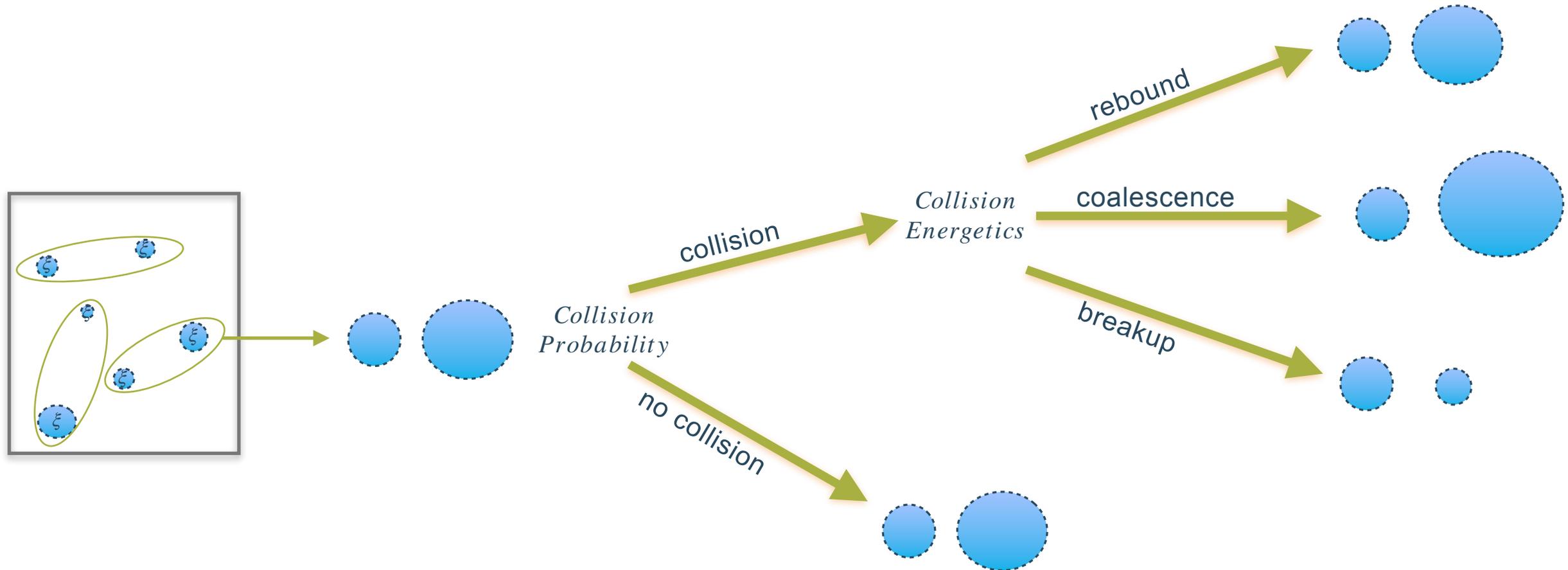


# ORIGINAL COLLISION-COALESCENCE ALGORITHM



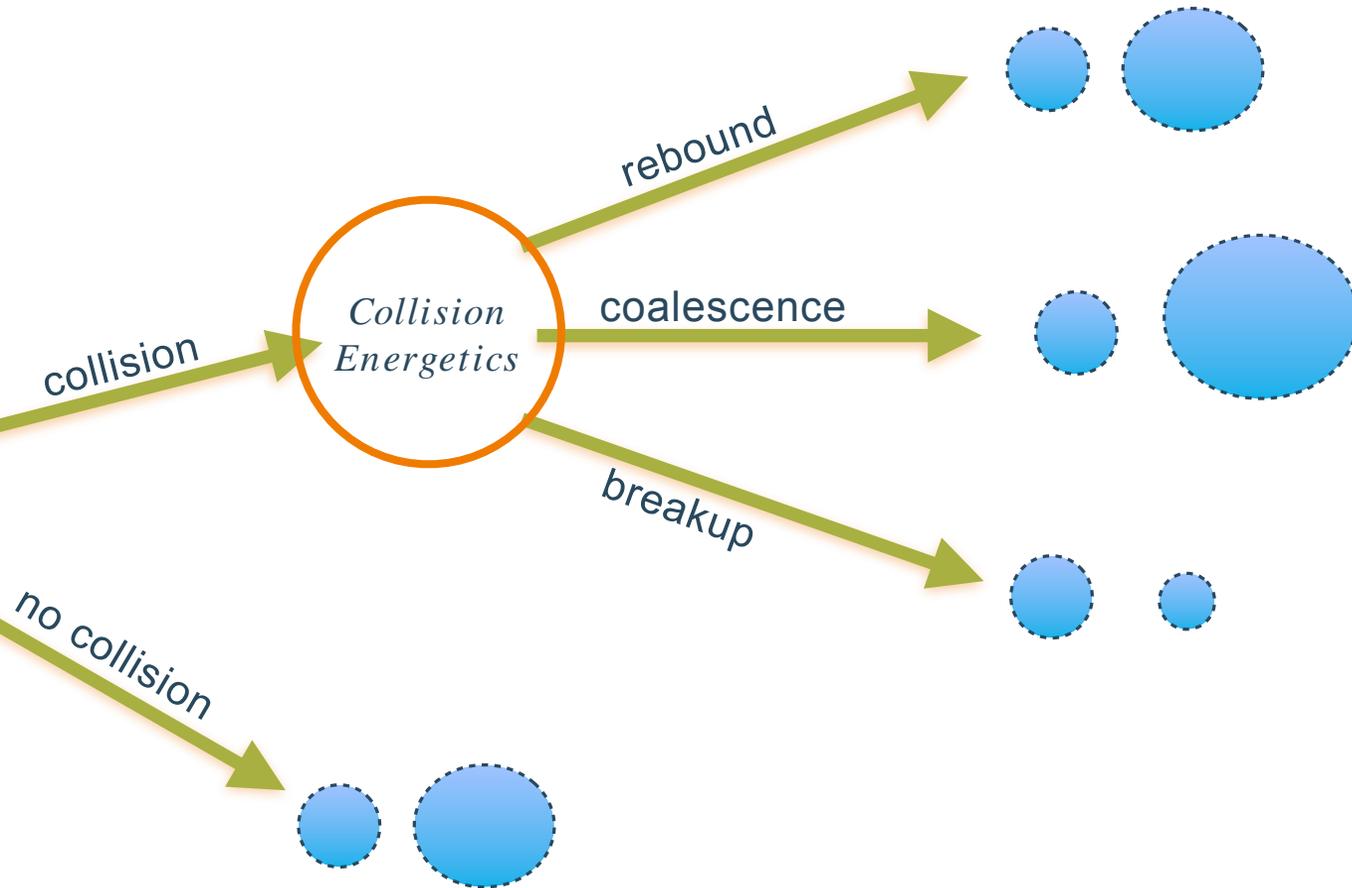


# EXTENSION TO INCLUDE REBOUND AND BREAKUP IN CLEO



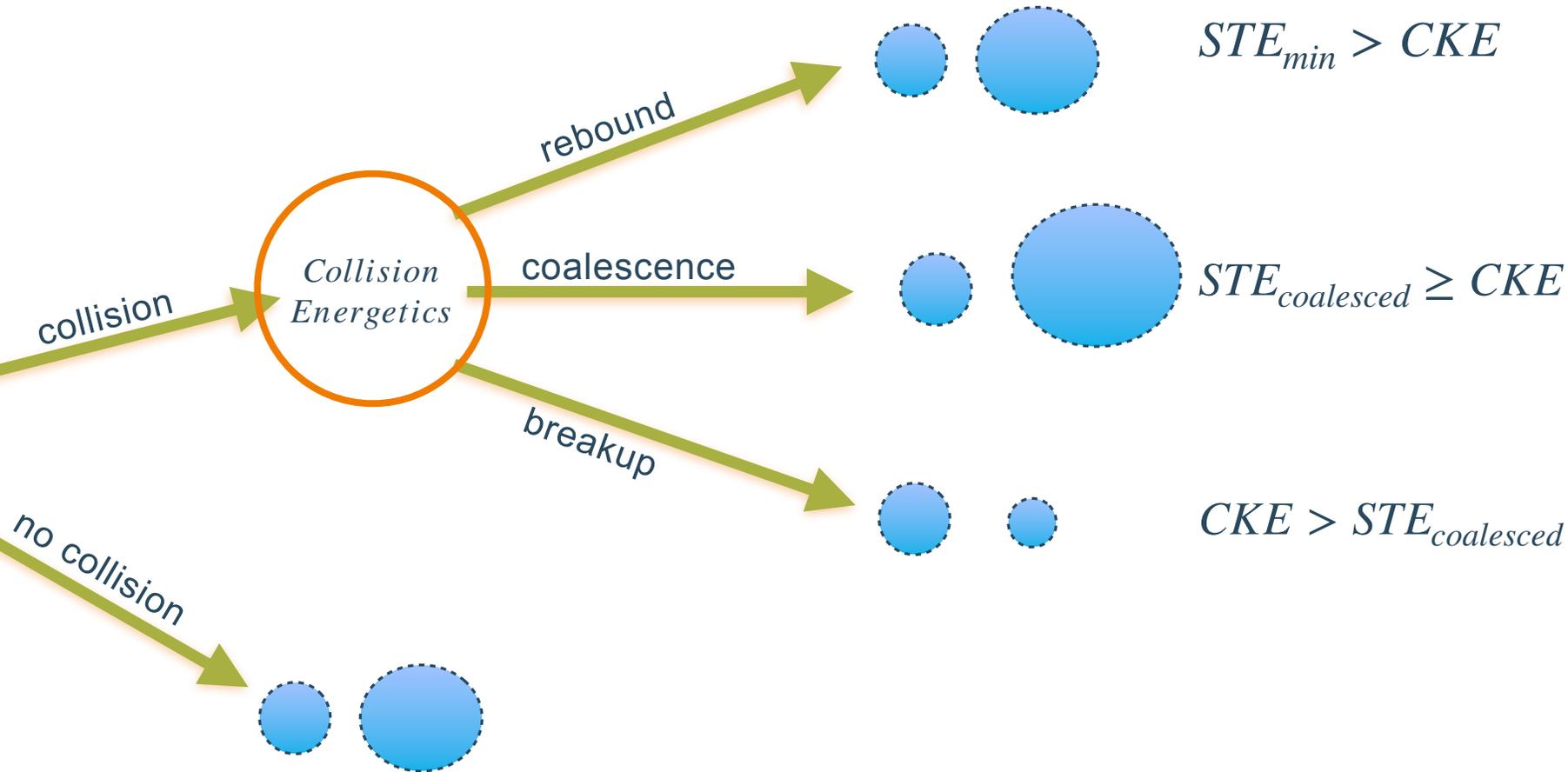


# COLLISION ENERGETICS DETERMINE OUTCOME





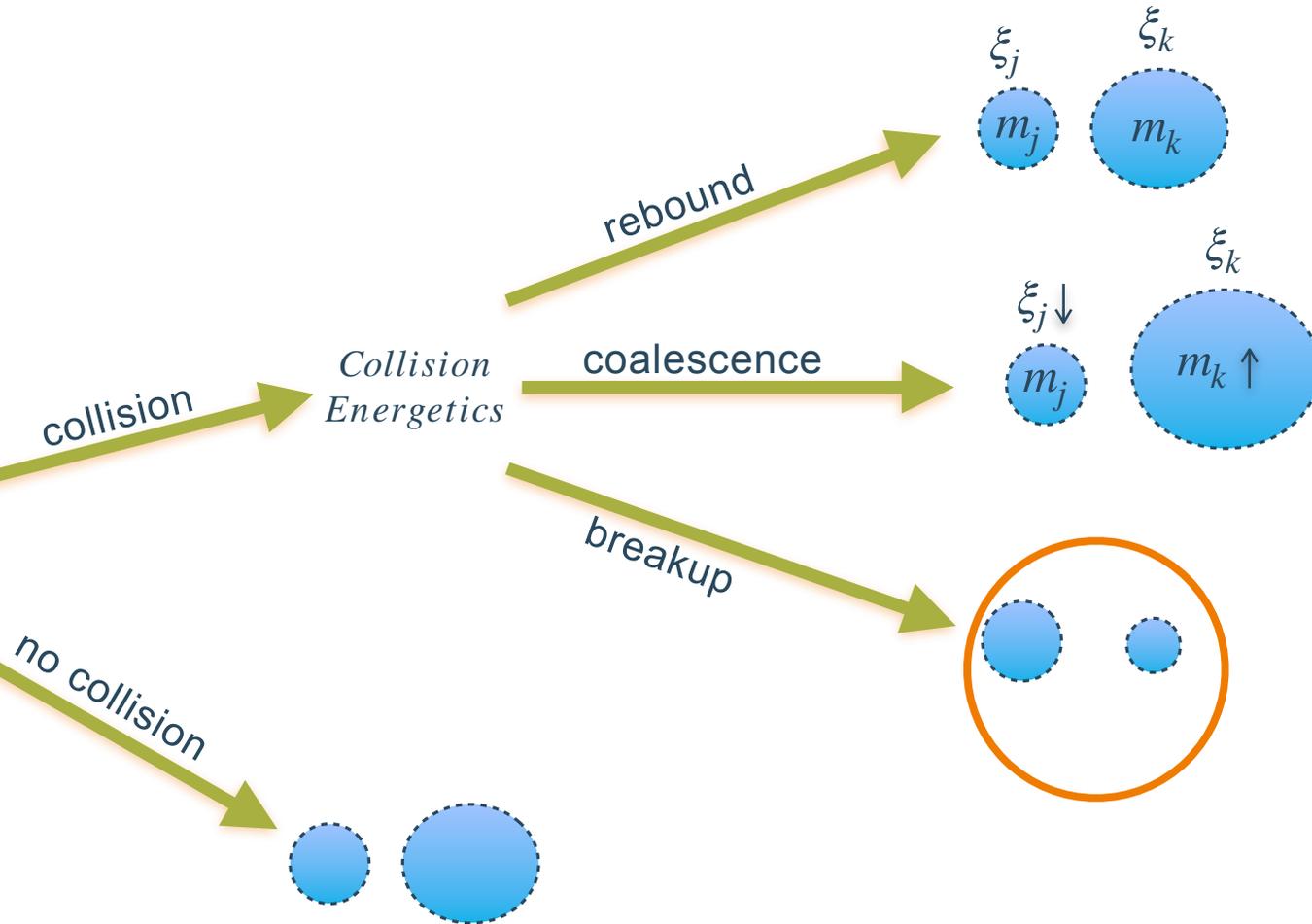
# COLLISION ENERGETICS DETERMINE OUTCOME



$STE$  = surface tension energy  
 $CKE$  = collision kinetic energy

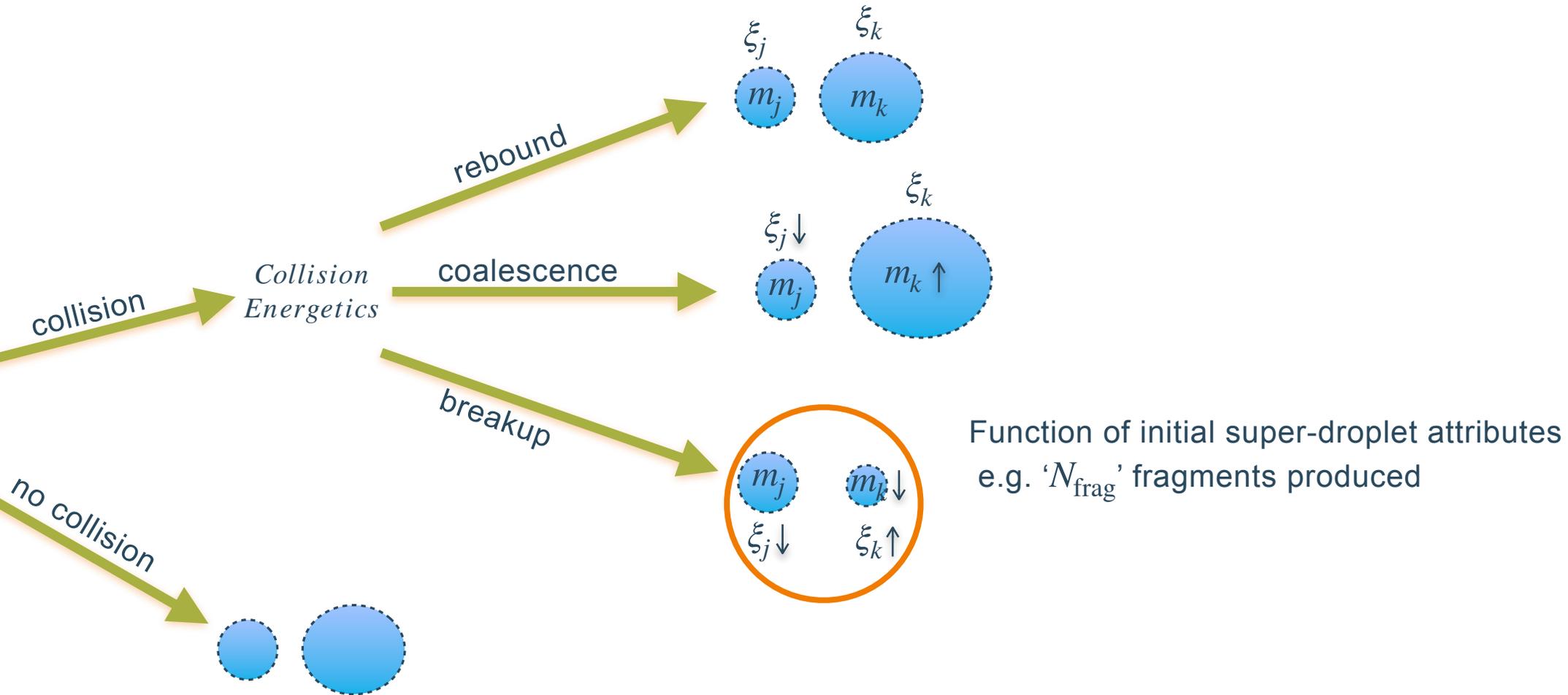


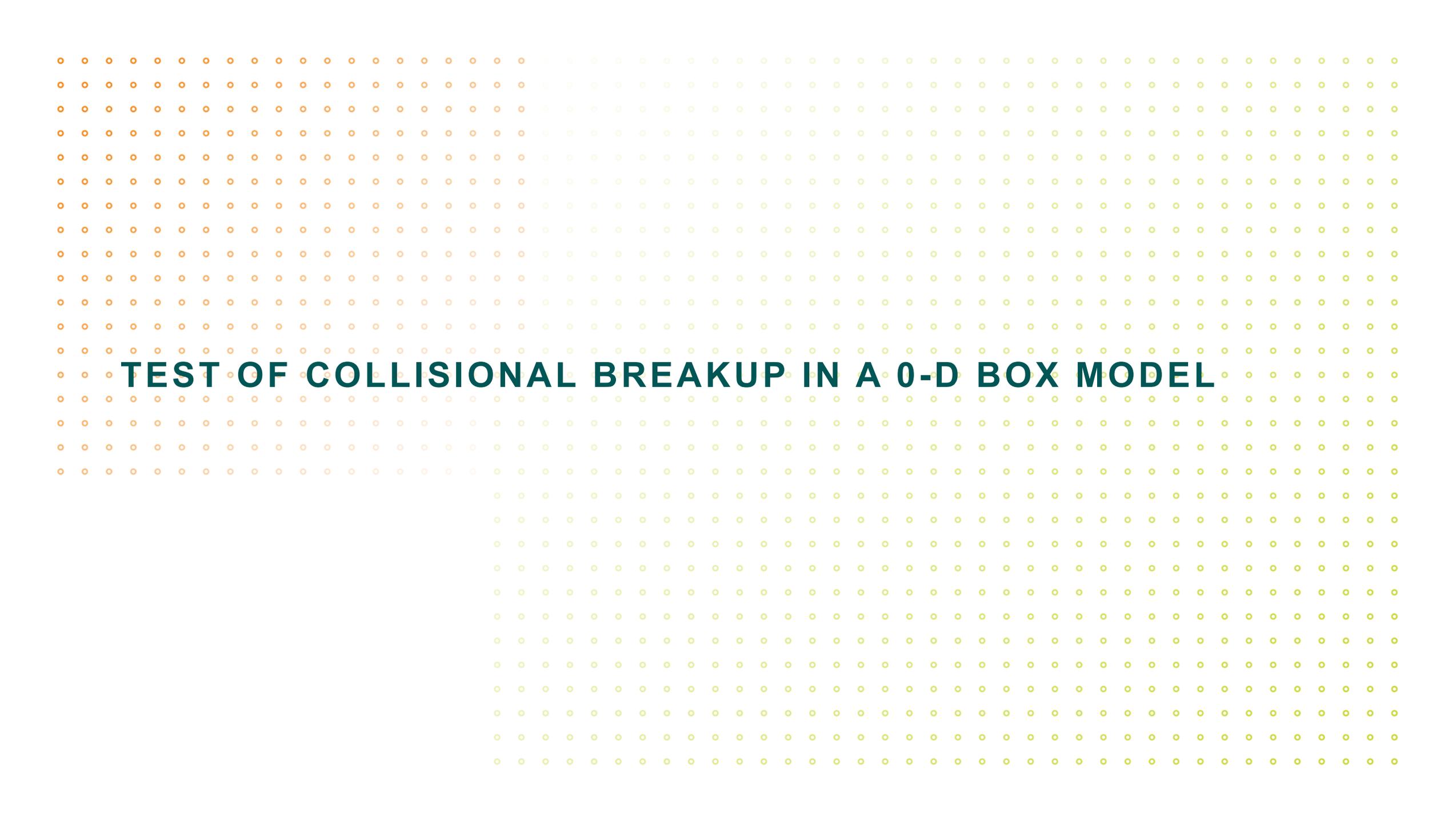
# COLLISION ENERGETICS DETERMINE OUTCOME, IF BREAKUP OCCURS, 'N<sub>FRAG</sub>' FRAGMENTS PRODUCED





# COLLISION ENERGETICS DETERMINE OUTCOME, IF BREAKUP OCCURS, 'N<sub>FRAG</sub>' FRAGMENTS PRODUCED

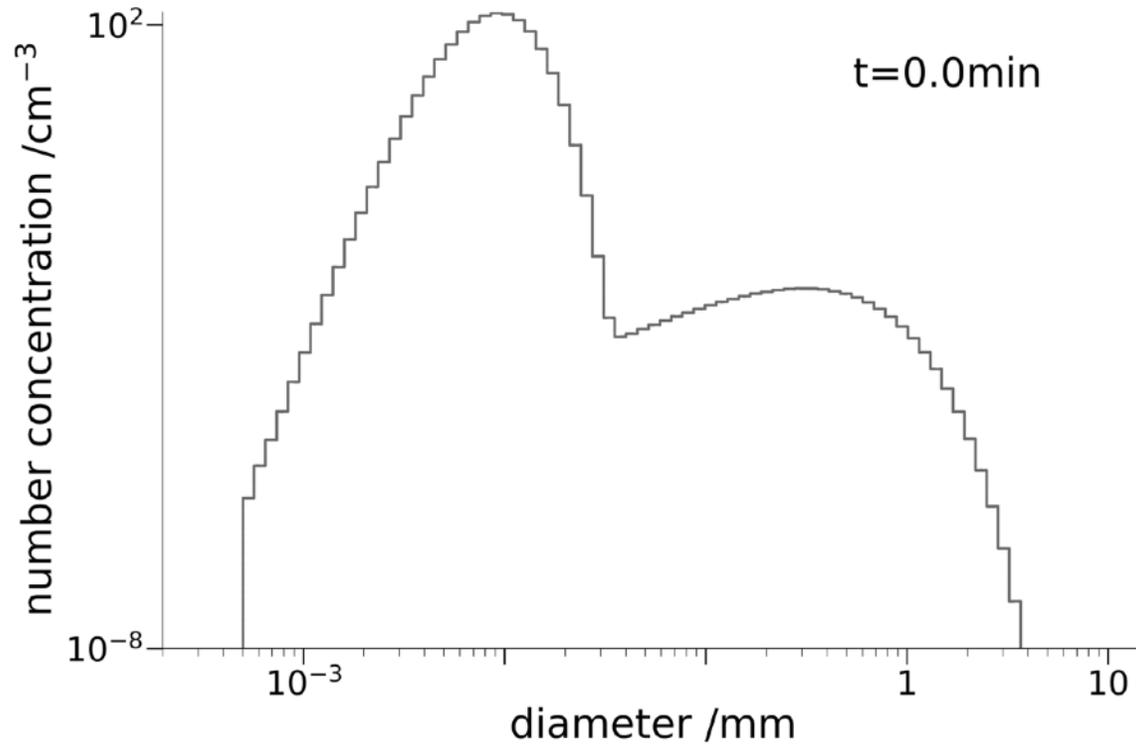




**TEST OF COLLISIONAL BREAKUP IN A 0-D BOX MODEL**



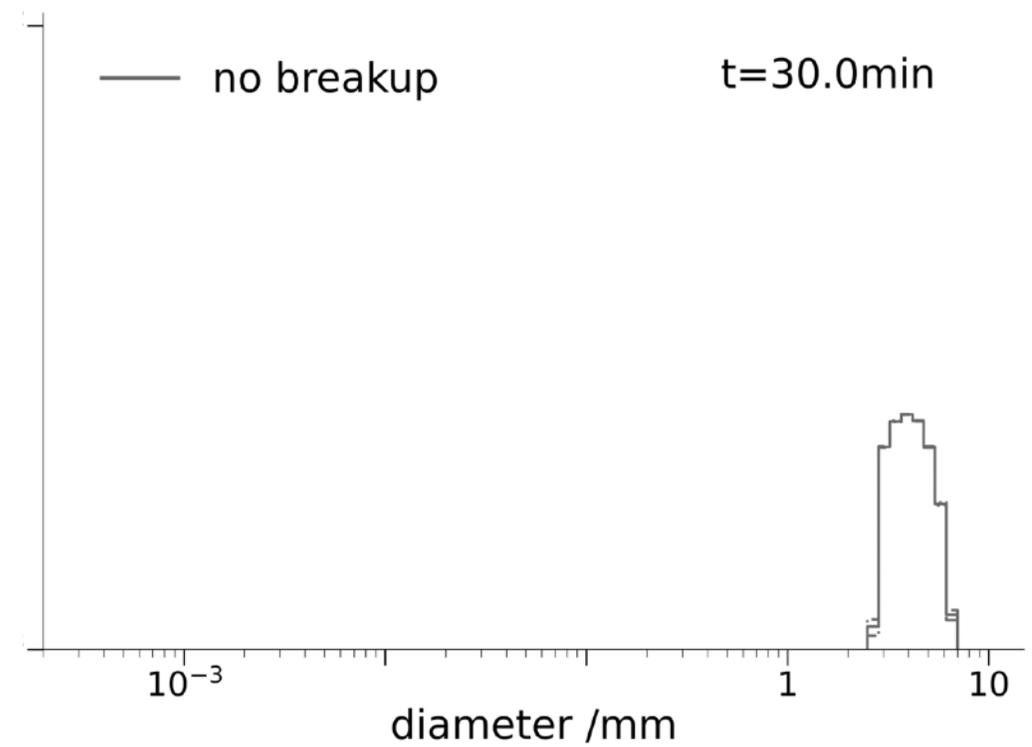
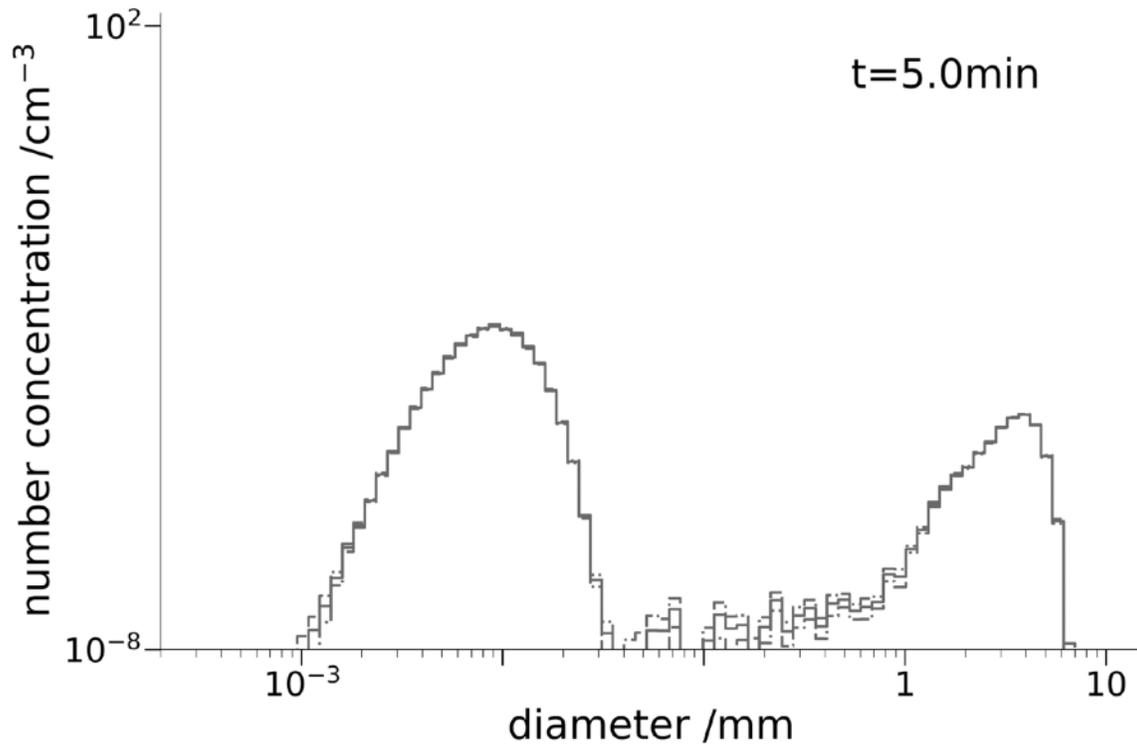
# 0-D BOX MODEL SETUP



- Mean over 15 runs of 4096 super-droplets
- Randomly initialised radii from cloud and raindrop distributions
- Initial droplet number concentration =  $1000 \text{ cm}^{-3}$  in  $8000 \text{ m}^3$
- $\Delta t_{\text{collisions}} = 0.5\text{s}$

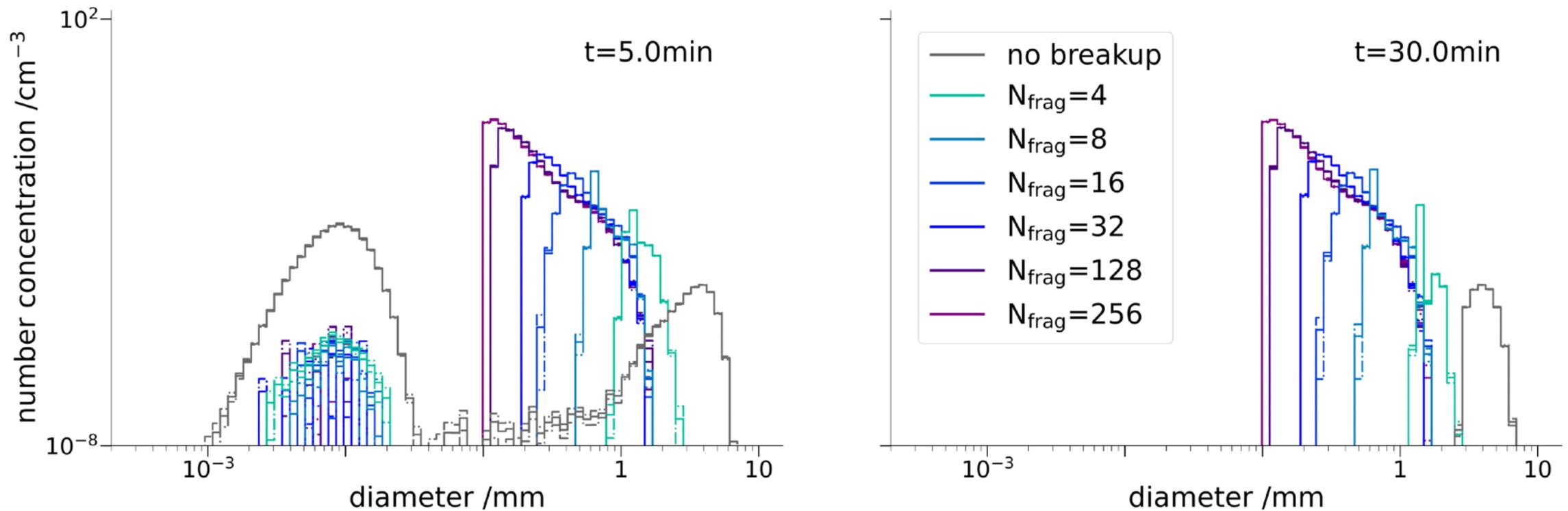


# WITHOUT BREAKUP DROPLETS GROW TO ~5MM



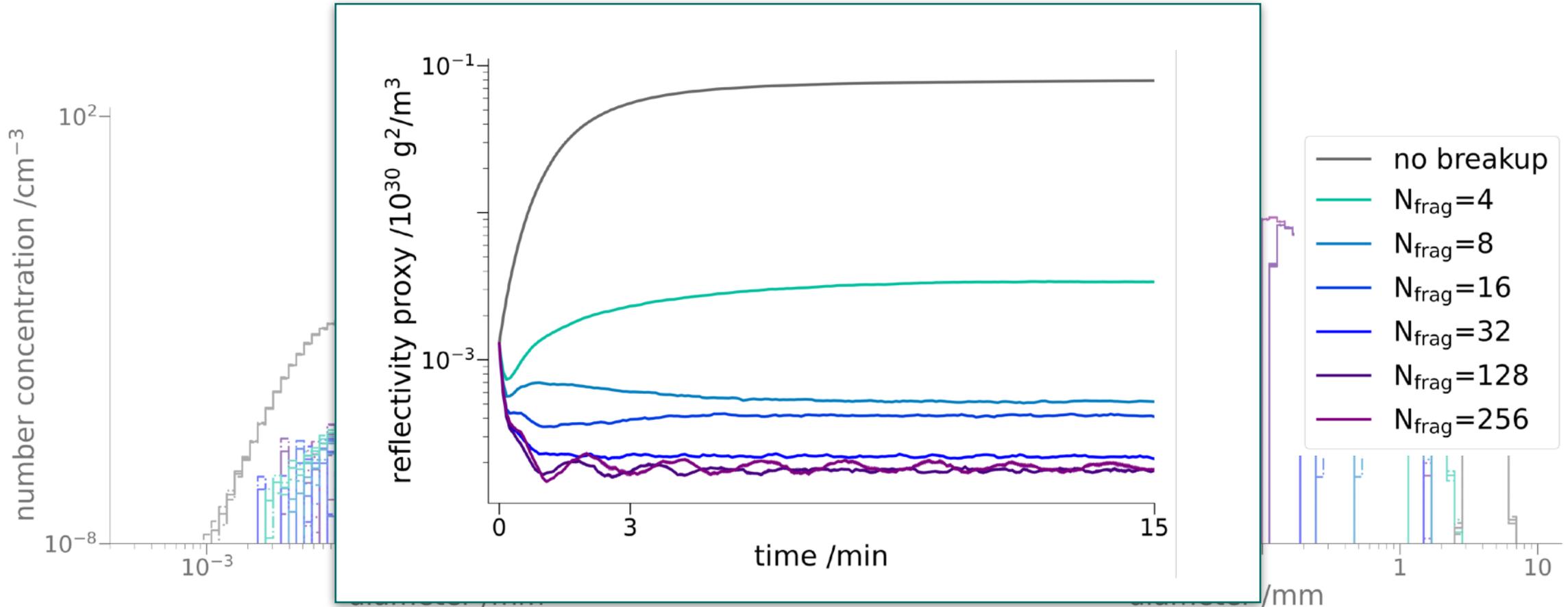


# BREAKUP BROADENS THE DROPLET SIZE DISTRIBUTION AND INHIBITS LARGE RAINDROPS



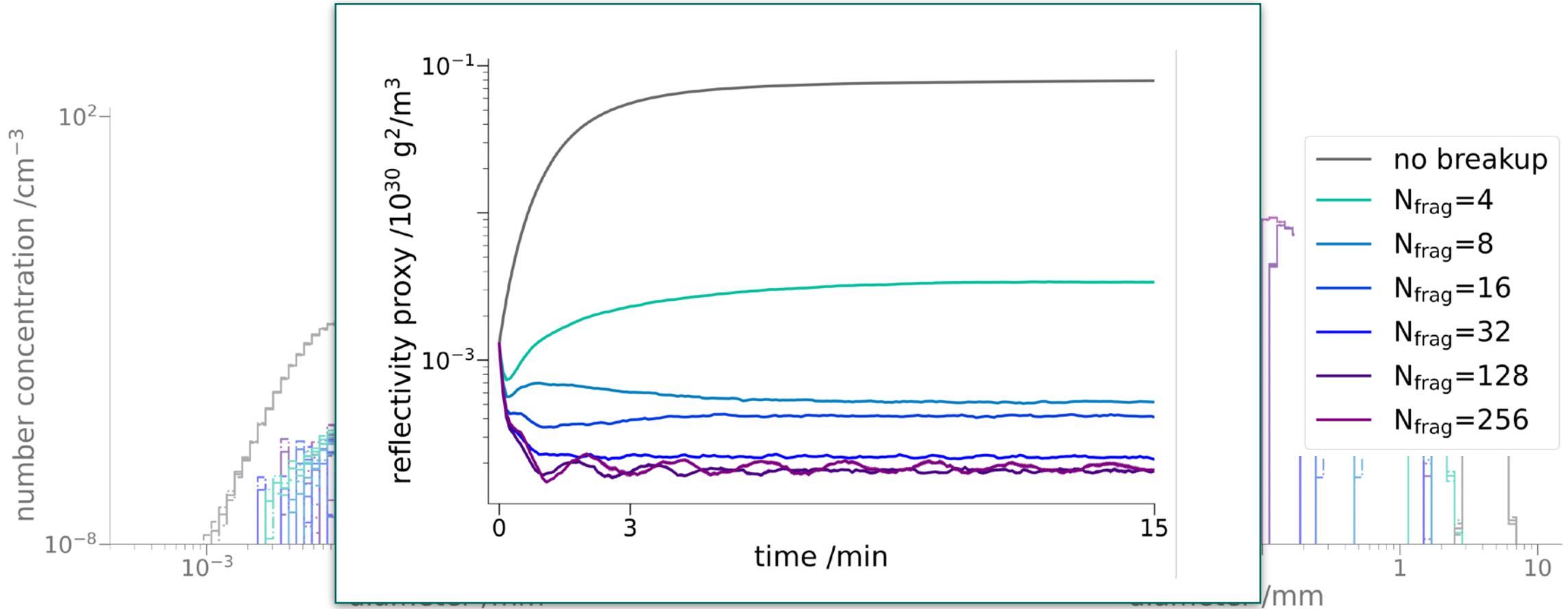


# DROPLET BREAKUP CAN STRONGLY ALTER RADAR REFLECTIVITY





# DROPLET BREAKUP CAN STRONGLY ALTER RADAR REFLECTIVITY



... also rain evaporation and thereby mesoscale cloud organisation?



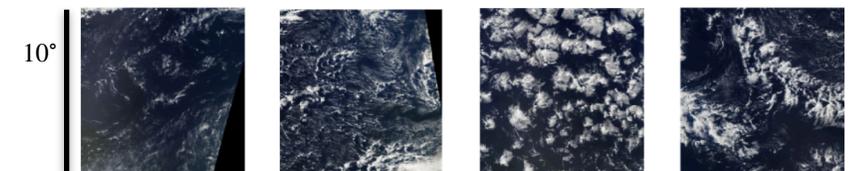
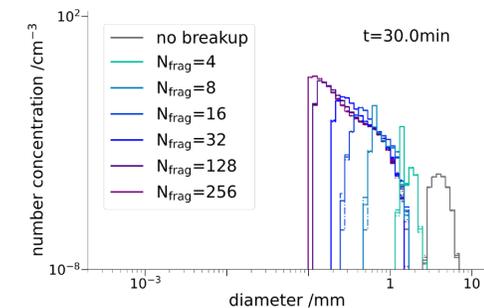
# INTRODUCING CLEO: A NEW SUPER-DROPLET MODEL WITH COLLISIONAL BREAK-UP

- CLEO's novel computational design targets SDM in large domain LES  $O(100\text{km})$
- Extended SDM collision algorithm includes rebound and breakup
- 0-D model shows breakup broadens the droplet size distribution and inhibits large raindrop formation

## Next steps:

- Coupling CLEO to ICON to study how shallow tropical cloud microphysics interacts with mesoscale cloud organisation
- Investigating implications of SDM on rain rates and evaporation

Open source!  
[yoctoyotta1024/CLEO](https://github.com/yoctoyotta1024/CLEO)





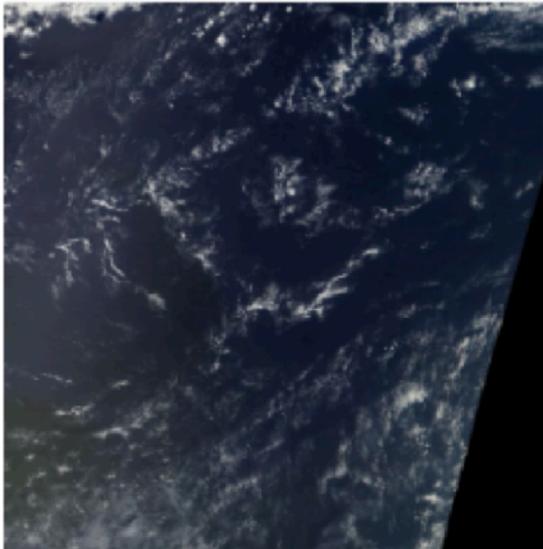
**BACK-UP SLIDES**



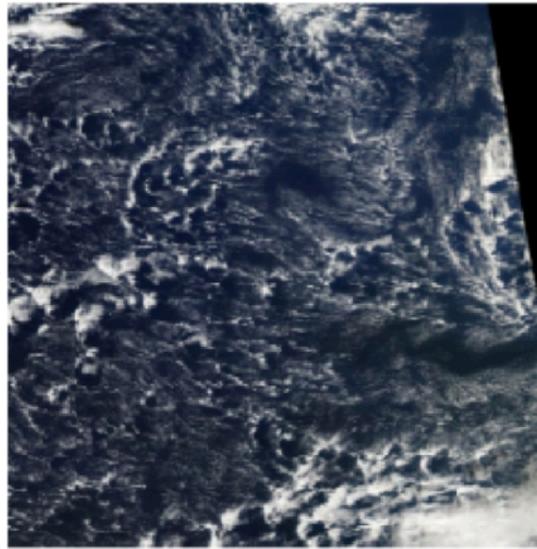
# CONVENTIONAL LES OF WARM RAIN IS HIGHLY UNCERTAIN AND INACCURATE

Mesoscale cloud organisation from EUREC4A:

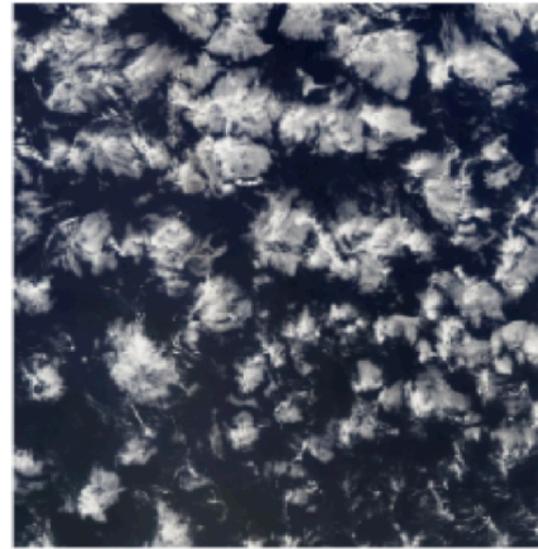
**Sugar** (MODIS/Terra 23 Feb 2010)



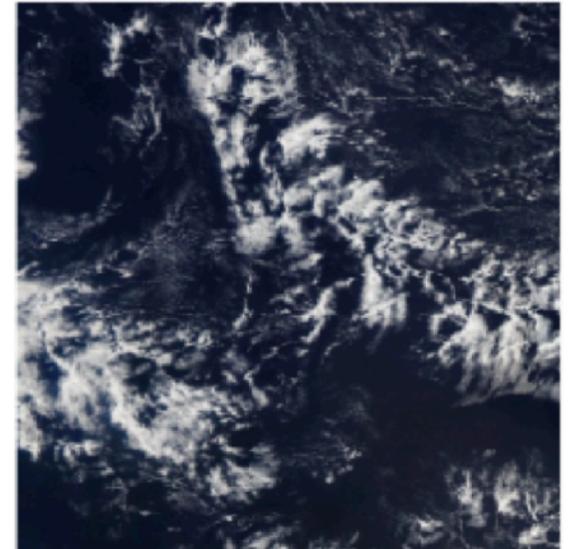
**Gravel** (MODIS/Aqua 19 Dec 2016)



**Flowers** (MODIS/Aqua 9 Feb 2017)



**Fish** (MODIS/Aqua 19 Jan 2011)

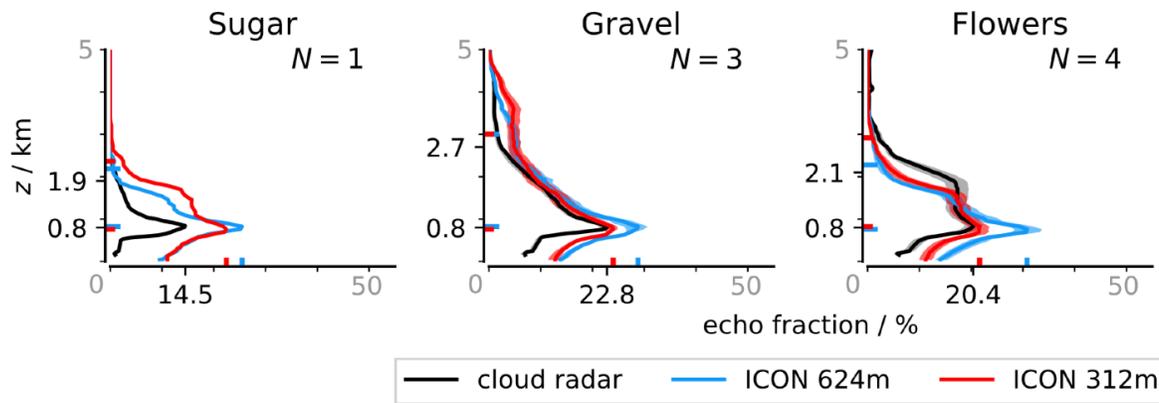


*(Stevens et al. 2019) Figure credit: Bony et al. 2020*

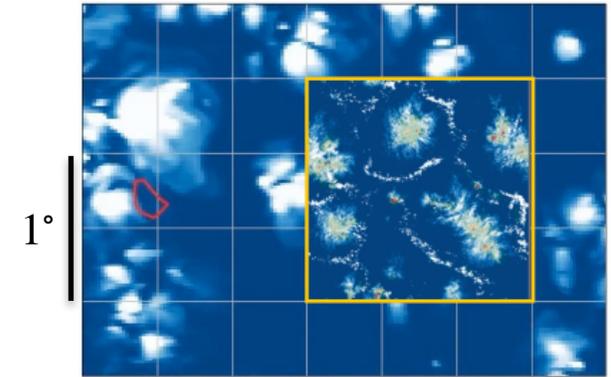


# CONVENTIONAL LES OF WARM RAIN IS HIGHLY UNCERTAIN AND INACCURATE

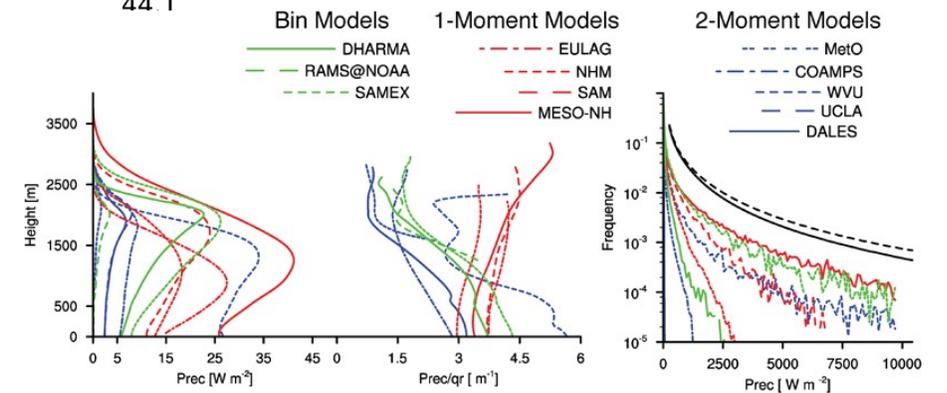
E.g. comparison of LES and EUREC<sup>4</sup>A observations:



(Schulz and Stevens 2023)



EUREC<sup>4</sup>A domain, credit: Alessandro Savazzi

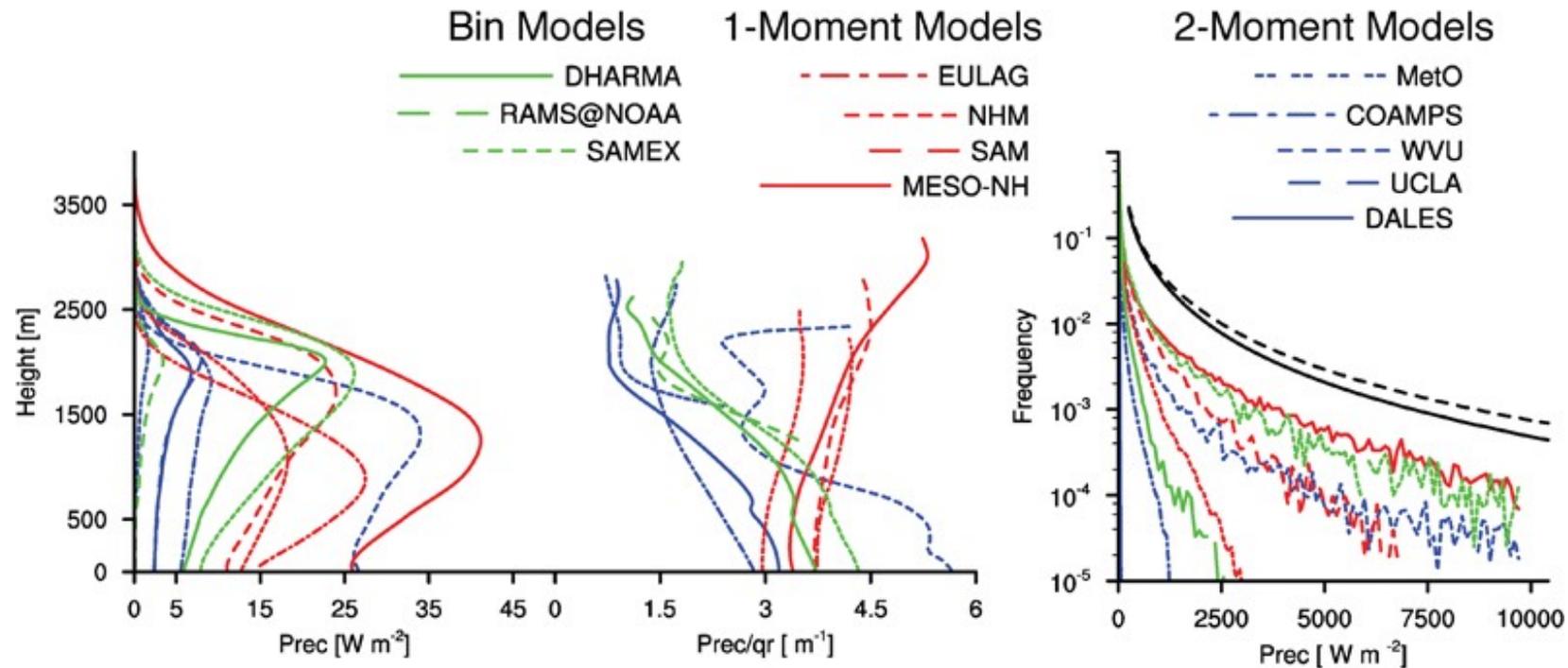


(van Zanten et al. 2011)



# CONVENTIONAL LES OF WARM RAIN IS HIGHLY UNCERTAIN AND INACCURATE

E.g. comparison of LES and RICO observations:



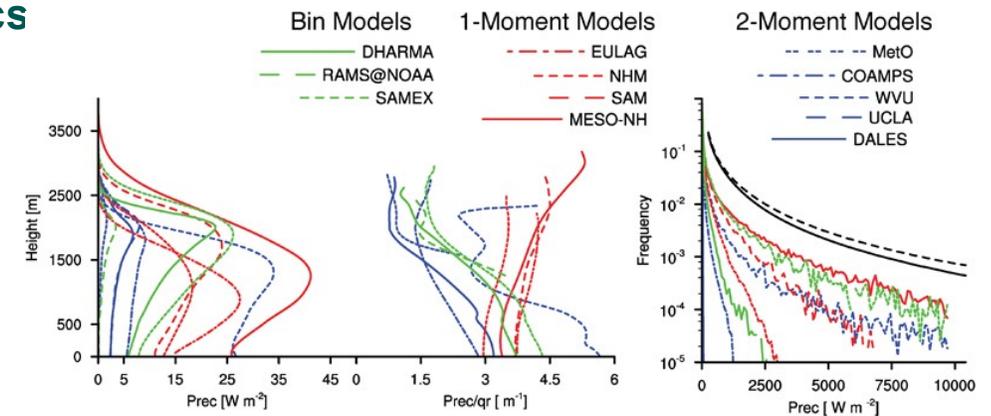
(van Zanten et al. 2011)



# THE SUPER-DROPLET MODEL (SDM) HAS SEVERAL MAJOR ADVANTAGES

Compared with conventional models for cloud microphysics  
SDM...

- has **less numerical ambiguity**
  - no numerical diffusion
  - greater fidelity to the underlying physics
- is **more suited to trends in High Performance Computing**
  - ~Linearly increasing computational cost
  - Highly parallelisable algorithms
- has **insightful convergence properties**



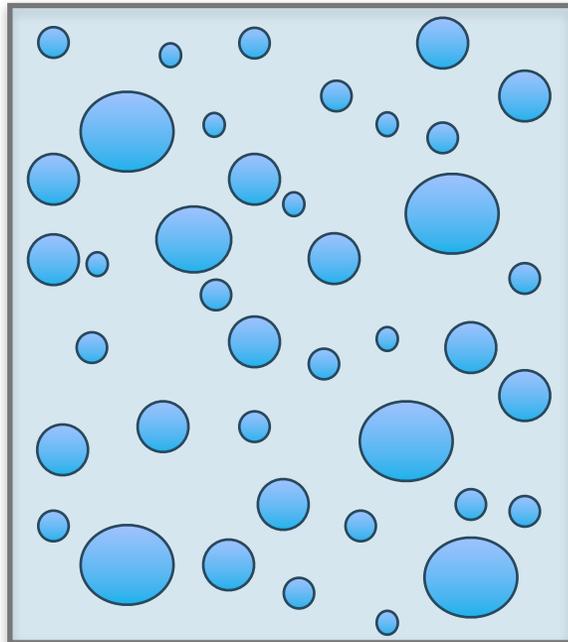
(van Zanten et al. 2011)



# THE SUPER-DROPLET MODEL (SDM) IS A FUNDAMENTALLY DIFFERENT VIEW OF CLOUD MICROPHYSICS

Reality

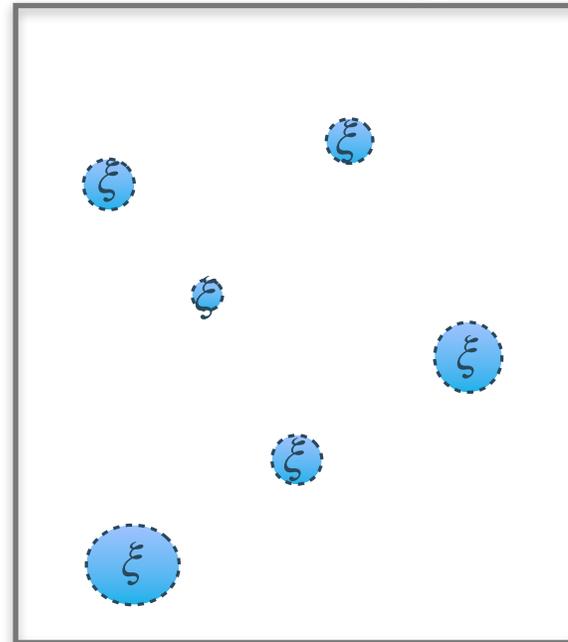
$N = 10^{15}$



SDM

$N = 10^{15}$

$N_{SD} = 10$



Each super-droplet has its own multiplicity,  $\xi$ ,

$$\xi = 1, 2, 3, \dots, \xi$$

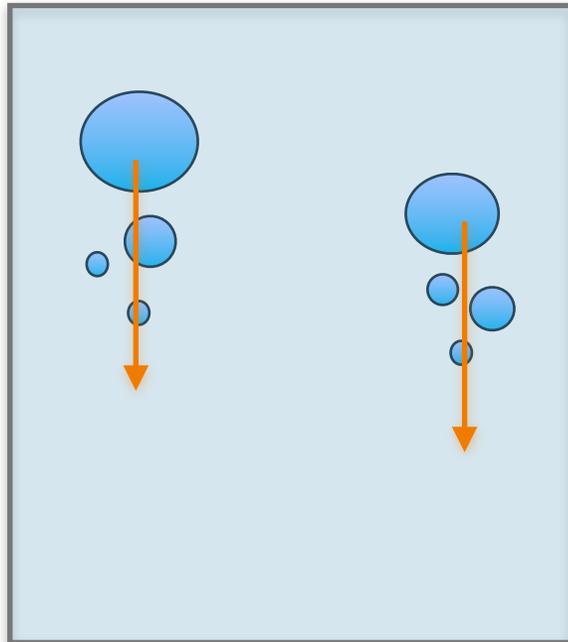
1 super-droplet =  $\xi$  real droplets

Shima et al. 2009

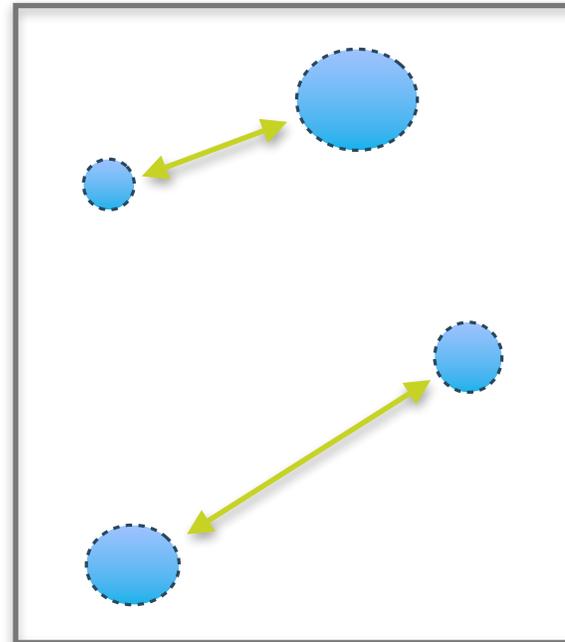


# COLLISION-COALESCENCE IN SDM IS PROBABILISTIC

Reality



SDM



- Randomly pair all the super-droplets in a gridbox
- For each  $ij$  pair:
  1. Calculate SDM collision probability,  $P_{ij}^{(SDM)}$
  2. Random number determines coalescence or not
  3. Update super-droplet properties accordingly



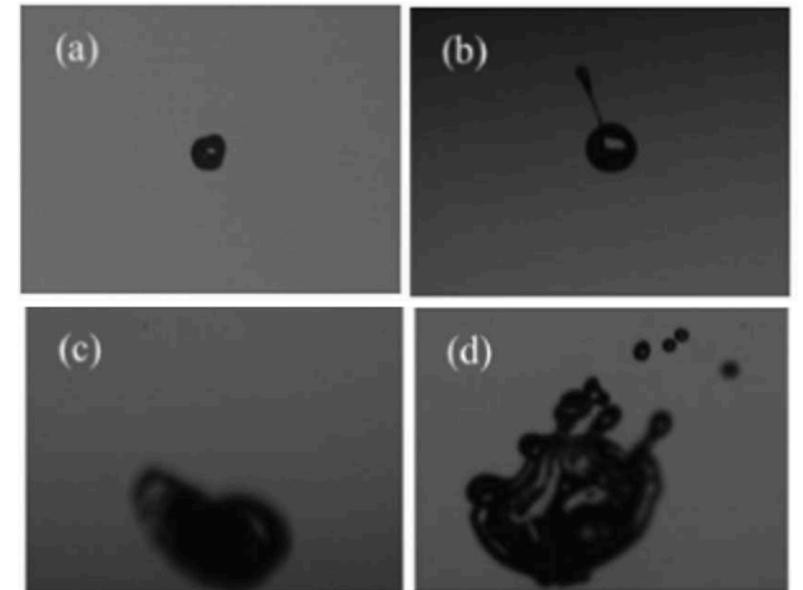
# COLLISIONAL BREAKUP MAY SUBSTANTIALLY ALTER THE DROPLET SIZE DISTRIBUTION

Collisional breakup:

- is **observed in rainfall events**
- **delays rain formation** and **decreases rain rates** in LES
- prevents unphysical large droplets and provides source of smaller droplets

Therefore could:

- Alter **radar reflectivity-rain-rate (Z–R)** relations
- Effect **rain evaporation rates** and thereby **mesoscale cloud organisation**



*(Testik and Rahman 2017)*

Testik and Rahman (2017), Seifert et al. (2005), McFarquhar (2004), Straub and Beheng (2010), Szakáll and Urbich (2018)



# LAB EXPERIMENTS LACK CLOUD DROPLET DATA

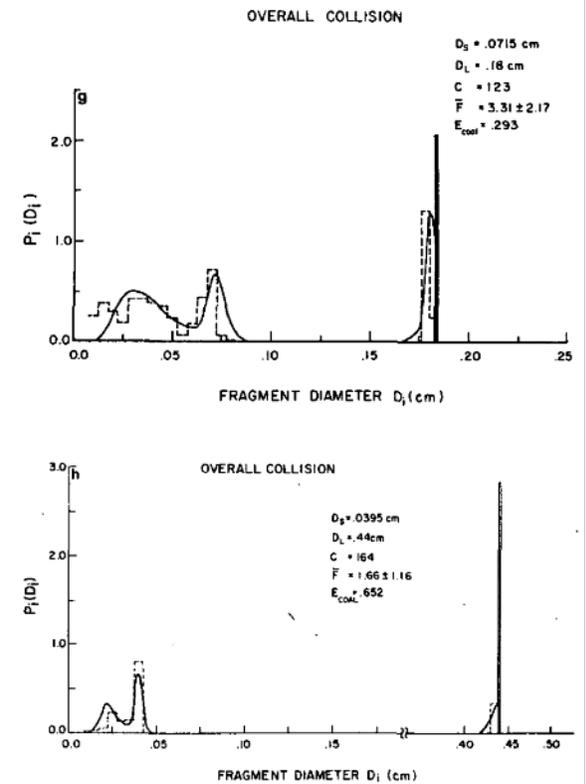
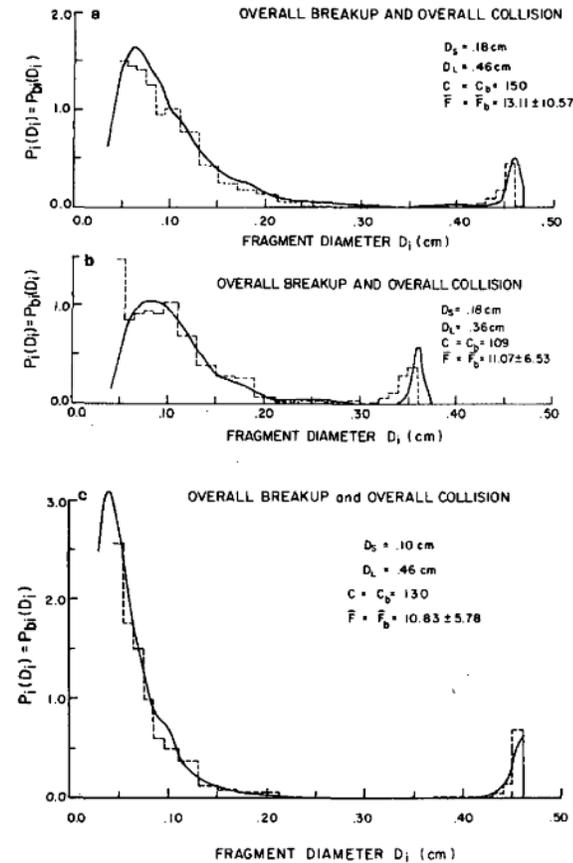
Measure fragment sizes and breakup probabilities but...

Apparatus sensitivity is 100 - 500 microns!

Very limited sample!

“applying the Low and List parameterisation to small drops would lead to an unrealistic overestimation of collisional breakup”

(Seifert et al., 2005)

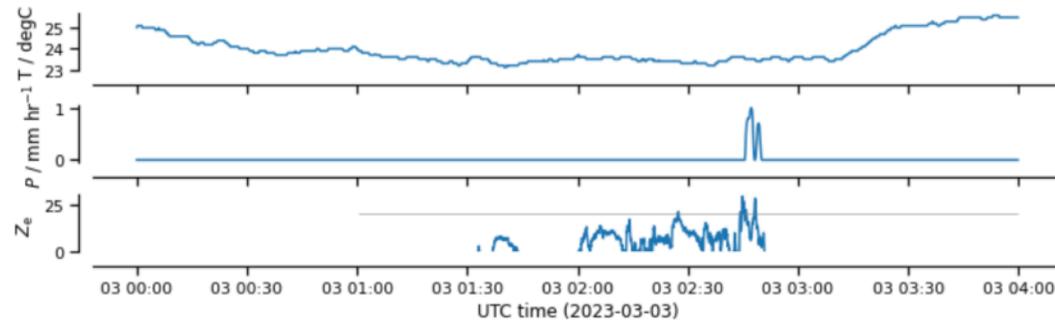


Low and List (1982)

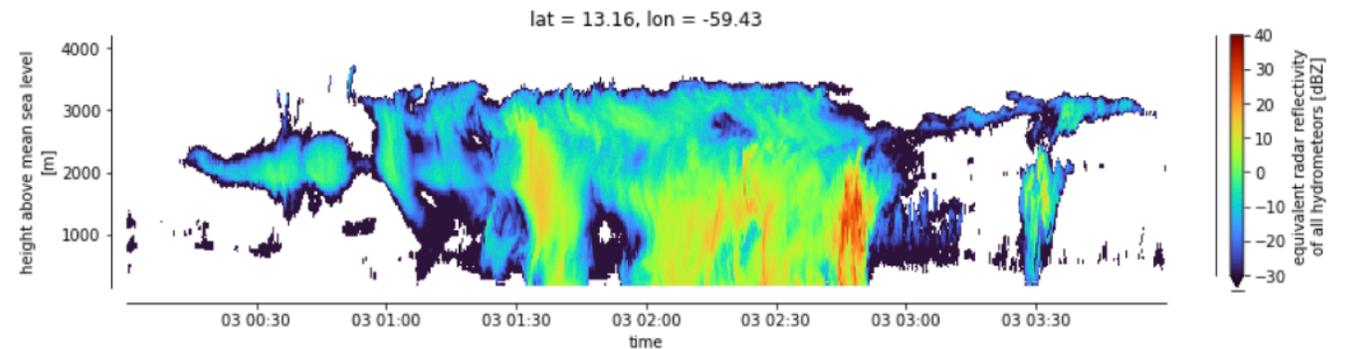


# BCO RADAR REFLECTIVITY SIGNAL

Credit: Bjorn Stevens <https://bjorn-stevens.github.io/TCODATA-fun-and-easy.slides.html#/2/2>



Random 2-day sample of BCO data from March 2023. Notice how much radar signal is detected without precipitation ( $Z < 15\text{dB}$ )

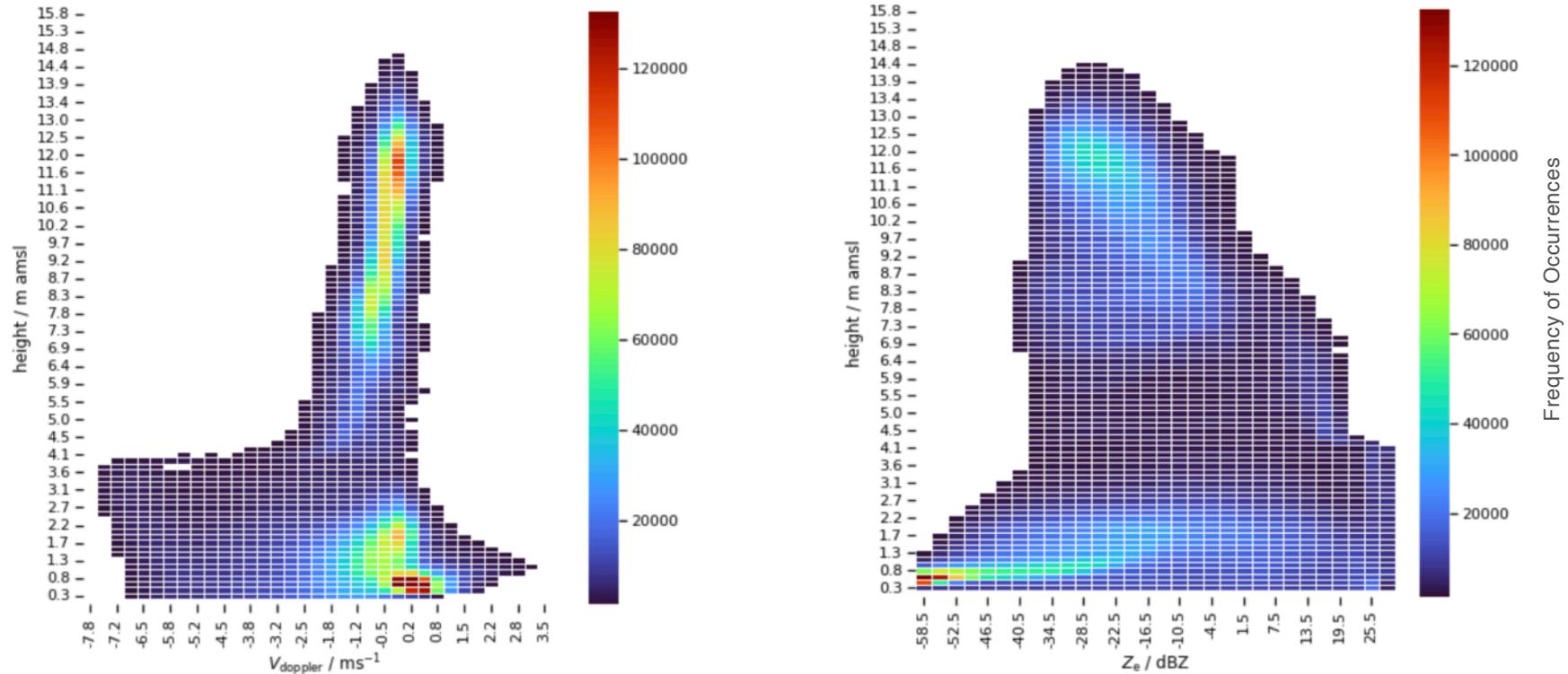


Interesting time-slice from BCO radar data in March 2023. Notice the signal from a strong up draught feature on 3rd March at 03:30



# BCO RADAR REFLECTIVITY SIGNAL AND DOPPLER VELOCITY

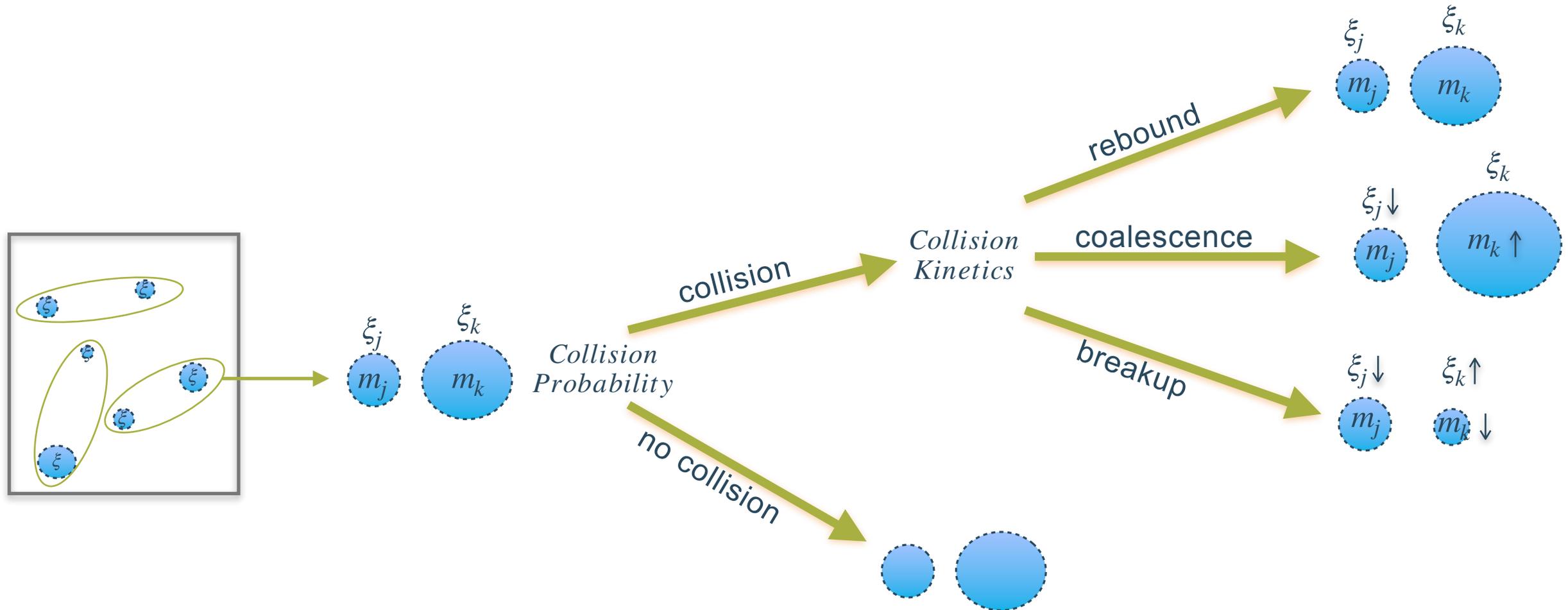
Credit: Bjorn Stevens <https://bjorn-stevens.github.io/TCODATA-fun-and-easy.slides.html#/2/2>



Histograms of all data from Dec 2022 to mid March 2023 (nearly 4 million time stamps!)



# EXTENSION TO INCLUDE REBOUND AND BREAKUP IN CLEO





# OUTCOME OF COLLISIONS DETERMINED BY COLLISION ENERGETICS, IF BREAKUP OCCURS ‘ $\Omega$ ’ FRAGMENTS PRODUCED

## “Collision Energetics”:

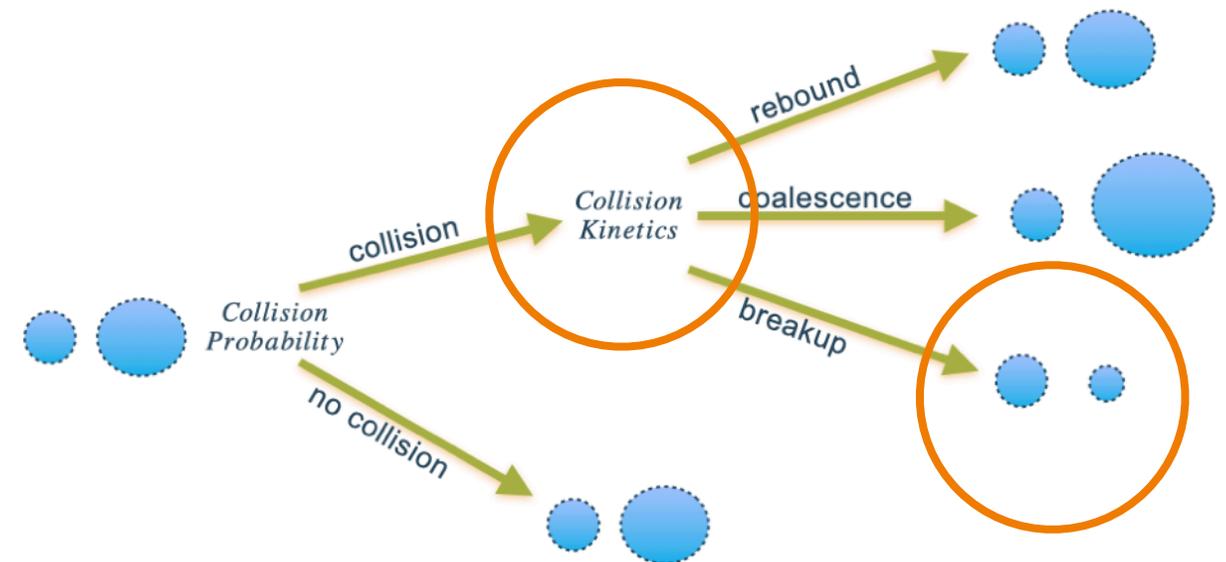
- Function of initial super-droplet attributes  
e.g. comparison of surface tension energy to their collision kinetic energy

## Super-droplet attributes after breakup:

- Function of initial super-droplet attributes  
e.g. ‘ $\Omega$ ’ fragments produced

## For computational tractability:

- Conserves super-droplet number
- Deterministic and non-iterative

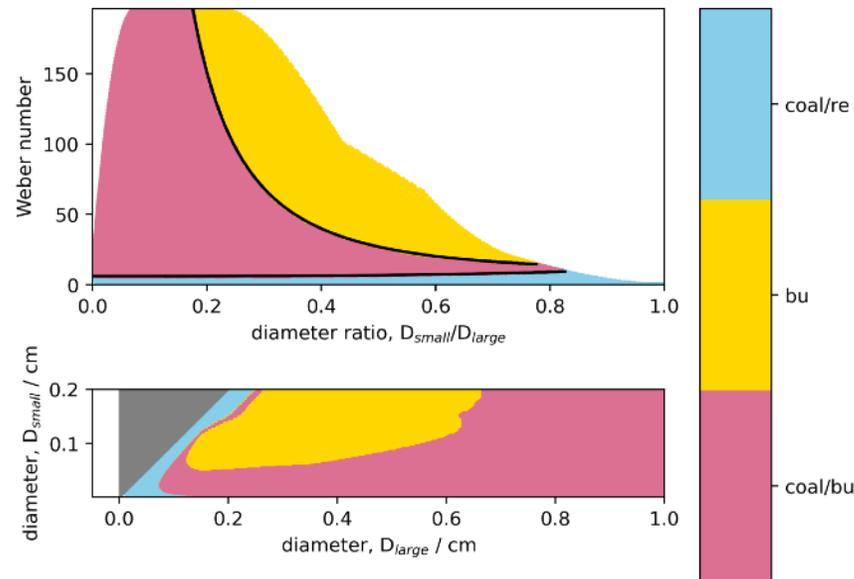




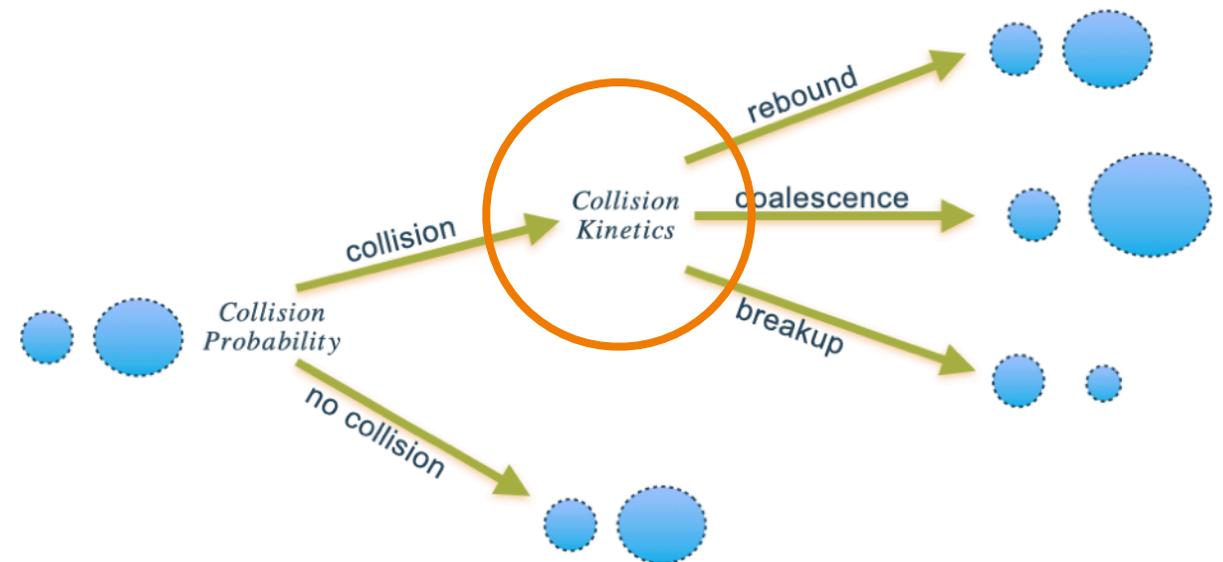
# OUTCOME OF COLLISIONS DETERMINED BY COLLISION ENERGETICS, IF BREAKUP OCCURS ‘ $\Omega$ ’ FRAGMENTS PRODUCED

## “Collision Energetics”:

- **Function of initial super-droplet attributes**  
e.g. comparison of their surface tension energy to collision kinetic energy

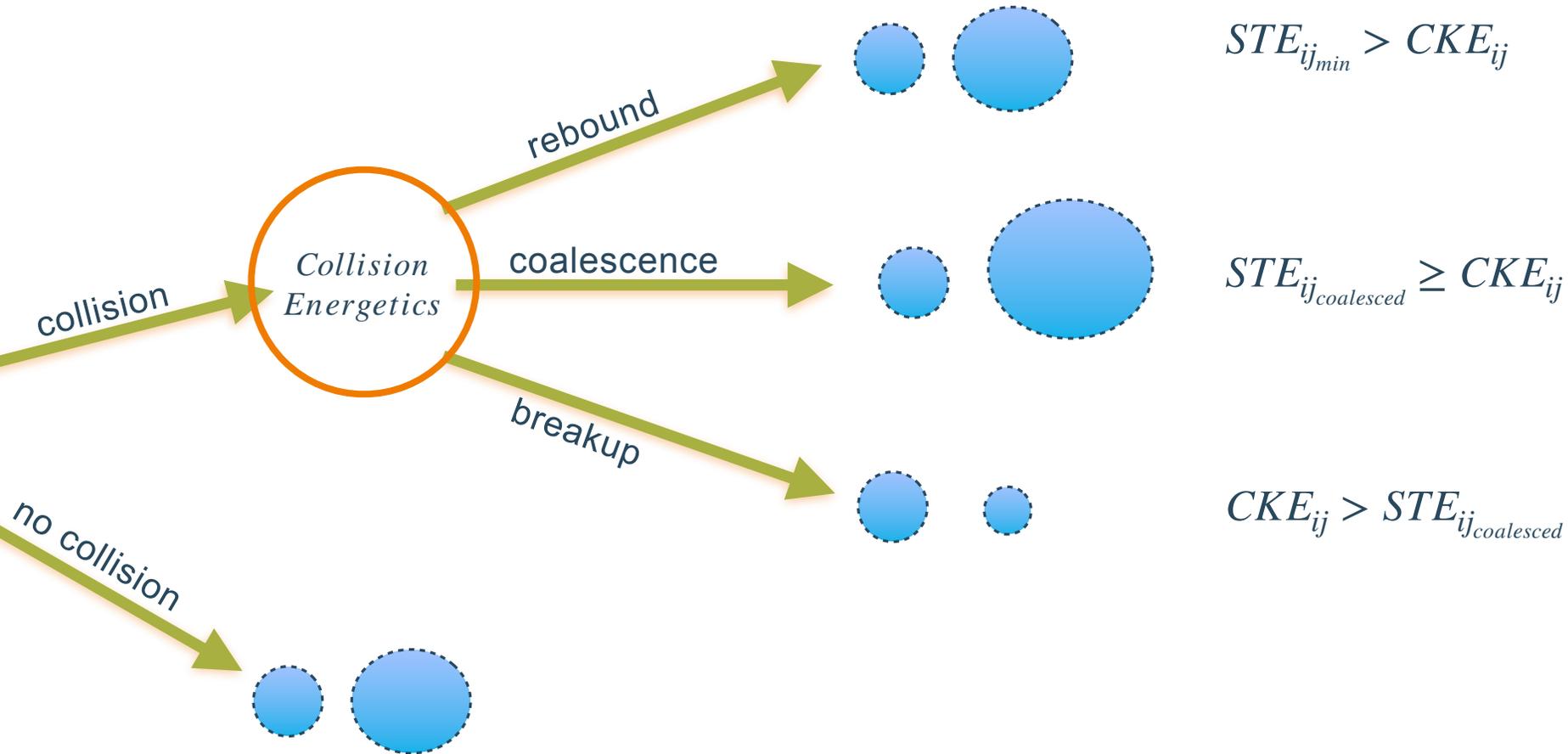


(Testik et al. 2009)





# COLLISION ENERGETICS DETERMINE OUTCOME



$$STE_{ij_{min}} > CKE_{ij}$$

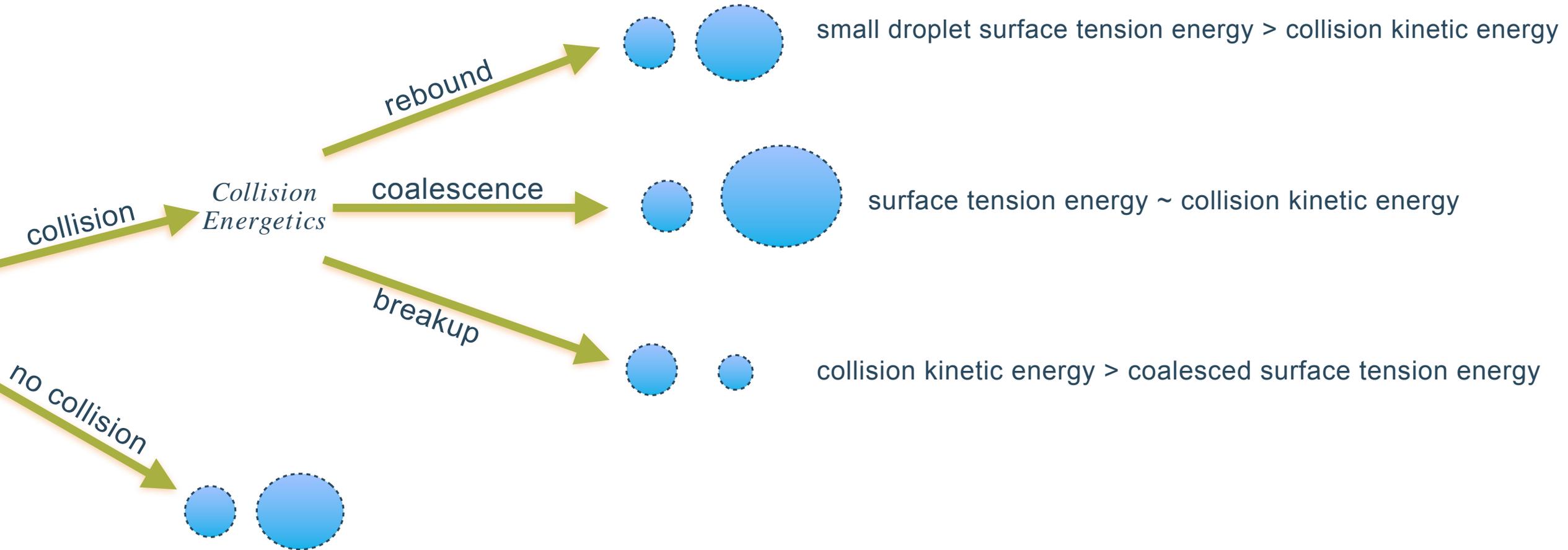
$STE_{ij}$  = surface tension energy  
 $CKE_{ij}$  = collision kinetic energy

$$STE_{ij_{coalesced}} \geq CKE_{ij}$$

$$CKE_{ij} > STE_{ij_{coalesced}}$$



# COLLISION ENERGETICS DETERMINE OUTCOME

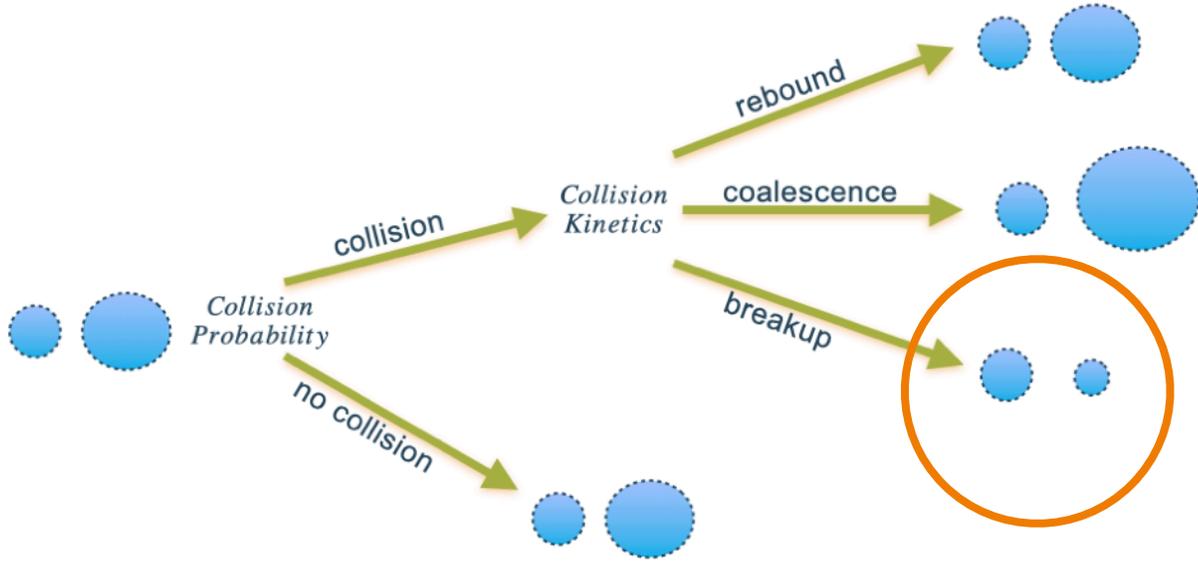
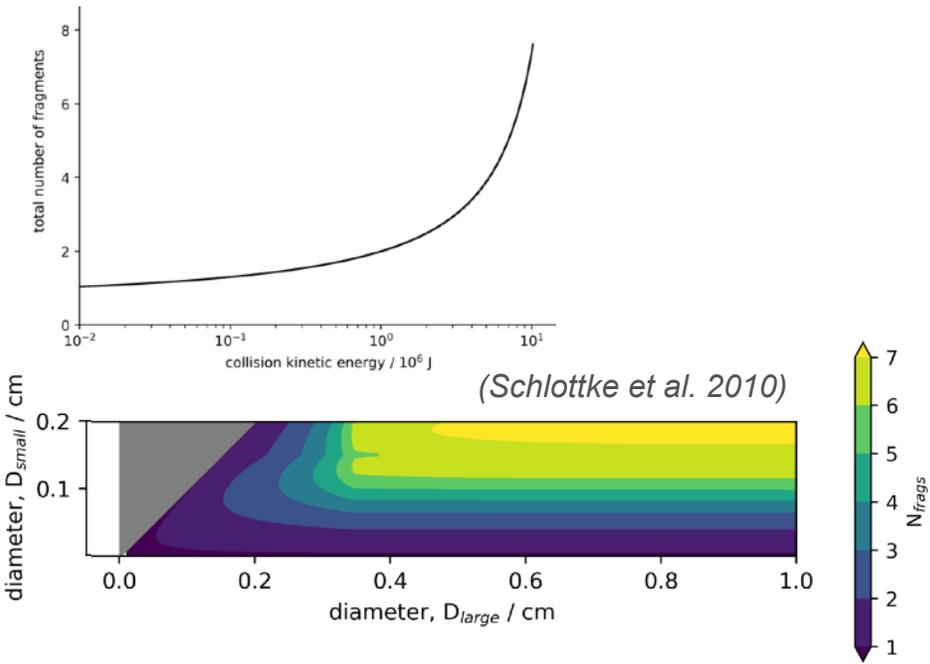




# OUTCOME OF COLLISIONS DETERMINED BY COLLISION ENERGETICS, IF BREAKUP OCCURS ‘ $\Omega$ ’ FRAGMENTS PRODUCED

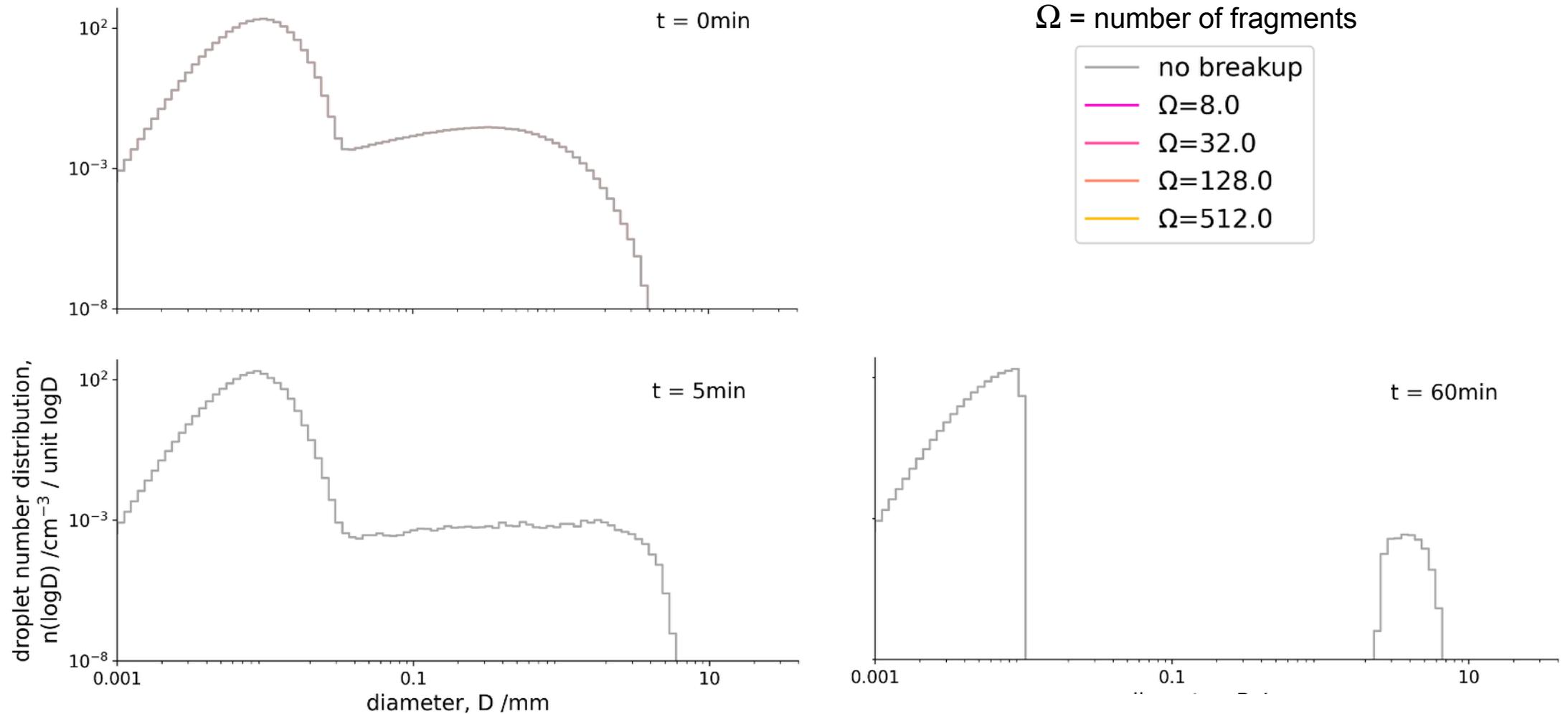
## Super-droplet attributes after breakup:

- Function of initial super-droplet attributes e.g. ‘ $\Omega$ ’ fragments produced



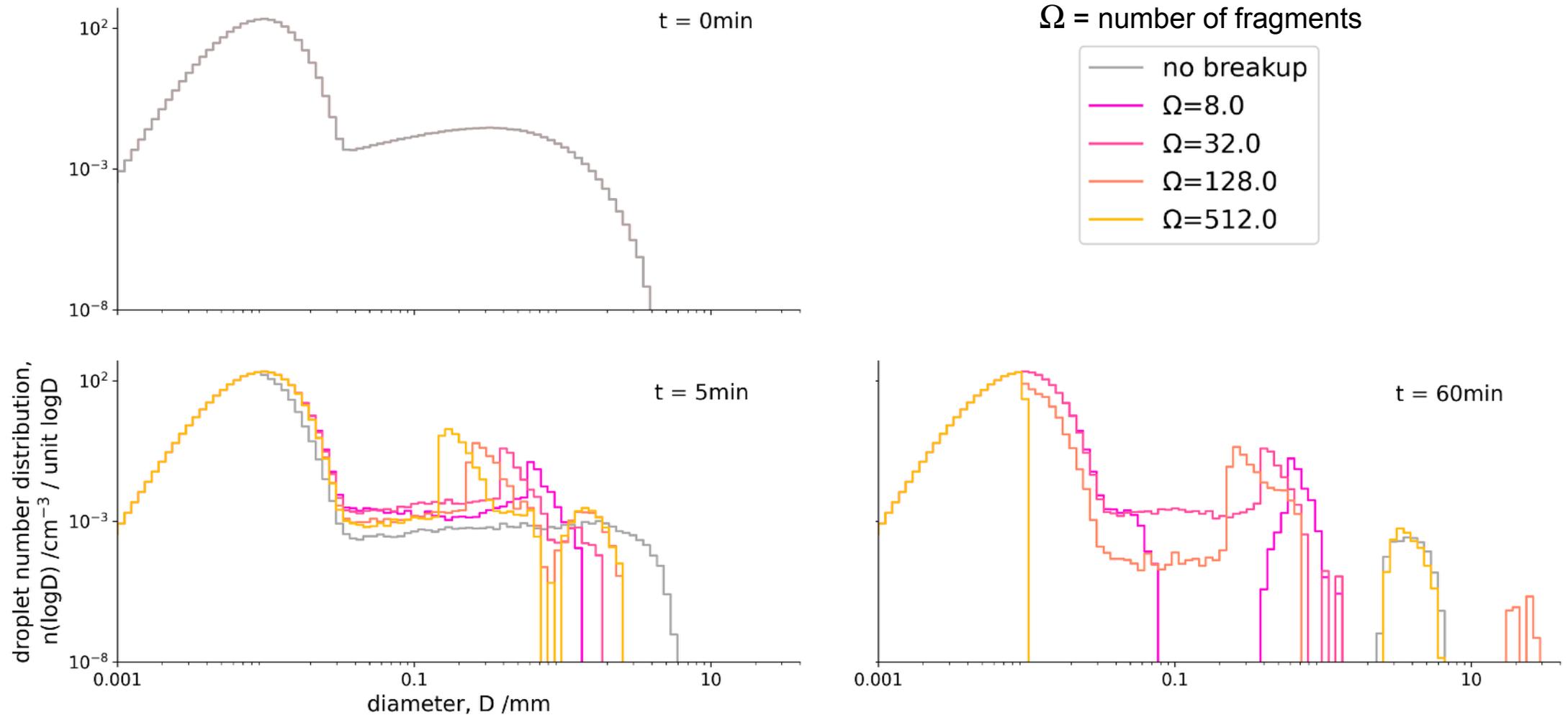


# 0-D BOX MODEL: FRAGMENTS FROM BREAKUP CAN EITHER INHIBIT OR PROMOTE THE FORMATION OF LARGE RAINDROPS



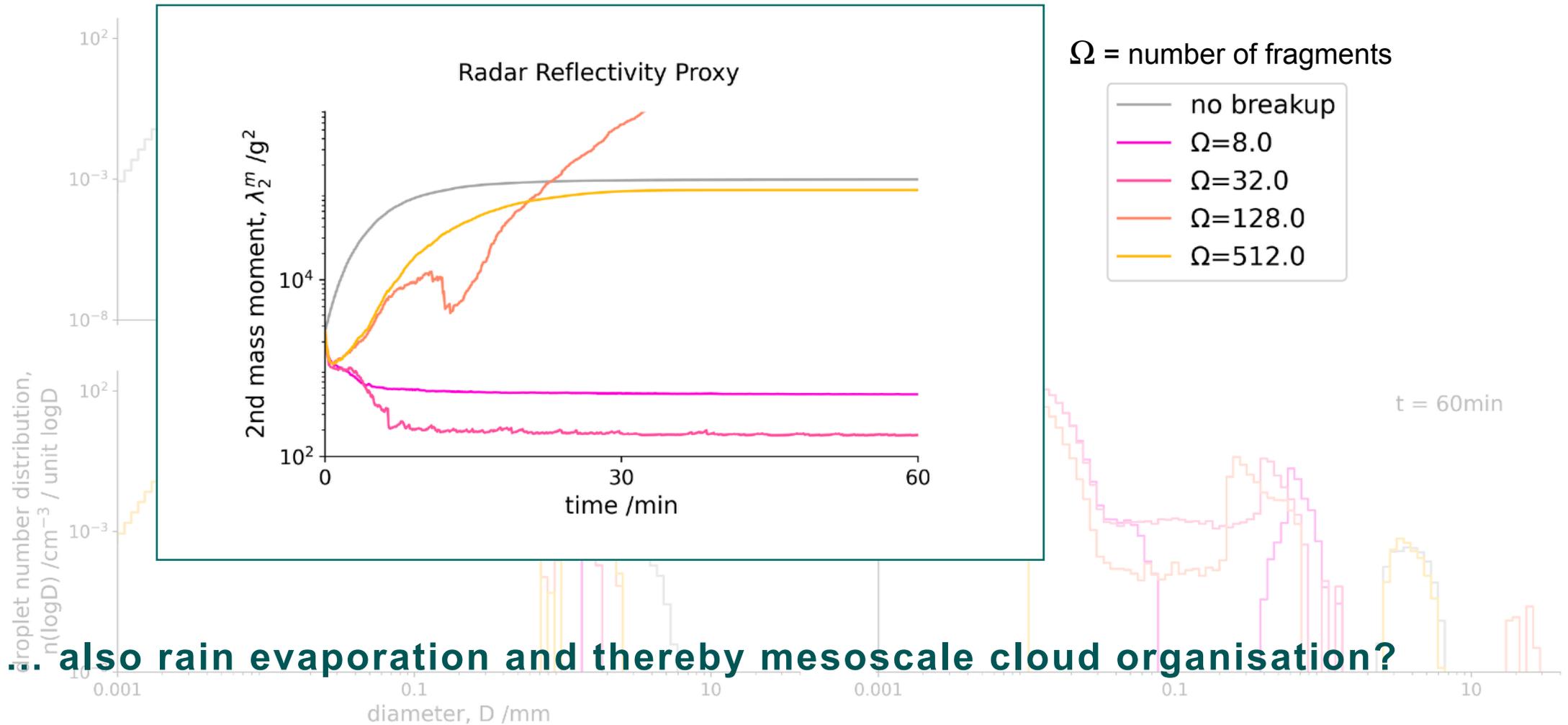


# 0-D BOX MODEL: FRAGMENTS FROM BREAKUP CAN EITHER INHIBIT OR PROMOTE THE FORMATION OF LARGE RAINDROPS



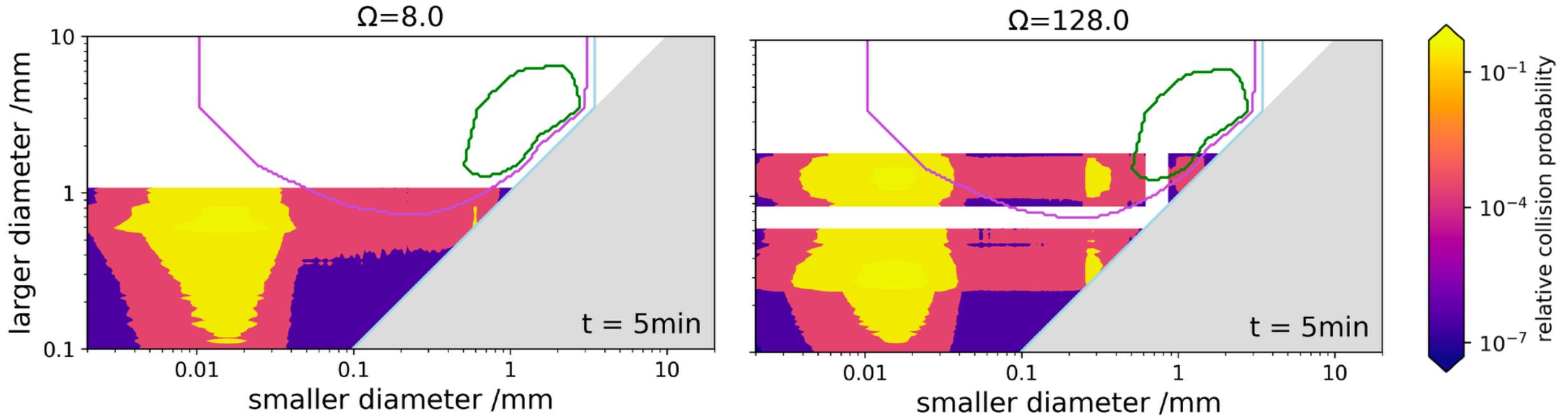


# DROPLET BREAKUP CAN STRONGLY ALTER RADAR REFLECTIVITY





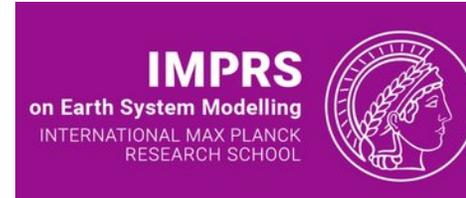
# FRAGMENTS “FEED” EITHER COALESCENCE OR REBOUND



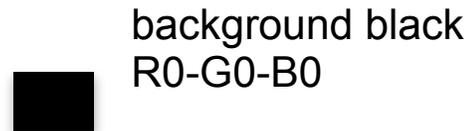
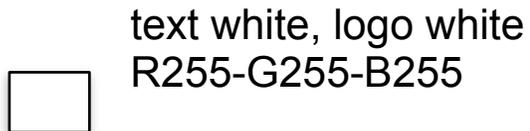
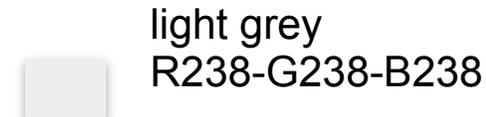
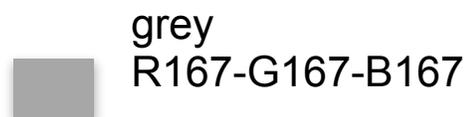
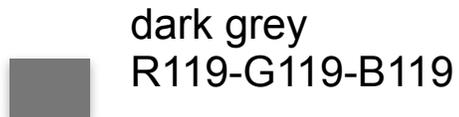
(See CPH Seminar 28.08.2023...)

# Color values Max Planck Institute for Meteorology from 2022

## Main colors



## Accompanying colors



## Accent colors

