

Abstract

The modern workforce is under relentless pressure to constantly acquire new skills and knowledge necessary to get the job done. Atmospheric science is not exempt. A typical practitioner must not only understand atmospheric physics (which alone has many branches) and its underlying mathematics (sophisticated), but also details of numerical techniques, and possess basic software engineering skills (for code development). Many classic books and papers in all branches of atmospheric and computer science are available. But that is partially the problem: there are too many. When switching between branches of atmospheric science (due to collaboration or change of projects), **nobody has time for deep immersion** in relevant literature. Also, successful completion of a project still requires understanding at the level of code developer (because using "black boxes" and "spaghetti codes" is unprofessional, risky, and counterproductive). Many of these theoretical papers are not written from the point of view of turning theory into workable, maintainable code.

In this talk we discuss two papers describing numerical simulation of two fundamental physical processes in the atmosphere: multiple scattering of solar light, and absorption by atmospheric trace gases. Following the format of "*Numerical* Recipes" by Press et al., our papers bundle small pieces of necessary theory with corresponding snippets of code. These are arranged in an order that is natural for code development, which is often opposite of the natural order for laying out the theoretical basis. The first paper has been published in 2022, while the second is a work in progress which we intend to finish in 2024. The goal of both papers is to simplify the transfer of knowledge from seniors to juniors, and exchange skills between experts from different branches of Earth science. The codes are open source to be a learning resource available to all.

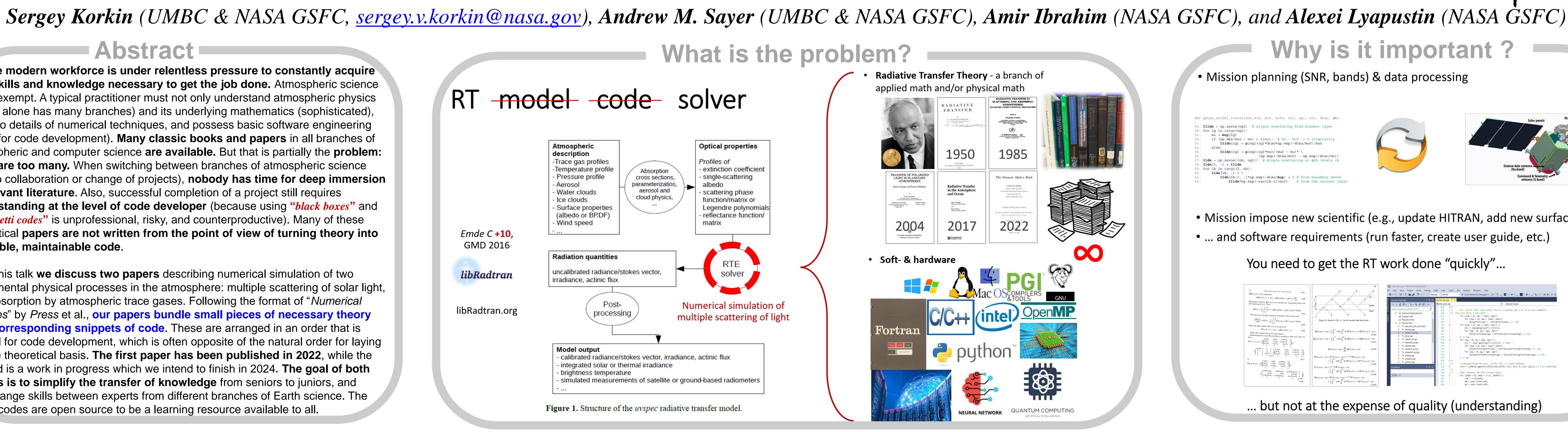
	Contents lists available at ScienceDirect	
Comp	uter Physics Communications	•
SEVIER	www.elsevier.com/locate/cpc	
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ture article practical guide to writing a	radiative transfer code <sup>☆,☆☆</sup>	•
Korkin <sup>a,b,*</sup> , A.M. Sayer <sup>a,b</sup> , A. Ibrahi	Check for	
, ,	S. Korkin, A.M. Seyer, A. Ibrahim et al. Computer Physics Communications 271 (2022) 108198	
	<ol> <li>import numpy as np</li> <li>from numba import jit</li> <li>@jit(nopython=True, cache=True)</li> <li>dof loconduc polymorial(r, know);</li> </ol>	•
	<pre>4. def legendre_polynomial(x, kmax): 5.</pre>	•
Sec. 17.2	8. $\mathbf{pk}[0] = 1.0$ 9. $\mathbf{elif} \ \text{kmax} = 1:$ 10. $\mathbf{pk}[0] = 1.0$ 11. $\mathbf{pk}[1] = \mathbf{x}$	
7146-655	12. else: 13. pk[0] = 1.0 14. pk[1] = x	
NG CASE	<pre>15. for ik in range(2, nk): 16. pk[ik] = (2.0 - 1.0/ik)*x*pk[ik-1] - \ 17. (1.0 - 1.0/ik)*pk[ik-2] 18. return pk</pre>	
	Fig. 8. Python function to compute ordinary Legendre polynomials for a given scalar value x and all orders $k = 0, 1, 2 \dots$ kmax.	S. Korkin, A.M. So
	Table 2Explicit expressions for a few low-order associated polynomials $Q_k^m(x)$ , Eq. (14). $k$ $m = 1$ $m = 2$ $m = 3$	
Link to paper	$\begin{array}{cccccc} 0 & 0 & 0 & 0 \\ 1 & \sqrt{(1-x^2)/2} & 0 & 0 \\ 2 & 3x\sqrt{(1-x^2)/6} & 3(1-x^2)/\sqrt{24} & 0 \\ 3 & 3(5x^2-1)\sqrt{(1-x^2)/3/4} & 15x(1-x^2)/\sqrt{120} & 15(1-x^2)^{3/2}/\sqrt{720} \end{array}$	
	$\frac{4 - \sqrt{5}x(3 - 7x^2)\sqrt{(1 - x^2)/4} + 15(7x^2 - 1)(1 - x^2)/\sqrt{1440} + 105x(1 - x^2)^{3/2}/\sqrt{5040}}{105x(1 - x^2)^{3/2}/\sqrt{5040}}$	
	$(k-m)P_k^m(x) = (2k-1)xP_{k-1}^m(x) - (k+m-1)P_{k-2}^m(x) $ (12) provided expressions for lower degree <i>k</i> and given order <i>m</i> are known. For all <i>m</i> < <i>k</i> , $P_k^m(x) = 0$ by definition due to <i>m</i> -th derivative of the <i>k</i> -order ordinary Legendre polynomial $P_k(x)$ . The analytical expression is known for $k = m$ (e.g., see Eq. (6.8.8) in [80,81])	
国際家国	$P_m^m(x) = (-1)^m (2m-1)!! (1-x^2)^{m/2}.$ (13)	Fig. 10. Single so is also attenuate
5 B 5 C 1 - 3 - 7	Eq. (12) and explicit formulae for low-order polynomials (e.g., Eqs. (12)–(27) in Wolfram <sup>19</sup> or in [83]) allow one to start iterations and check the result. Source code for $P_k^m(x)$ is published in C [81] and Fortran [80]. Built-in functions scipy.special.lpm <sup>20</sup> and legendre <sup>21</sup> are available in Python and Matlab, respectively.	
<u>í mart</u> e	In this paper, however, we use a slightly different form of the associated polynomials (Schmidt semi-normalized polynomials, <sup>22</sup> see also [84]) $\sqrt{(t_{e} - m)!}$	
	$Q_k^m(x) = (-1)^m \sqrt{\frac{(k-m)!}{(k+m)!}} P_k^m(x) $ (14) for two reasons. First, the $(-1)^m$ factor removes the same factor from $P_k^m(x)$ (e.g. see Eq. (13)). Second, the use of the square root factor	
	simplifies the orthogonal property $\int_{-\infty}^{1} O_{m}^{m}(x) O_{m}^{m}(x) = -\frac{2}{2} \delta_{x}$ (15)	
RT code gsit:	$\int_{-1} Q_k^m(x) Q_l^m(x) = \frac{2}{2k+1} \delta_{kl},$ (15) where $\delta_{kl}$ is the Kronecker delta (compare e.g., with Eq. (5) in Wolfram <sup>16</sup> ). Therefore, one must be careful when comparing associated	Fig. 11a. Python
source code	polynomials from different sources. Note that the Schmidt and associate polynomials are direct substitution of each other in terms of the final result, but their orthogonal properties differ by a scaling factor. In Table 2 we provide analytical expressions for a few low-order associated polynomials as defined in Eq. (14); Fig. 9 shows source code.	- see Section 3. all $\Delta \tau$ -layers
	<ul> <li>https://mathworld.wolfram.com/AssociatedLegendrePolynomial.html.</li> <li>https://docs.scipy.org/doc/scipy/reference/generated/scipy.special.lpmn.html.</li> </ul>	which we wi For valida to implemen equation "au
ython.	<ul> <li>https://www.mathworks.com/help/matlab/refjlegendre.html.</li> <li>https://en.wikipedia.org/wiki/Spherical_harmonics.</li> </ul>	Benchmark r scalar approv and downwa

- Isotropic (Lambertian) surface.
- Single scattering correction.
   No polarization

  - No BRDF (but we explain equations)
  - No vertical profile (but we give algorithm)
     No absorption spectroscopy

of the scattering angle  $(\Theta)$ 

# The Paper-and-Code Bundle Concept in Atmospheric Radiation Science



## What do we propose? To bundle paper & code!

### Scattering of Sunlight

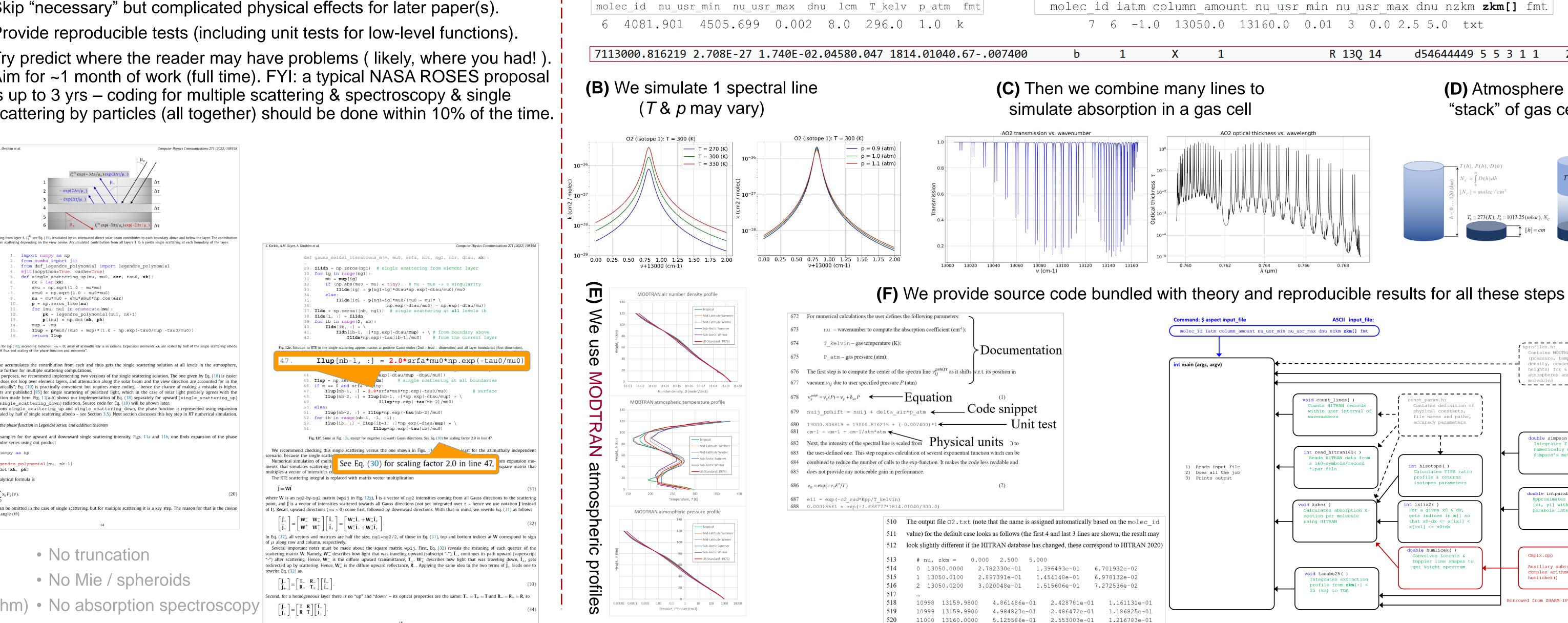
### al "strategy":

cate equations (only necessary) with code snippets (short).

nge these in an order natural for code development (e.g., starting from evel function without dependencies).

the right balance: practically valuable but not overcomplicated. "necessary" but complicated physical effects for later paper(s).

ide reproducible tests (including unit tests for low-level functions).



### **2.** Line-by-Line Atmospheric Absorption Spectroscopy (in preparation)

• We have used LBL solver from Interpolation and Profile Correction (IPC) Method by A. Lyapustin, J. Atm Sci, 2003 -- QR-code:

• HPOSS22: "The paper-and-code bundle as a new paradigm supporting the TOPS initiative in Earth Science" (status = "selectable") -- thank you for considering our proposal

(A) We explain input & output in two modes: gas cell & atmospheric absorption (both use HITRAN)

