

On the Order of Atmospheric Scattering, Its Polarization and Computation Efficiency



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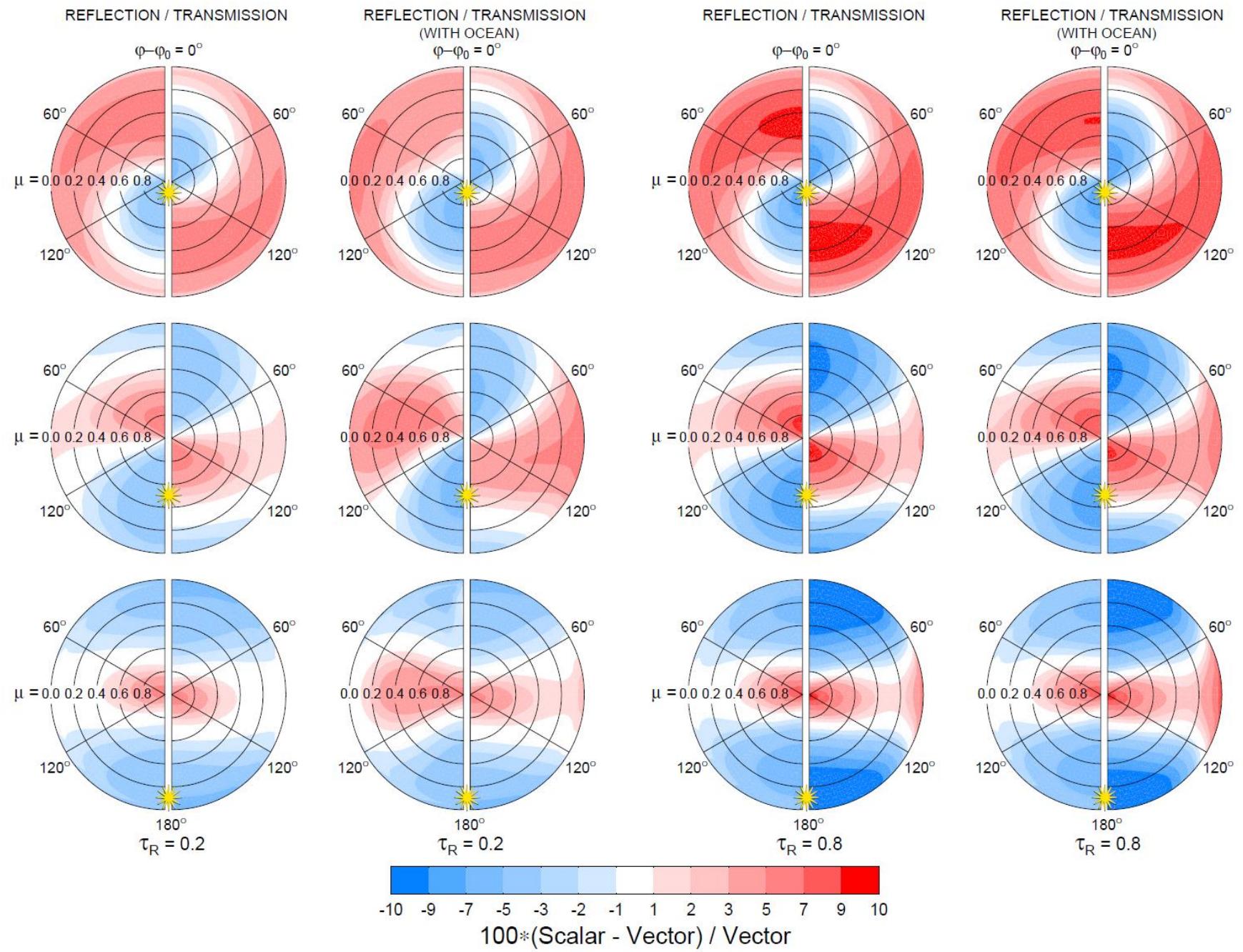
主要 內容

CONTENTS

- ① Background
- ② Polarized Radiative Transfer
- ③ N-Appr method
- ④ N-Plus method
- ⑤ Summary

Background

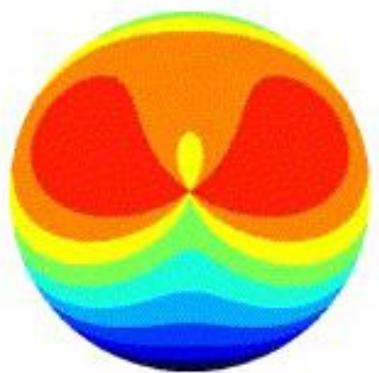
1. Properties of Atmosphere scattering:
2. More polarized instrument
(PARASOL, 3MI, SGLI, APS, SPEX, MSPI...)
3. Errors due to neglecting polarization
4. Hyperspectral Measurements for Gases such OCO2, TanSAT are much polarized sensitive



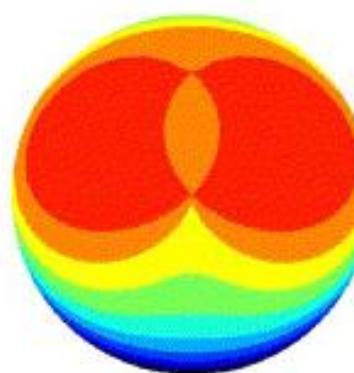
M.I.Mishchenko et al, 1994

Errors due to neglecting polarization in O₂-A Band

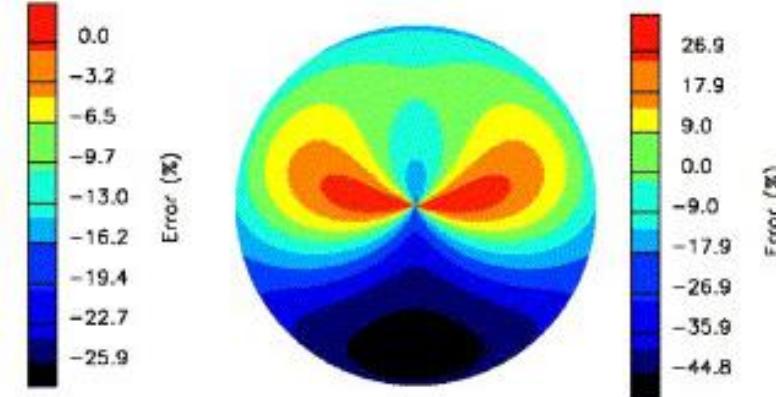
$\theta_0=40^\circ$, Albedo=0.3, No Aerosol



Weak absorption



Moderate absorption



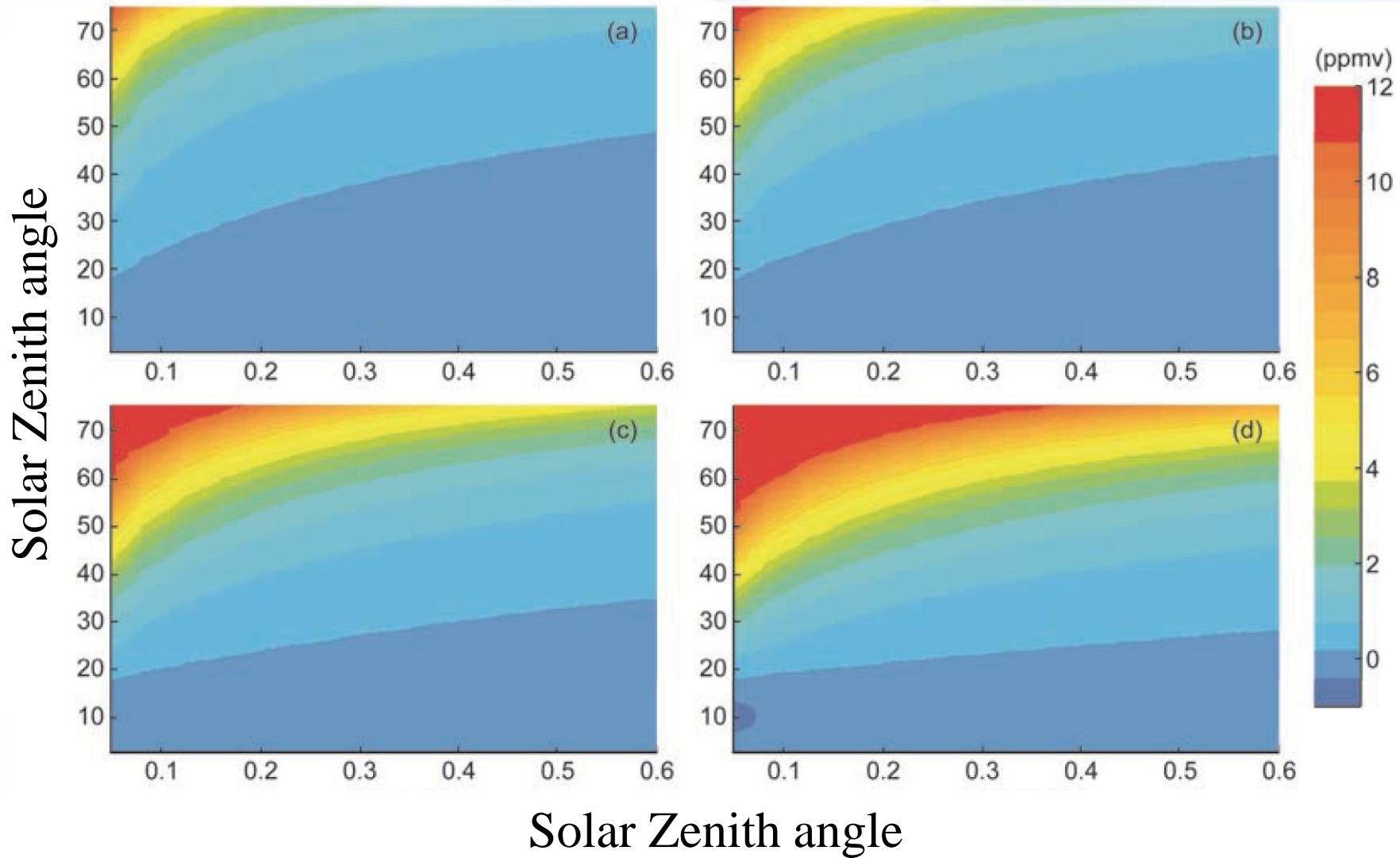
Strong Absorption

Table 2

Retrieval and smoothing errors and errors from neglecting polarization for January and July scenes in Park Falls, WI, USA

Scenario	Retrieval error (ppm)	Polarization error (ppm)	Smoothing error (ppm)
January	1.8	7.4	1.0
July	0.4	0.4	0.1

XCO₂ retrieval errors due to neglecting polarization



Radiative Transfer Equation

$$\mu \frac{d\mathbf{I}(\tau, \Omega)}{d\tau} = \mathbf{I}(\tau, \Omega) - \mathbf{J}_1(\tau, \Omega) - \mathbf{J}_m(\tau, \Omega)$$

$$\mathbf{J}_m(\tau, \Omega) = \frac{\omega}{4\pi} \int_0^{4\pi} \mathbf{I}(\tau, \Omega') \mathbf{M}(\tau, \Omega; \Omega') d\Omega'$$

$$\mathbf{J}_1(\tau, \Omega) = \frac{\omega}{4\pi} \pi F_0 \exp(-\tau / \mu_0) \mathbf{P}(\tau, \Omega; -\Omega_0)$$

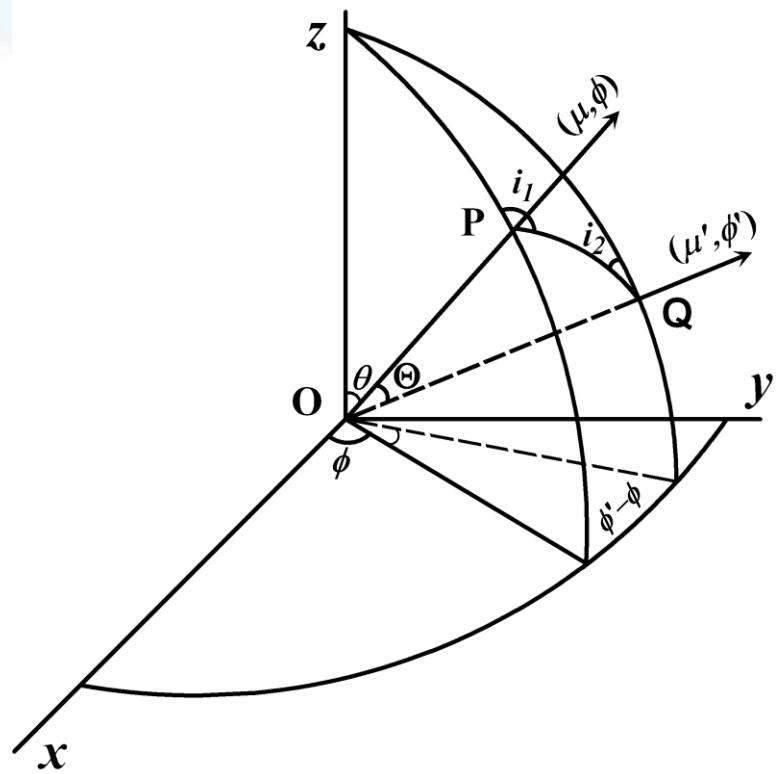
$$\mathbf{I} = [I, Q, U, V]^T$$

Coordinate system

$$\mathbf{I} = \begin{pmatrix} I \\ Q \\ U \\ V \end{pmatrix} \quad \bar{\mathbf{P}} = \begin{pmatrix} a_1 & b_1 & 0 & 0 \\ b_1 & a_2 & 0 & 0 \\ 0 & 0 & a_3 & b_2 \\ 0 & 0 & -b_2 & a_4 \end{pmatrix}$$

a_i, b_i depend on scattering angle Θ

$$\vec{\mathbf{M}} = \vec{L}(\pi - i_2) \bar{\mathbf{P}}(\Theta) \vec{L}(-i_1)$$



Numerical Algorithms

1. MC: (Kattawar & Plass, 1968; Roberti & Kummerow, 1999;
Wu & Lu, 989)
2. Adding-doubling method (De Haan et al., 1987; Evans
& Stephens, 1991; Hansen, 1971)
3. Inverse of matrix method (Schulz et al., 1999; Siewert,
2000)
4. Successive order of Scattering (Duan, 2004; 6s; Pstar)
5. SCIATRAN (2009?)

N-Appr method

It is supposed that just the first a few orders are needed

How & What ?

Two order scattering approximation

- 👉 Vijay Natraj & Robert Spur, *JQSRT* 107,2007
- 👉 Sergey Korkin et. al., *JQSRT* 113,2012

N-Approaximation method

$$\mathbf{I} = \mathbf{I}_1 + \mathbf{I}_2 + \mathbf{I}_3 + \dots + \mathbf{I}_{\infty}$$

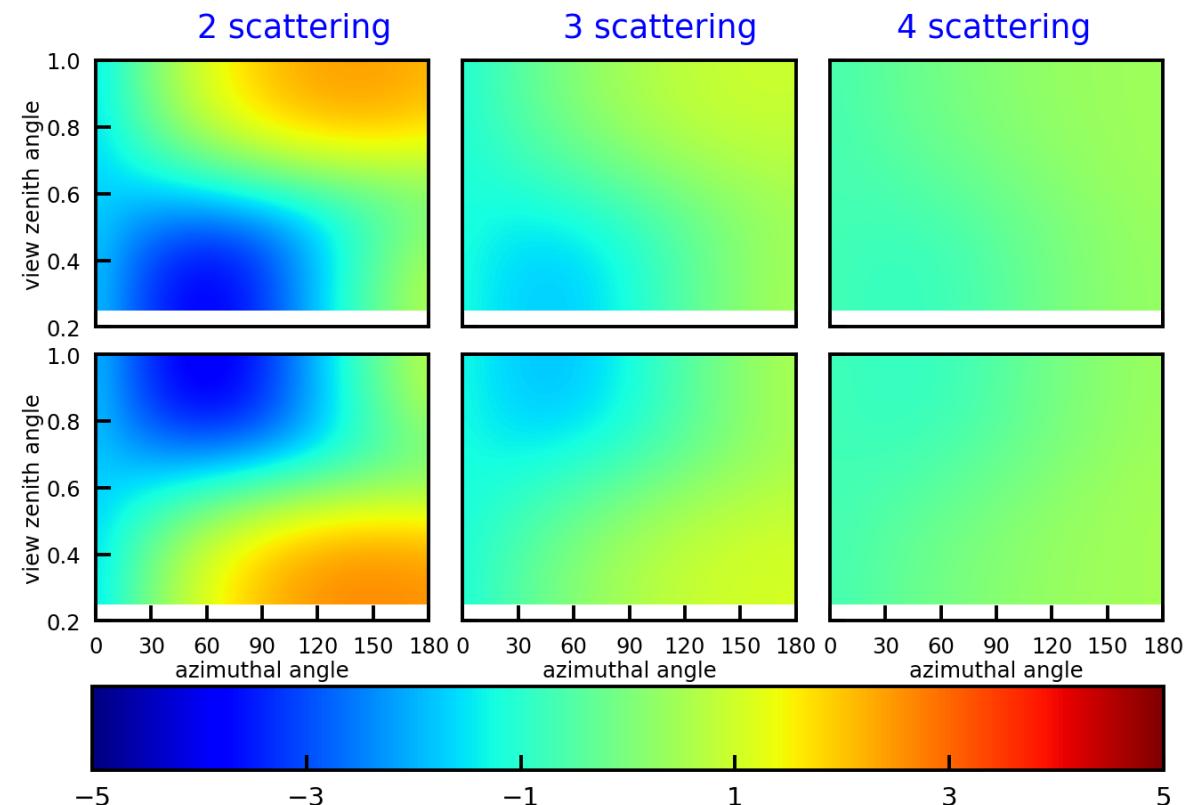
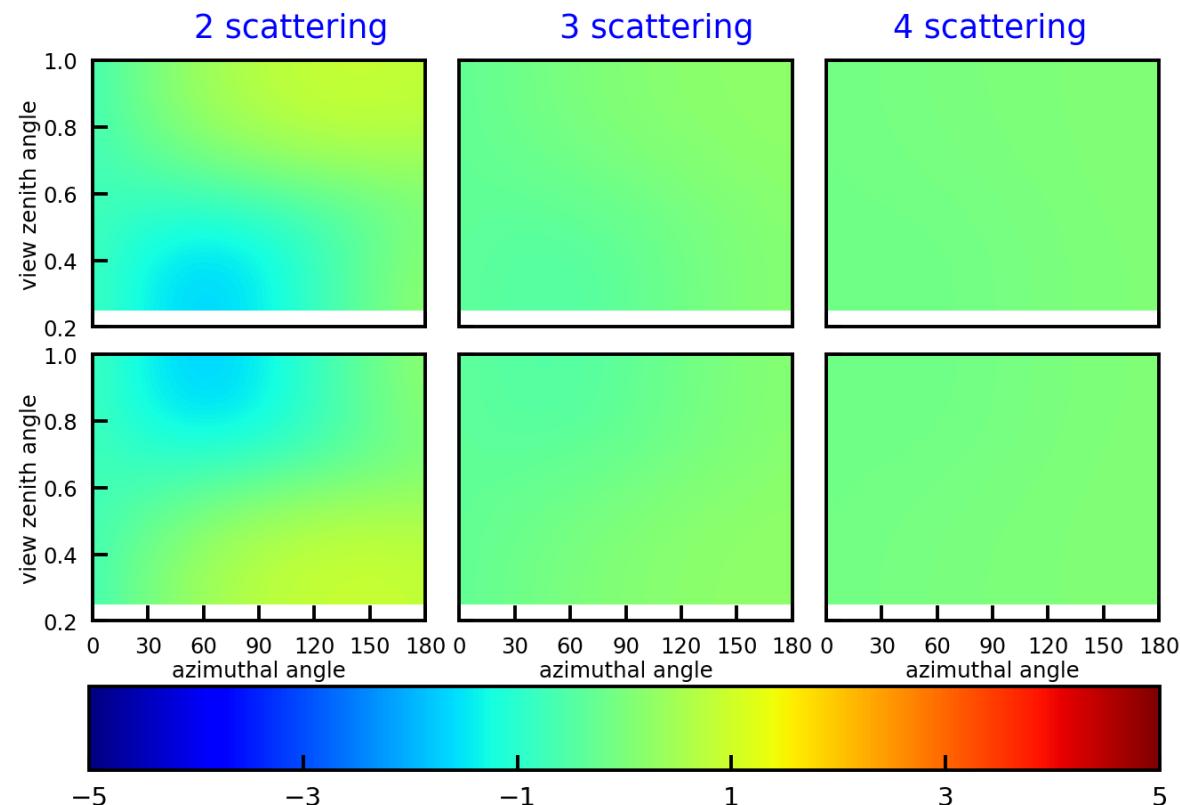
$$\mathbf{I}^* = \sum_{i=1}^n \mathbf{I}_i + \sum_{i=n+1}^{\infty} [I_i, 0, 0, 0]^T$$

SOSVRT: A polarized radiative transfer model
based on Successive order of Scattering

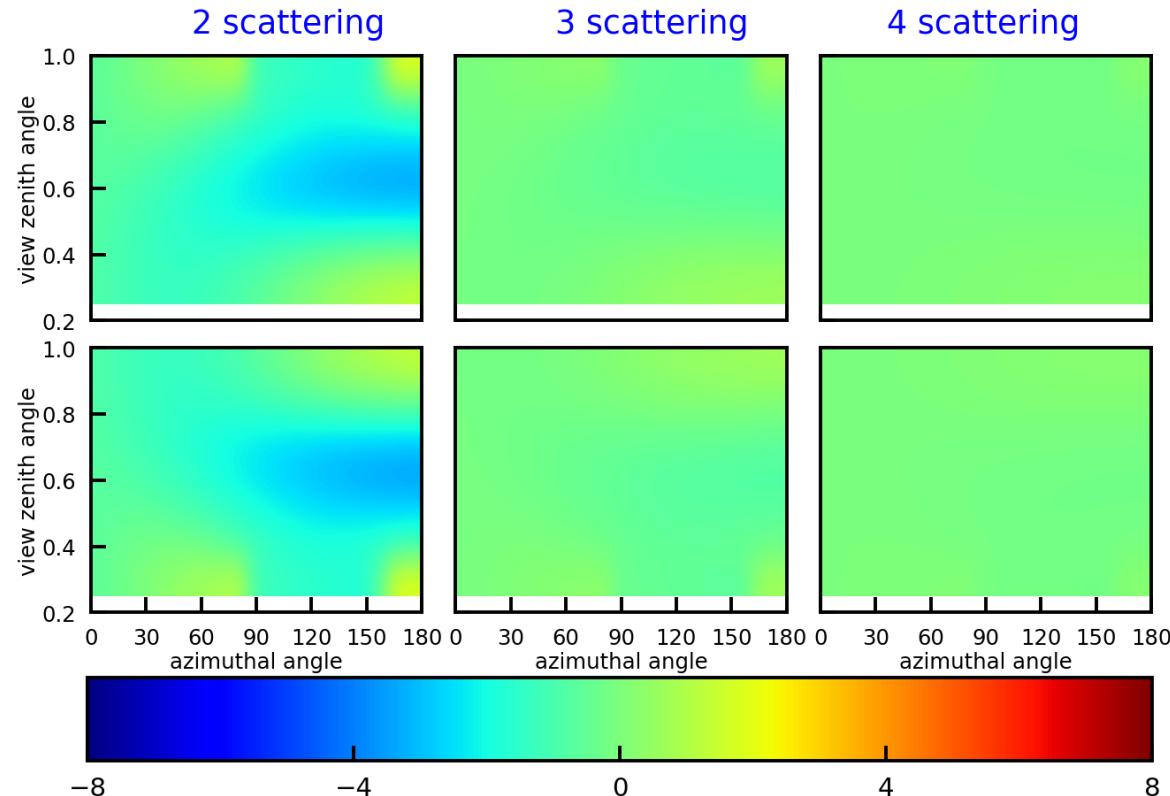
CASE A: pure molecular atmosphere with different optical depth

CASE B: molecular with aerosol, where the aerosol is supposed to
be exponentialy decreased with height, the scale height
is set to be 1.8km for aerosol, and 7.8km for molecular

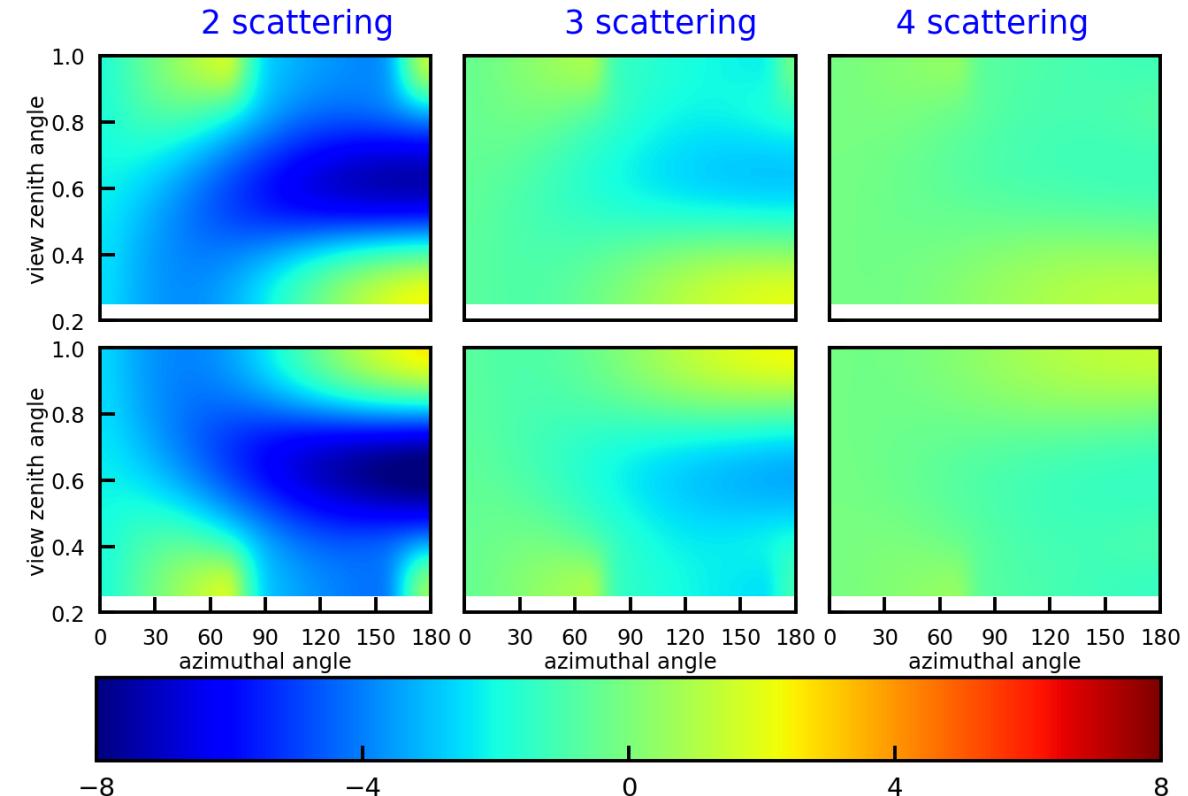
N-APPR



N-APPR

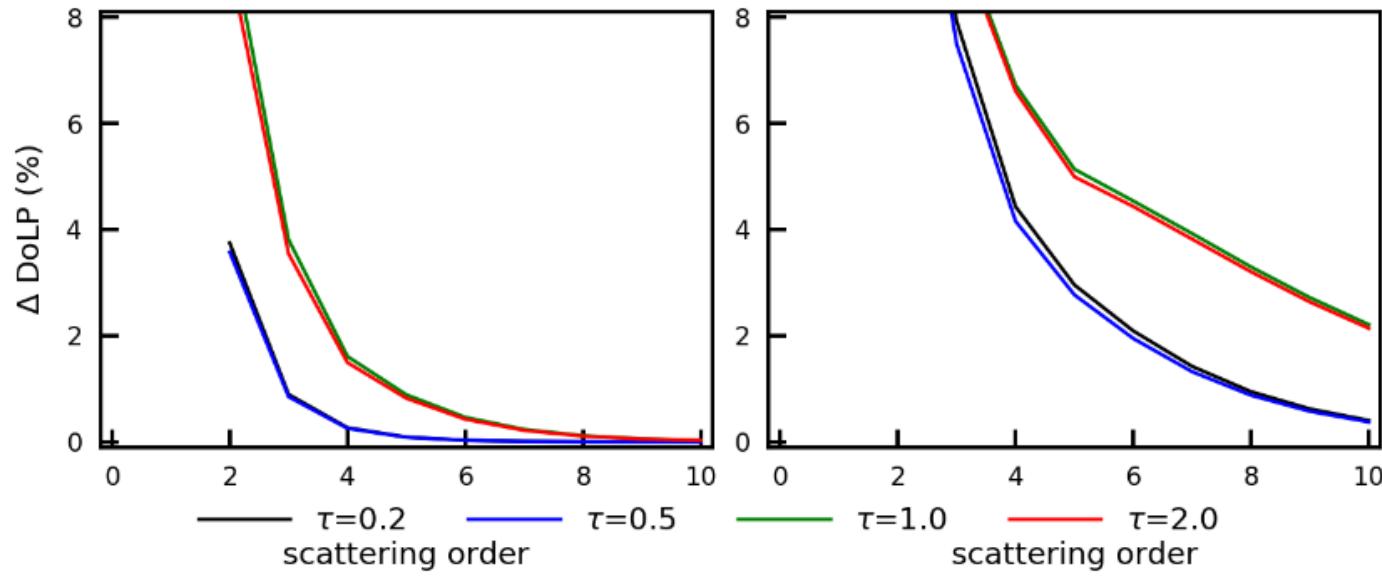
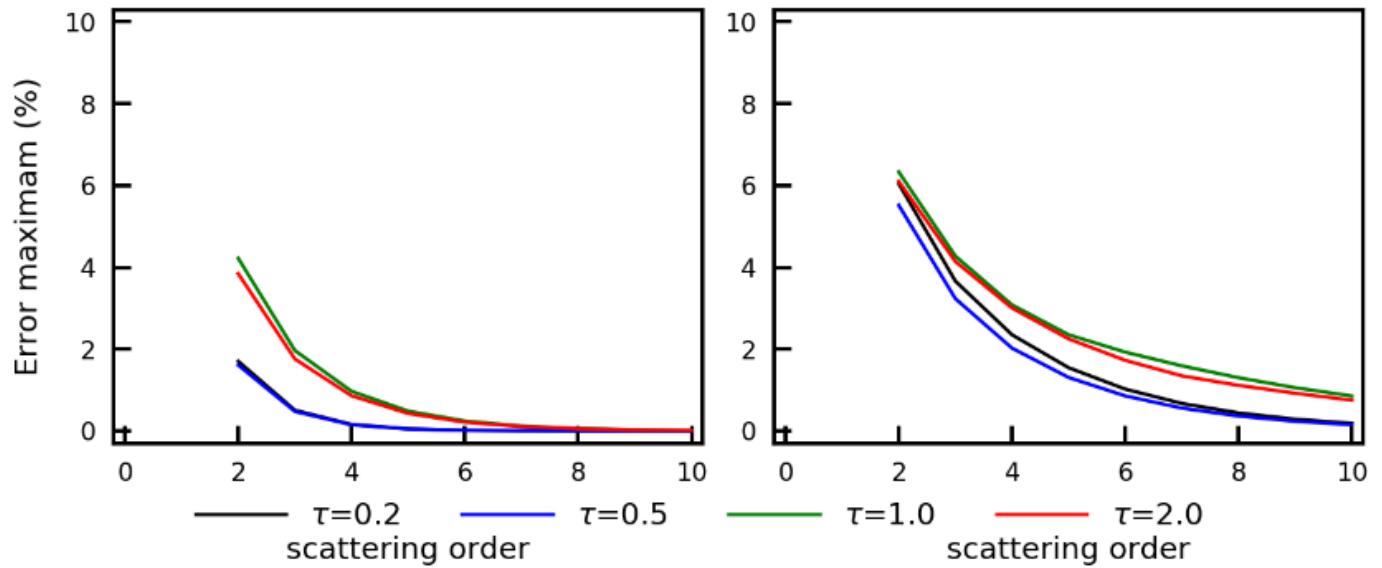


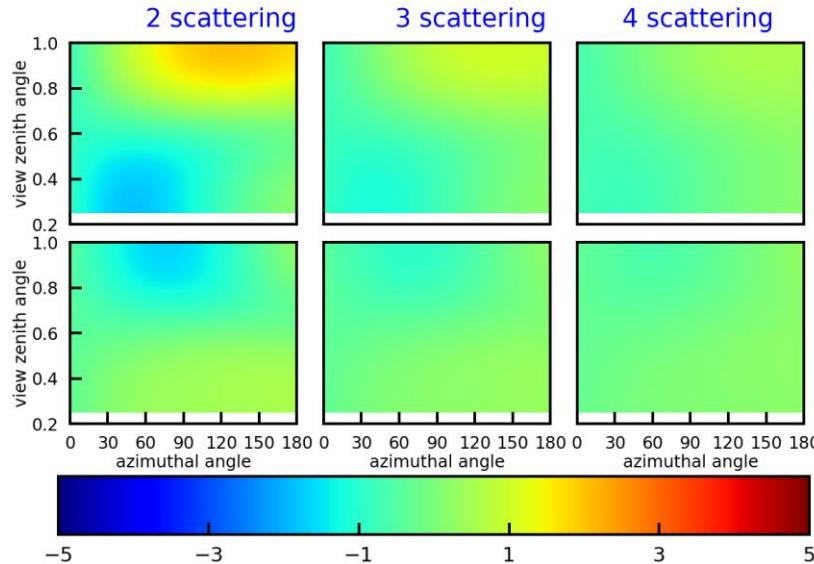
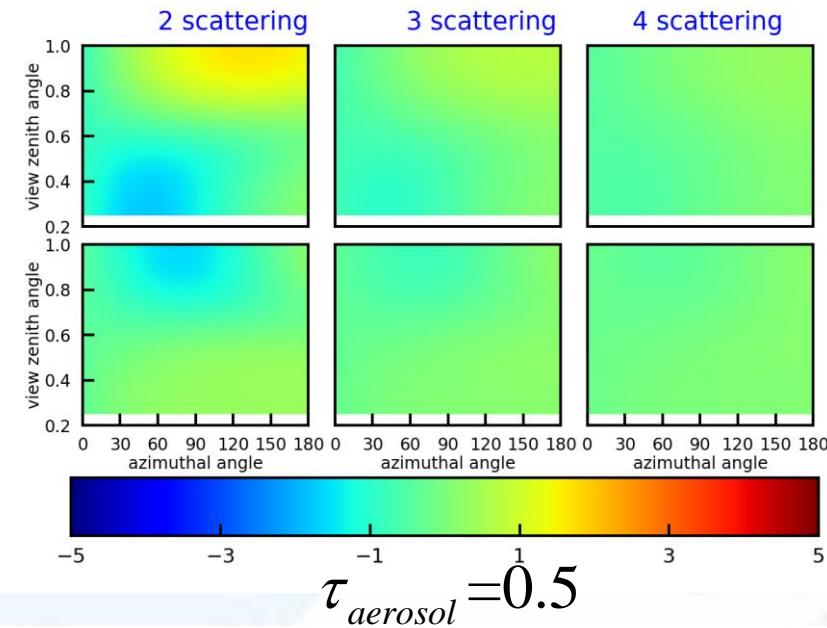
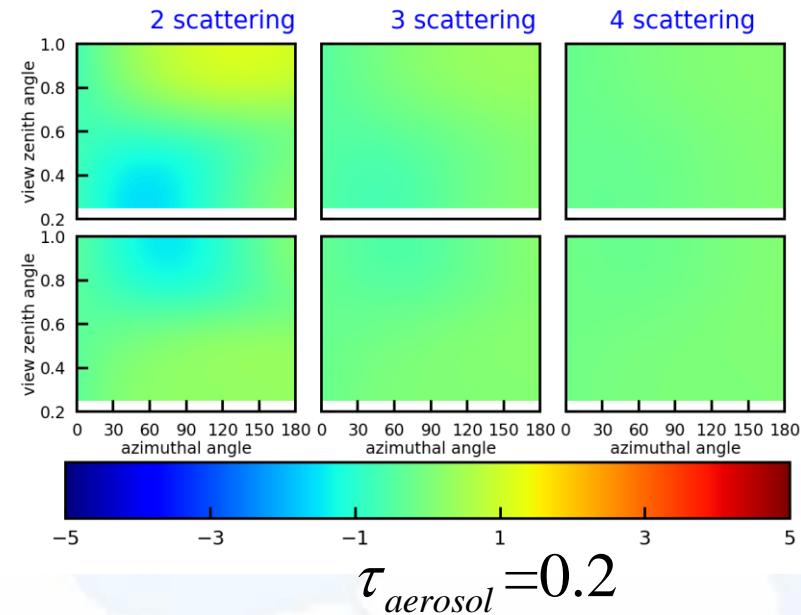
$\Delta DoLP$ $\tau=0.2$



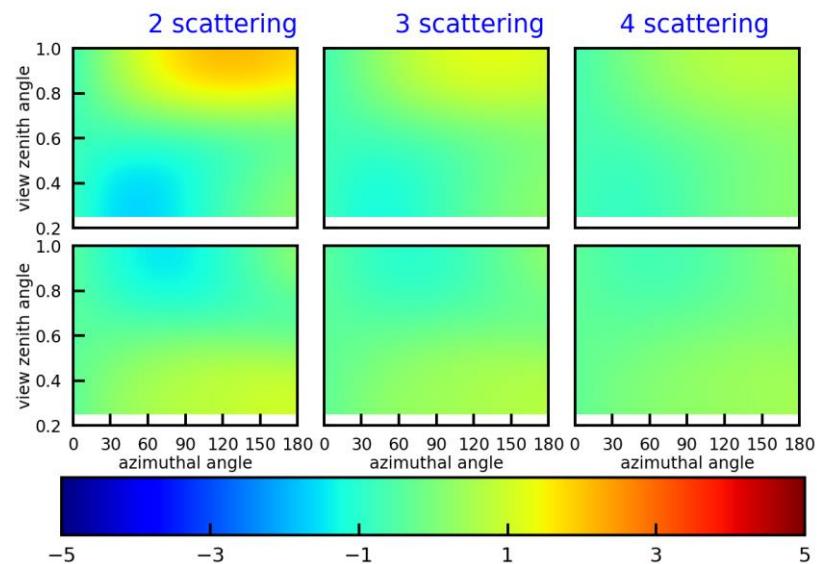
$\Delta DoLP$ $\tau=0.5$

N-APPR No Aerosol





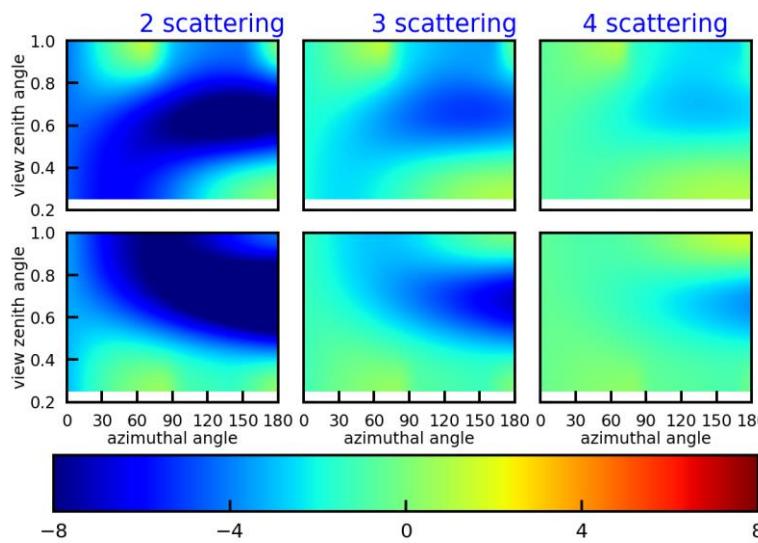
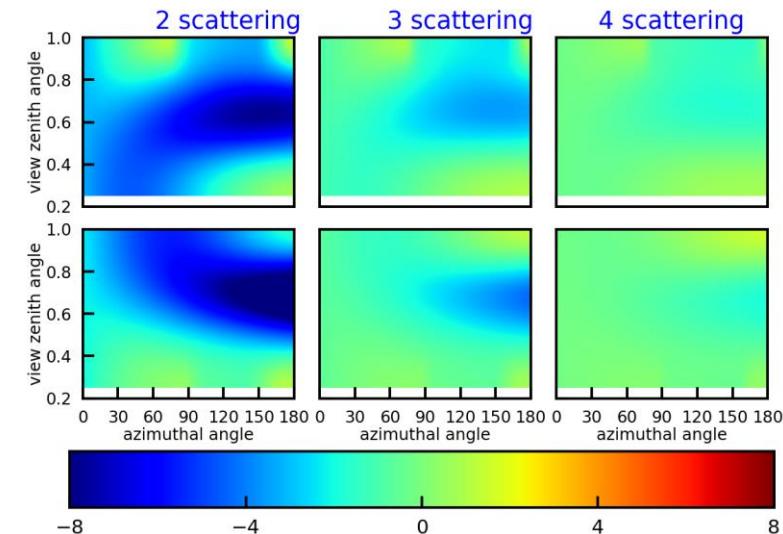
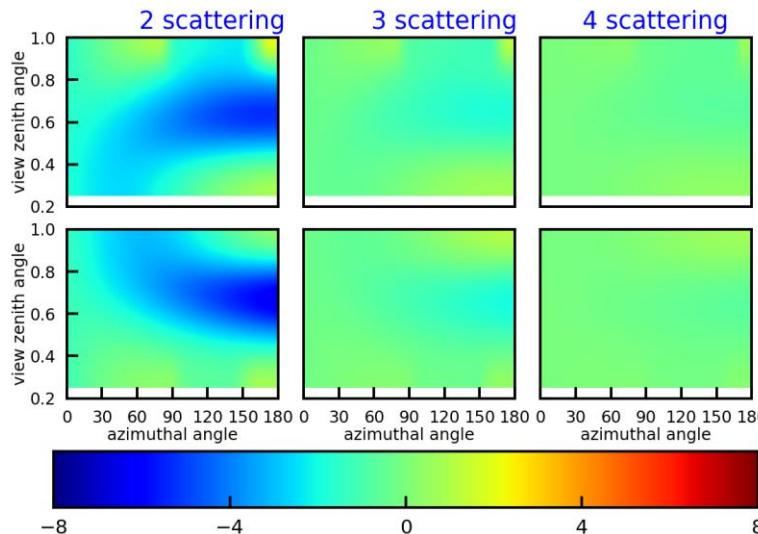
$\tau_{aerosol} = 1.0$



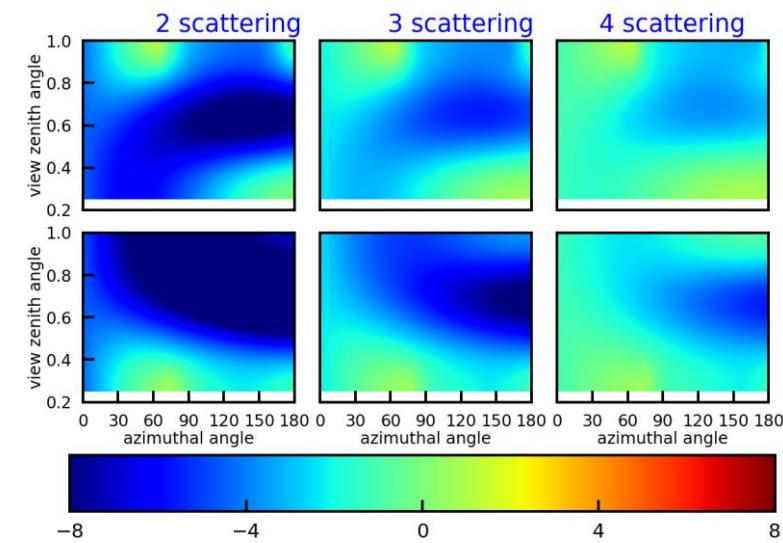
$\tau_{aerosol} = 2.0$

$$(I - I_{true}) / I_{true} \times 100\%$$

$$\tau_{mol} = 0.156$$



$\tau_{aerosol} = 1.0$

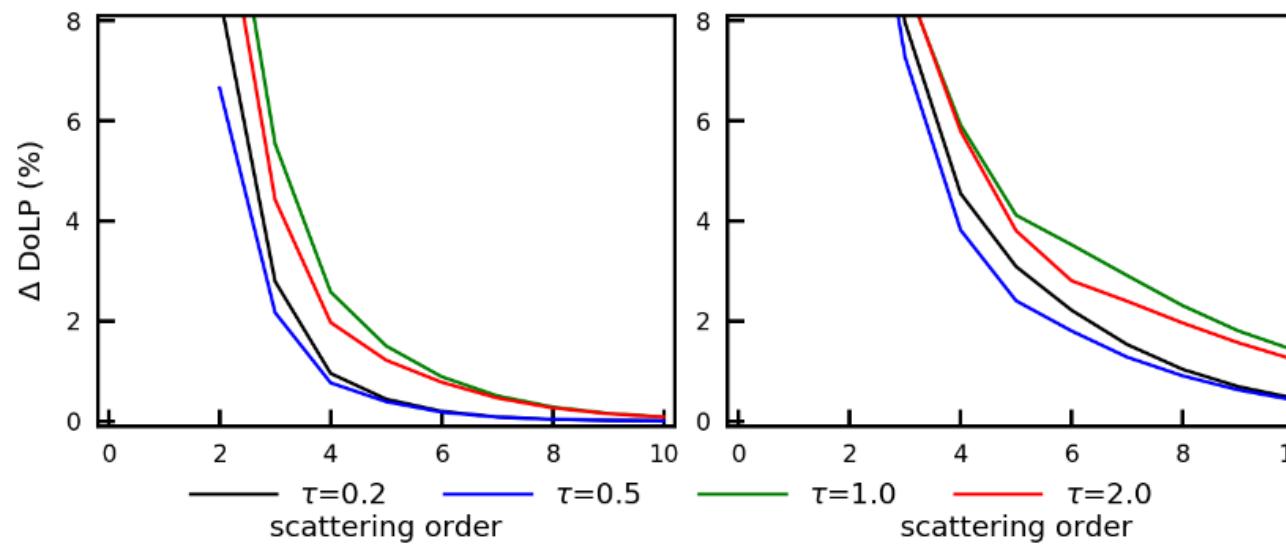
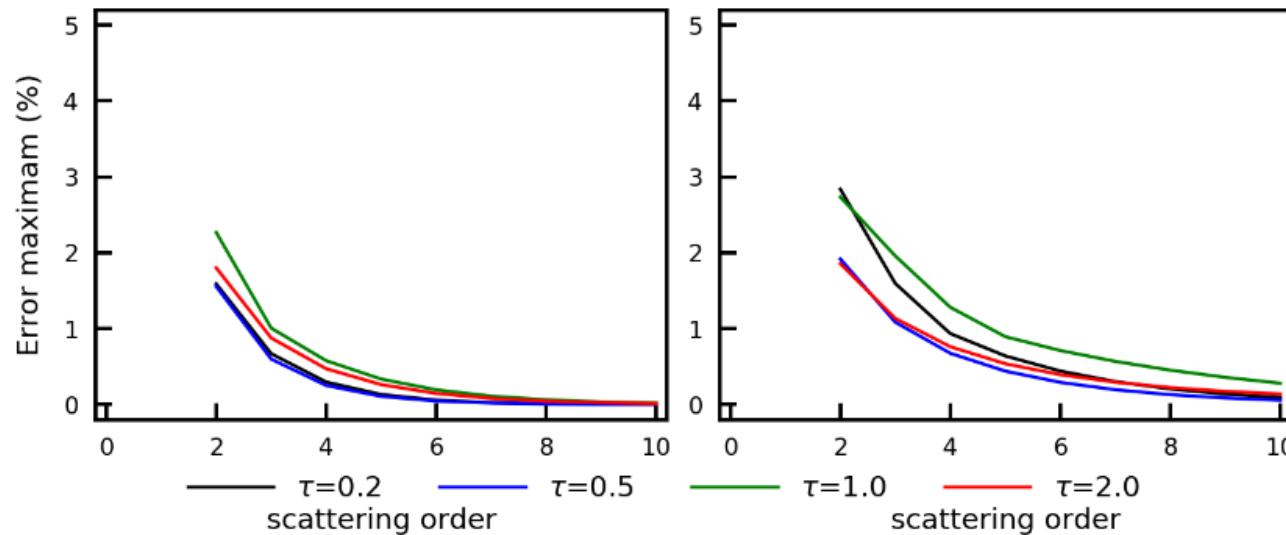


$\tau_{aerosol} = 2.0$

$\Delta DoLP$

$\tau_{mol} = 0.156$

N-APPR with Aerosol



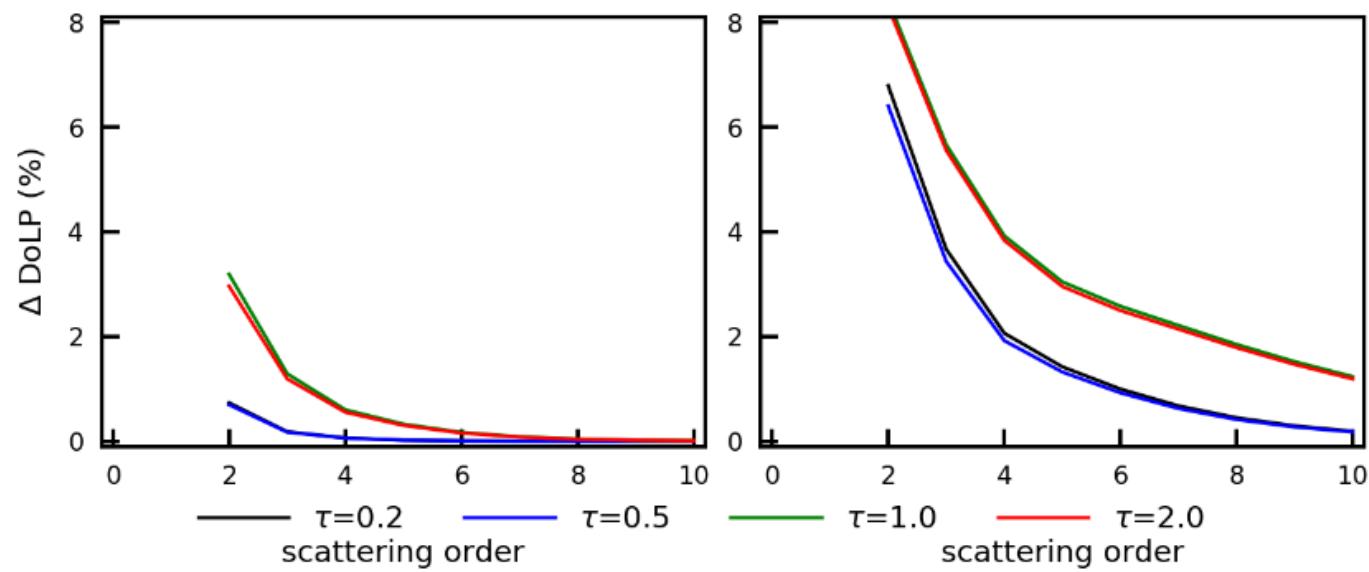
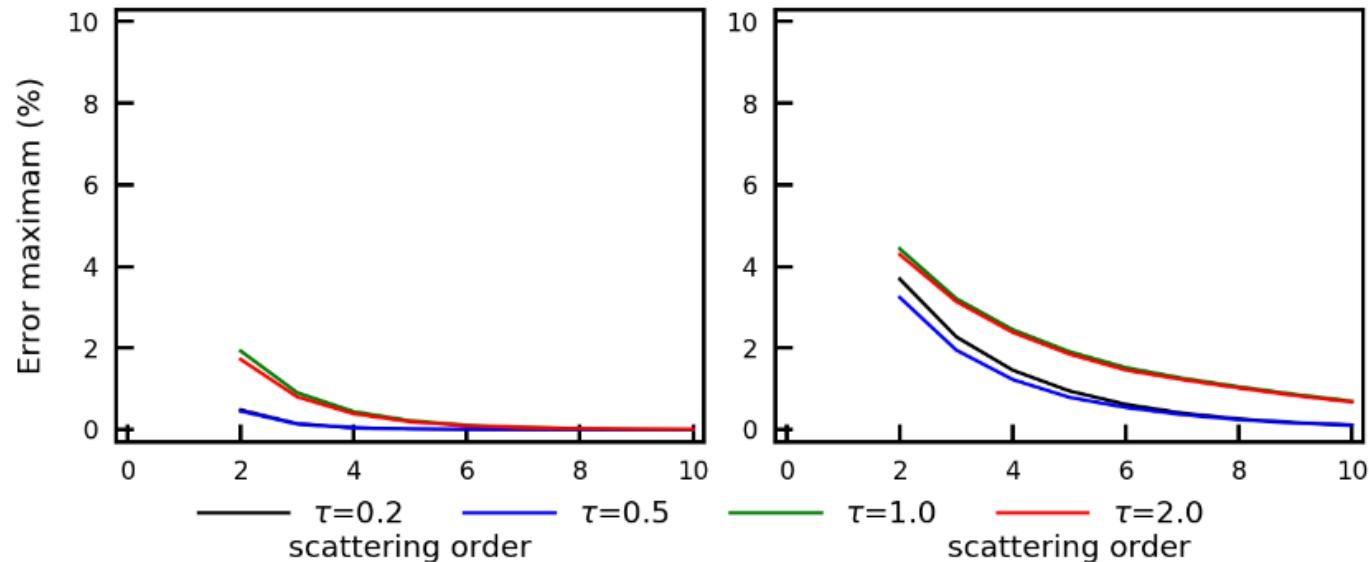
N-PLUS method

$$\mathbf{I} = \mathbf{I}_1 + \mathbf{I}_2 + \mathbf{I}_3 + \dots + \mathbf{I}_{\infty}$$

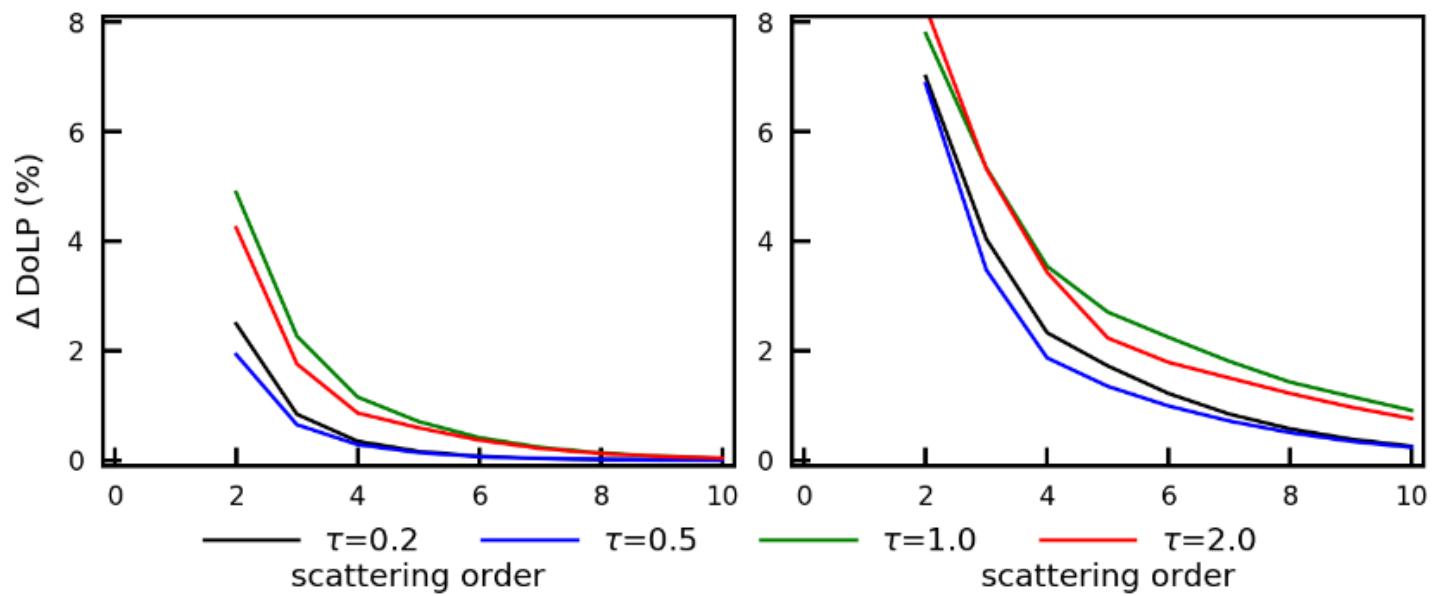
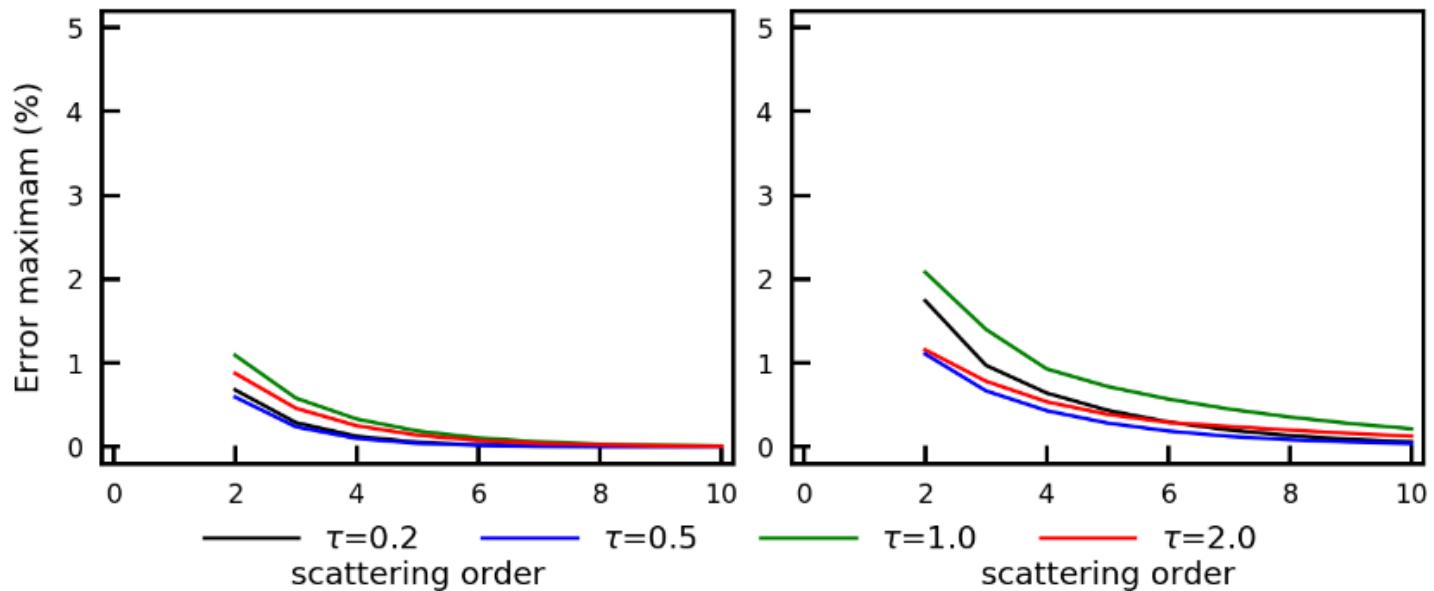
$$\mathbf{I}^* = \sum_{i=1}^n \mathbf{I}_i + \sum_{i=n+1}^{\infty} [I_i, 0, 0, 0]^T$$

$$\begin{aligned} \mu \frac{d\mathbf{I}}{d\tau} &= -\mathbf{I} + \frac{\omega}{4\pi} \mathbf{M}(\mu, \phi; \mu_0, \phi_0) \mathbf{F}_0 e^{-\tau/\mu_0} \\ &\quad + \frac{\omega}{4\pi} \int_0^{2\pi} \int_{-1}^1 \mathbf{M}(\mu, \varphi; \mu', \phi') \mathbf{I}^*(\mu', \phi') d\mu' d\phi' \end{aligned}$$

N-PLUS No Aerosol



N-PLUS with Aerosol



Summary

- **N-PLUS method, a correction of the N-appr method, is a little bit more accurate, and efficient**
- **the number of scattering must be carefully considered, especially for polarization sensitive instruments such as OCO2, TanSAT, Where two scattering is not accurate enough**

谢谢！ THANK YOU
FOR YOUR TIME.



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