

I. MOTIVATING REMARKS

- Global mean sea level rise reflects ocean mass & steric (i.e., density) change (e.g., ref. 1).
- Due to the nonlinearity of the density equation of state, processes effecting global mean steric sea level (η_ρ) change remain opaque.
- Using a data-constrained state estimate (ref. 2), we diagnose closed budgets of η_ρ (e.g., ref. 3) to address the following questions—

- 1 Are η_ρ changes mainly controlled by atmospheric forcing (i.e., sea-surface exchanges of heat & freshwater)?
- 2 Do oceanic transports (e.g., small-scale diffusion & large-scale advection) also contribute?
- 3 How well can the η_ρ budget be constrained by ocean circulation models?

II. GLOBAL CHANGES

- Global ocean heat content [Fig. 1a] & freshwater content [Fig. 1b] from the state estimate over 1993-2003 show annual, interannual, & decadal changes, with the ocean gradually warming & freshening, in qualitative agreement with IPCC AR4 (ref. 4).
- Consistent with warming & freshening [Figs. 1a-b], η_ρ over 1993-2003 exhibits long-term rise [Fig. 1c].

III. STERIC BUDGET

- What processes are contributing to the long-term rise in η_ρ over 1993-2003?
- We formulate a budget for η_ρ in terms of advection, diffusion, & local forcing (ref. 3).
- Long-term rise in η_ρ represents a slight imbalance between a positive trend due to atmospheric forcing & negative trends owing to oceanic advection & diffusion [Fig. 2].

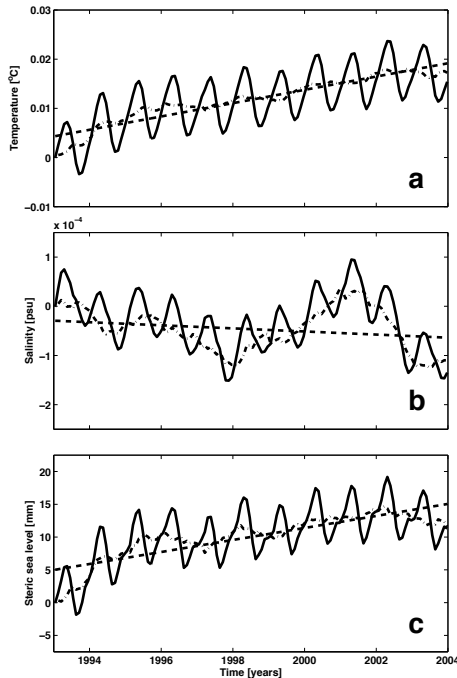


Fig. 1: Global mean ocean (a) temperature, (b) salinity, & (c) steric sea level anomalies from the estimate over 1993-2003 (solid); non-seasonal series (dash-dot) & linear trends (dashed) are also shown.

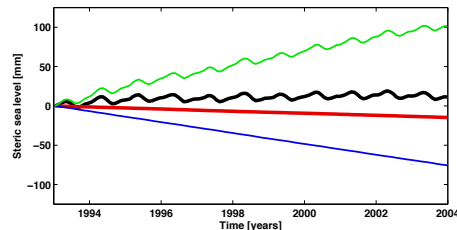


Fig. 2: Budget for η_ρ (black) in terms of advection (red), diffusion (blue), & forcing (green) from the ocean state estimate over 1993-2003.

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IV. ADVECTION CONTRIBUTES?

- How is it that advective redistribution contributes to the η_ρ budget [Fig. 2]?
- Contributions from advection (as well as diffusion) reflect nonlinearities in the equation of state of seawater.
- For advection to contribute, flow must occur across pressure surfaces (i.e., isobars) & across temperature or salinity surfaces (i.e., isotherms or isohalines) [see Fig. 3].

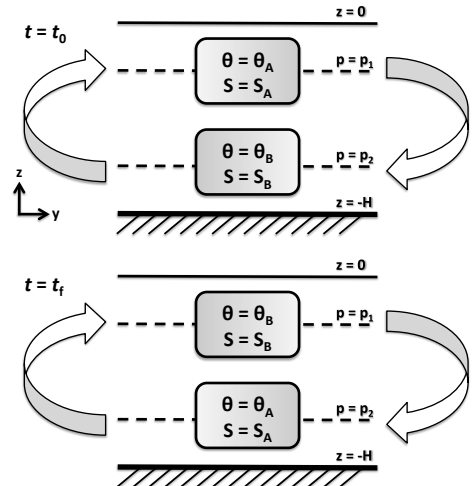


Fig. 3: A thought experiment. Consider two water parcels (boxes) of equal mass. Parcel A (B) has temperature θ_A (θ_B) and salinity S_A (S_B). At $t=t_0$ (top), parcel A (B) feels pressure p_1 (p_2). Now imagine that a circulation (arrows) rearranges the parcels such that, at $t=t_f$ (bottom), parcel A (B) feels pressure p_2 (p_1). Does this scenario imply a change in steric sea level?

Given a nonlinear equation of state $\rho(S, \theta, p)$, it can be shown that the combined volume of the two parcels can change (hence steric sea level can change) between t_0 & t_f under this scenario provided two conditions are met:

- 1 Flow is across isobars ($p_1 \neq p_2$), &
- 2 Flow crosses isotherms or isohalines ($\theta_1 \neq \theta_2$ or $S_1 \neq S_2$).

V. SENSITIVITY EXPERIMENTS

- Are estimates of η_ρ changes [Figs. 1-2] sensitive to ocean model formulation?
- To gauge the sensitivity of η_ρ changes to representational choices, a set of numerical experiments was performed such that the tracer advection scheme was varied.
- Changes in η_ρ are very sensitive, with positive or negative decadal change resulting depending on advection scheme [Fig. 4].

VI. MAIN CONCLUSIONS

✓ Both advective and diffusive oceanic transports make important contributions to global mean steric sea level change [Fig. 2].

✓ Contributions from oceanic transports reflect nonlinearities in density equation of state [Fig. 3].

✓ Estimates of global mean steric sea level changes from ocean general circulation models can be sensitive to tracer advection scheme [Fig. 4].

REFERENCES

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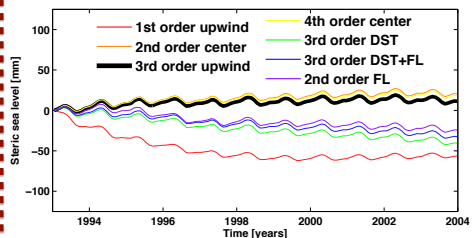


Fig. 4: Changes in η_ρ produced under advection scheme experiments. Experiments are performed using the following differencing schemes for tracer advection: first order upwind-biased (red); second order centered (orange); third order upwind-biased (black; from Fig. 2); fourth order centered (yellow); third order direct space time without a flux limiter (green) & with a flux limiter (blue); & second order with a flux limiter (purple).