

# Potential vorticity homogenization in an idealized model of the Southern Ocean

Daniel C. Jones<sup>1,2</sup>, Takamitsu Ito<sup>1</sup>, and Thomas Birner<sup>2</sup>

<sup>1</sup>School of Earth and Atmospheric Sciences, Georgia Institute of Technology, Atlanta, Georgia, USA

<sup>2</sup>Department of Atmospheric Science, Colorado State University, Fort Collins, Colorado, USA

## Motivation/questions

What determines the equilibrium slope of buoyancy surfaces in the interior of the Southern Ocean?

How sensitive is the interior buoyancy structure to surface wind stress?

## Theory

Buoyancy decomposition:

$$b = \tilde{b}(z) + b'(x, y, z, t) \quad N^2(z) = \partial_z \tilde{b} \quad M^2(x, y, z, t) = \partial_y b' = \partial_y b$$

Quasi-geostrophic potential vorticity gradient:

$$\partial_y q = \beta + \partial_z (f_0 N^{-2} \partial_y b') \quad (1)$$

Slope of buoyancy surfaces:

$$N^{-2} \partial_y b' = M^2/N^2 = \partial_y b / \partial_z \tilde{b} = -s_b$$

So equation (1) can be written (zonal and depth mean):

$$\overline{\partial_y q} = \beta - f_0 \overline{\partial_z s_b} = \beta \left( 1 - \frac{\overline{\partial_z s_b}}{\beta/f_0} \right) = \beta(1 - r)$$

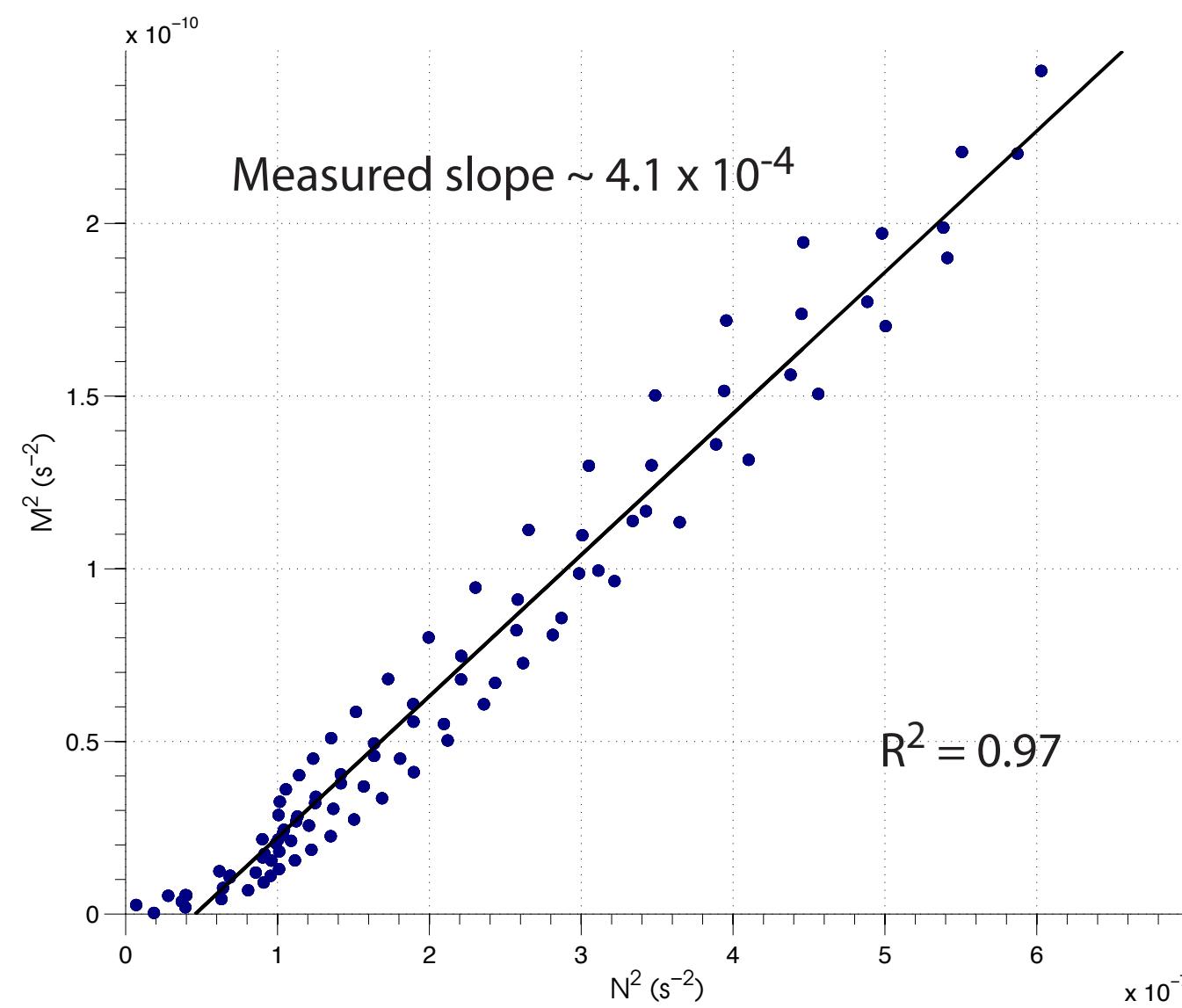
PV homogenization metric:  $r(y, t) \equiv \frac{\overline{\partial_z s_b}}{\beta/f_0}$

Under homogenous PV ( $r=1$ ):

$$\left( \overline{\frac{\partial s_b}{\partial z}} \right) = \frac{\beta}{f_0} = \frac{2\Omega a^{-1} \cos(\phi_0)}{2\Omega \sin(\phi_0)} = a^{-1} \cot(\phi_0)$$

The large-scale slope structure is constrained by planetary-geometric parameters

## Results: steady state



Prediction:

$$\frac{\Delta s_b}{\Delta z} = -\frac{1}{H} \frac{M^2}{N^2} = \frac{\beta}{f_0}$$

$$M^2 = \beta H |f_0|^{-1} N^2$$

$$\text{Slope} = \beta H |f_0|^{-1}$$

$$\text{Slope} \approx 4.7 \times 10^{-4}$$

Fig. 1. Horizontal stratification versus vertical stratification in an idealized Southern Ocean model. Each point is calculated from a particular longitude/depth across the channel.

The large-scale slope structure is constrained by planetary geometric parameters

The planetary-geometric constraint is most effective when PV is uniform ( $r=1$ )

Stronger wind stress increases eddy activity, which homogenizes large-scale PV and makes the planetary-geometric constraint *more* dynamically relevant

## Model setup

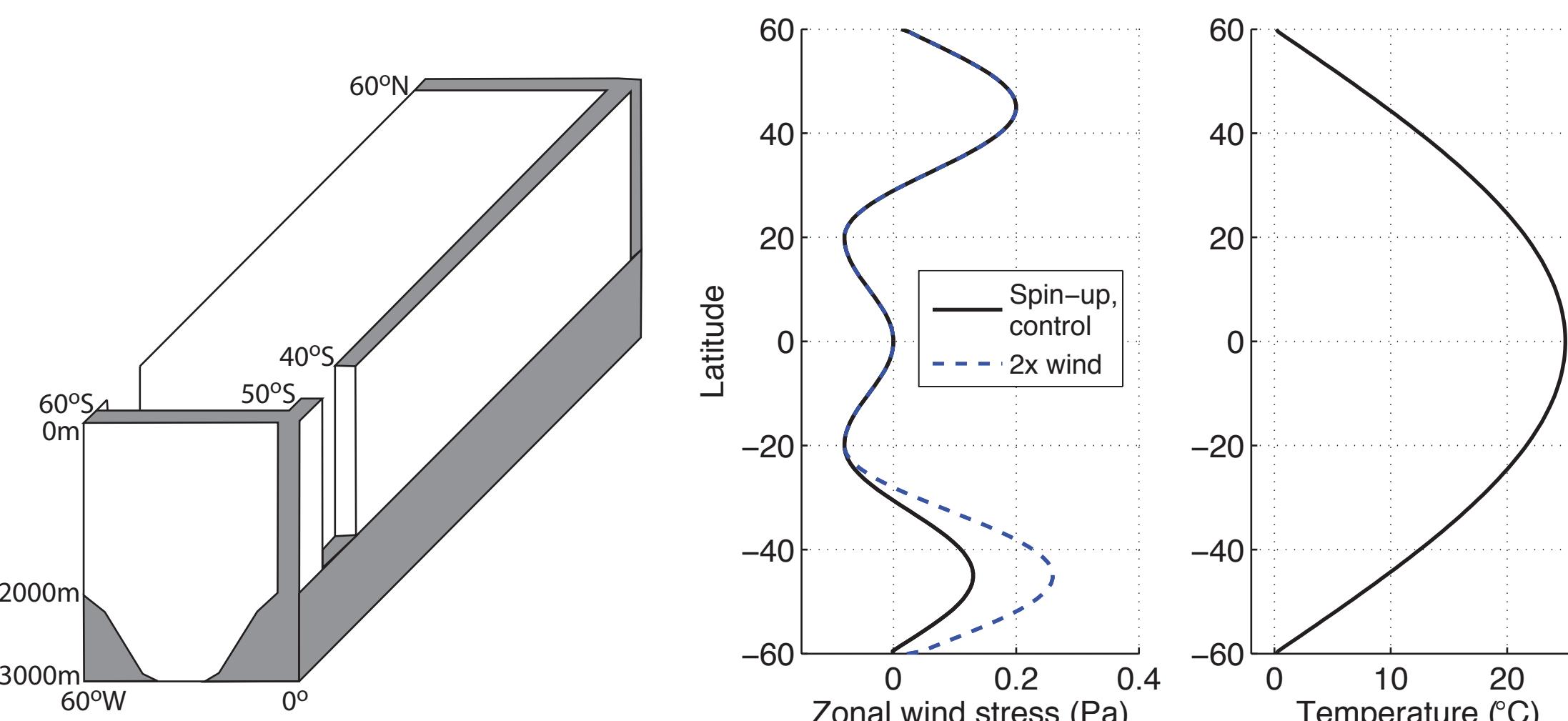


Fig. 2. Model geometry with circumpolar channel (left), surface wind forcing (middle), and surface temperature profile (right). The domain has 42 vertical levels and an eddy-permitting horizontal resolution ( $1/6^\circ \times 1/6^\circ$ ).

## Results: variability

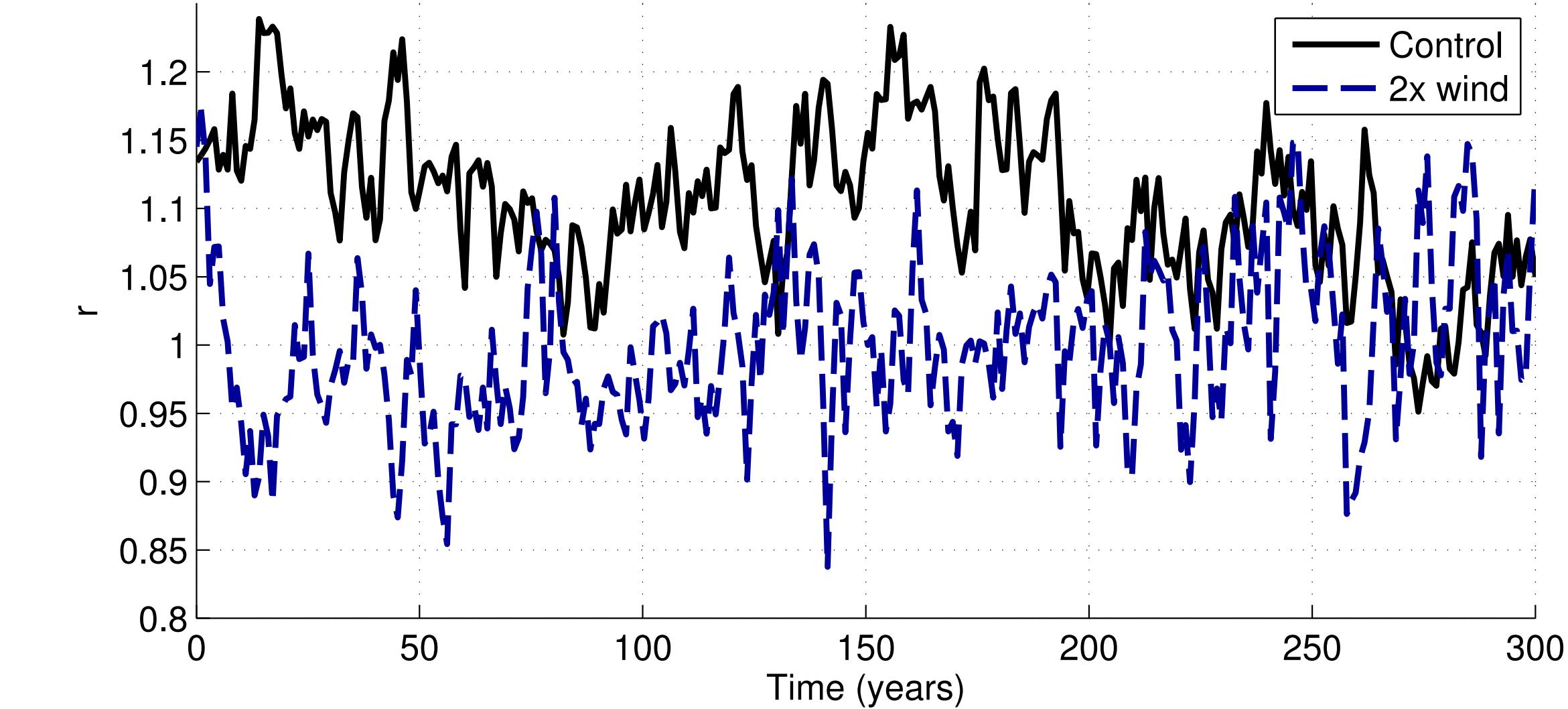


Fig. 3. Mean value of  $r$  (the PV homogenization metric) in the circumpolar channel for the control (black, solid) and strong wind (blue, dashed) cases.

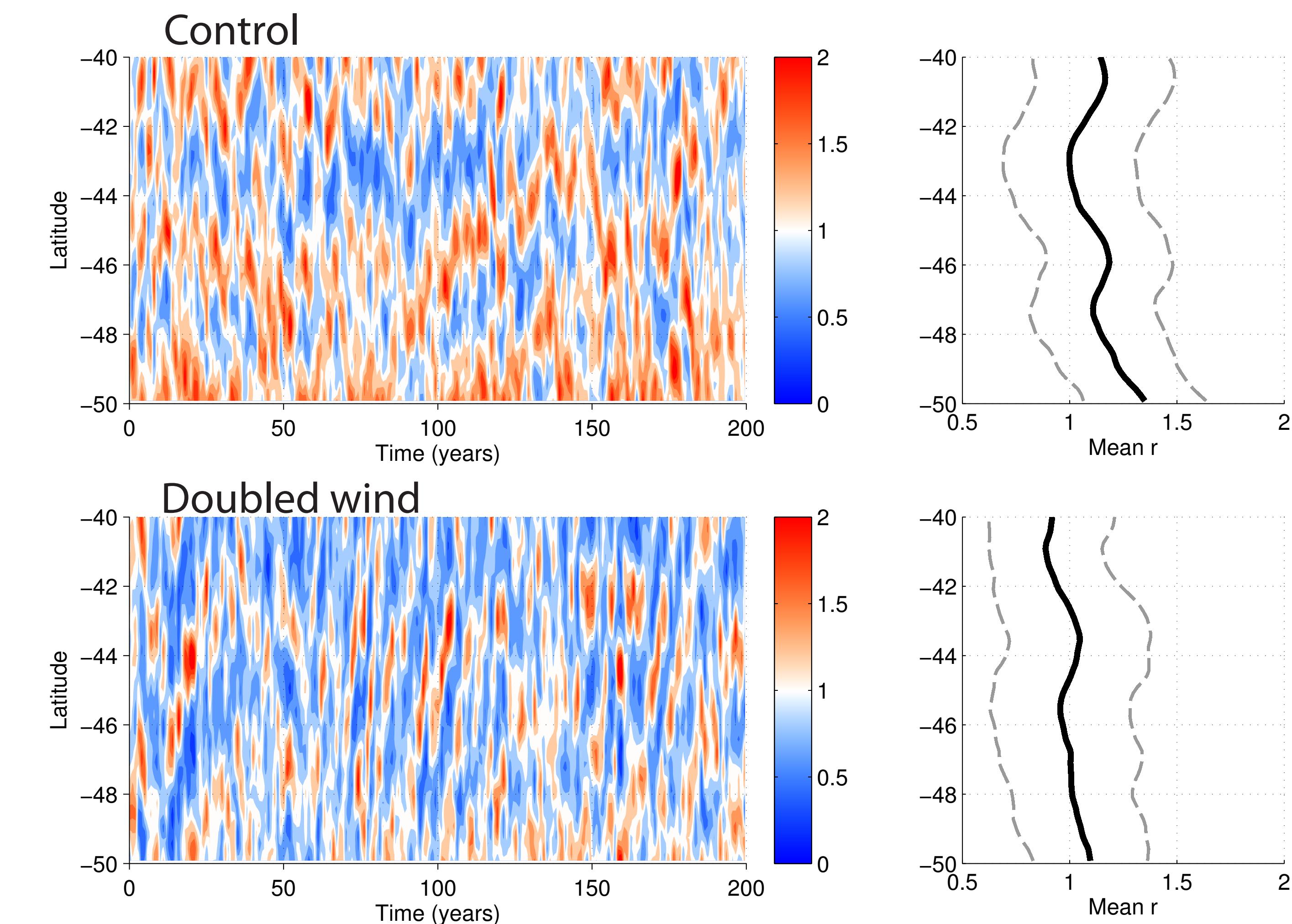


Fig. 4. Hovmöller diagrams (left column) and long-term zonal mean (right column) of  $r$  for both the weak wind (top row) and strong wind (bottom row) cases.

$r > 1$  stratification dominant (negative PV gradient)  
 $r = 1$  stratification/planetary balance (zero PV gradient)  
 $r < 1$  planetary constraint dominant (positive PV gradient)