

# A Simple Vertical Transport Parameterization for Convective Boundary Layer Simulations at Gray-Zone Resolutions

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## Backgrounds

### The Gray-zone problem of the SGS turbulence model

FROM "the theoretical view"

Two traditional numerical modeling methods of turbulent flows according to  $\Delta/l$  (Wyngaard 2004)

$l$ : the scale of energy-containing turbulence  
 $\Delta$ : the scale of the spatial filter used in Eq. of motion

Larger scale  $\leftarrow \Delta \gg l$   $\Delta \sim l$   $\Delta \ll l$   $\rightarrow$  Smaller scale

Mesoscale modeling : all the turbulence is parameterized by so-called PBL parameterization.

No SGS model designed for this scale!

LES : Only small-scale eddies are parameterized ( $\Delta$  in the inertial subrange).

$\rightarrow \Delta \sim l$ : "Terra Incognita" or "Gray zone" (NWP terminology)

TO "a practical view"

The bidirectional consequences of the gray-zone problem according to the SGS vertical transport model used (Honnert et al. 2011; LeMone et al. 2013; Ching et al. 2014)

$$\overline{w\phi}^\Delta - \overline{w}^\Delta \overline{\phi}^\Delta = -K_\phi \frac{\partial \overline{\phi}^\Delta}{\partial z} + F_{w\phi}^{NL} \quad (1) \text{ Term for local (L) transport by small eddies}$$

$$(1) \quad (2) \quad (2) \text{ Term for nonlocal (NL) transport by large eddies}$$

Simulations at the gray-zone resolution show that using the SGS models

with term (2)

(e.g., nonlocal PBL schemes)

$\rightarrow$  Overestimated SGS transport

$\rightarrow$  Excessive diffusion

$\rightarrow$  Too weak resolved motions

Between?!

without term (2)

(local PBL schemes; LES SGS models)

$\leftarrow$  Underestimated SGS transport

$\leftarrow$  Remaining instability

$\leftarrow$  Too strong resolved motions

$\rightarrow$  The question is how to decrease modeled SGS energy for the nonlocal PBL schemes (or increase it for the local schemes) while leaving an accurate amount of energy for resolved motions!

$\rightarrow$  How to decrease the SGS energy? By reducing the SGS NL transport term?

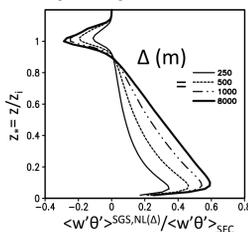
### Resolution dependency of the SGS nonlocal transport profile

Method (Honnert et al. 2011; Dorrestijn et al. 2013; Shin and Hong 2013)

1. Benchmark LES for  $\Delta_{LES} = 25$  m and horizontal domain  $D^2 = 8^2$  km<sup>2</sup>.

2. Through spatial filtering, the reference fields for resolved and SGS transport are calculated for  $\Delta: \Delta_{LES} < \Delta < D$ .

3. By conditional sampling using vertical velocity and a passive scalar (Couvreur et al. 2010), the SGS transport is decomposed into nonlocal (NL) and local (L) SGS transports.



Results – Notes for a simple parameterization

$\checkmark$  The role of NL transport: Surface-layer cooling, Mixed-layer heating, and Entrainment.  $\uparrow$

$\checkmark$  The basic role is kept for different  $\Delta$ .

### In this study: simplification of the problem

A parameterization is designed to "force" the SGS vertical transport to follow the resolution dependency, and its effects are investigated for convective boundary-layer simulations at gray-zone resolutions.

## A simple parameterization

### Representation of vertical heat transport in CBLs

$$\overline{w\theta}^\Delta - \overline{w}^\Delta \overline{\theta}^\Delta = -K_\theta \frac{\partial \overline{\theta}^\Delta}{\partial z} + F_{w\theta}^{NL} \quad (1) \text{ Term for local (L) transport by small eddies}$$

$$(1) \quad (2) \quad (2) \text{ Term for nonlocal (NL) transport by large eddies}$$

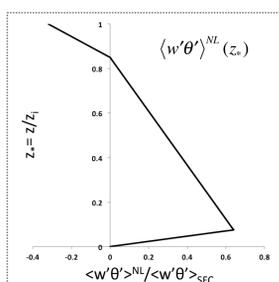
Vertical diffusivity used in conventional PBL schemes (i.e., used for  $\Delta \gg l$ )

(1) Local transport

$$K_\theta(\Delta_*) = K_{\theta, meso} \cdot P_L^{w\theta}(\Delta_*)$$

(2) Nonlocal transport

$$F_{w\theta}^{NL} = \langle w'\theta' \rangle^{NL}(z_*) \cdot P_{NL}^{w\theta}(\Delta_*)$$



A linear profile fit to the LES-derived NL transport profile (cf. Figure in the above section)

Resolution dependency functions for SGS heat transport Honnert et al. (2011) for total (NL + L) SGS heat transport; Shin and Hong (2013) for its decomposition into NL and L parts

NOTE The SGS NL transport profile only depends on the external forcing (surface heating and mean wind shear), as it is fit to the domain-averaged LES profile.

More details in Shin and Hong (2014)

## Evaluation

### Experimental setup – Idealized simulations

Model: LES version of WRFV3.5.1

Forcing:  $\langle w'\theta' \rangle_{SFC} = 0.2$  K m s<sup>-1</sup>;  $U_g = 10$  m s<sup>-1</sup>

Initial  $\theta$  profile:  $\theta = 300$  K for  $z \leq 925$  m; Inversion strength =  $0.053$  K m<sup>-1</sup>

Table 1: SGS turbulence models, horizontal grid size, horizontal domain size

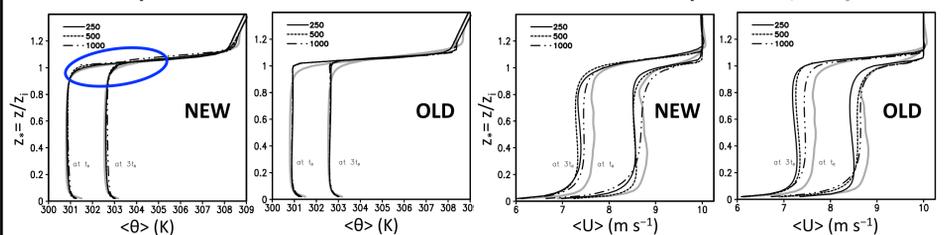
	Vertical SGS model	Horizontal SGS model	Grid size (m)	Horizontal domain (km <sup>2</sup> )
Benchmark LES	3D TKE (Deardorff 1980)		25	8 <sup>2</sup>
GZ Reference	Derived from the Benchmark LES		250, 500, 1000	8 <sup>2</sup>
NEW	NEW	3DTKE	250, 500, 1000	8 <sup>2</sup> , 16 <sup>2</sup> , 32 <sup>2</sup>
OLD	YSU (Hong et al. 2006)	3DTKE	250, 500, 1000	8 <sup>2</sup> , 16 <sup>2</sup> , 32 <sup>2</sup>

The simple NEW model is evaluated against the LES and gray-zone (GZ) reference data, and compared with a conventional nonlocal PBL parameterization (OLD).

### Results

#### 1. Mean profiles

Black - experiment, Gray - LES

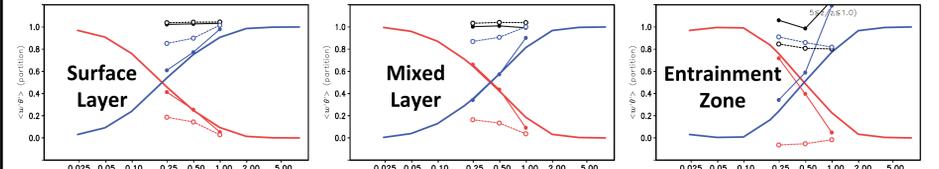


$\checkmark$  Improvement in the entrainment and the inversion strength

$\checkmark$  No degradation or improvement in  $\langle U \rangle$

#### 2. Grid-size dependency of resolved, SGS, and total (resolved + SGS) transports

— LES ● NEW ○ OLD RED - resolved, Blue - SGS, Black - total

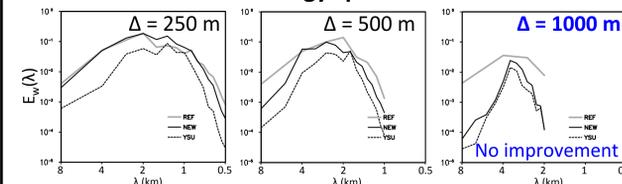


$\checkmark$  The OLD nonlocal scheme (○...○) overestimates the SGS transport, and suppresses resolved motions (cf. Honnert et al. 2011; LeMone et al. 2013; Ching et al. 2014).

$\checkmark$  The NEW model (●...●) improves the resolution dependency of the SGS transport, since  $P(\Delta)$  functions fit to the LES results are used.

#### 3. Resolved motions

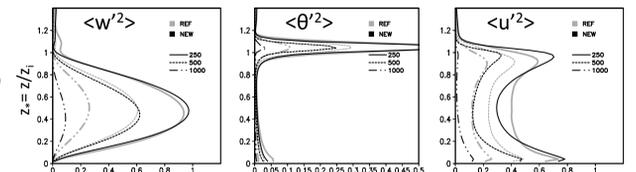
Energy spectrum



NOTE For  $\lambda < 6-7\Delta$ , the NEW & OLD experiments are affected by the 6<sup>th</sup>-order numerical diffusion due to the 5<sup>th</sup>-order advection scheme (cf. Skamarock 2004). For a better comparison, the reference fields (gray) are filtered by a 6<sup>th</sup>-order numerical filter.

$\uparrow$  Due to the reduced SGS transport the remaining resolved energy for the NEW is relatively closer to the reference spectrum, compared to the OLD.

Resolved variances



$\checkmark$  The resolved energy are still underestimated in the NEW, especially at  $\Delta = 1000$  m.

## Summary and Discussions

- The CBL simulations are improved by using the nonlocal transport profile fit to the LES and the resolution dependency functions in the SGS model (as expected).
- The new algorithm introduced here is based on the empirical fitting and corresponding numerical parameters. Accepting the algorithm as a complete scheme or not might be another part of the "gray-zone" problem.

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### Acknowledgement

We gratefully acknowledge Jimmy Dudhia and Peggy LeMone at NCAR whose thorough reviews improved the manuscript, Yign Noh at YSU for his comments during the early stages of our study, and Sang-Hun Park at NCAR for his help in the use of the sixth-order filter in calculating the reference energy spectrum. We would like to acknowledge high-performance computing support from Yellowstone (ark:/85065/d7wd3xhc) provided by NCAR's Computational and Information Systems Laboratory (CISL), sponsored by the National Science Foundation (NSF).