



# *Non-linear interaction between the lower-atmosphere and vegetation canopy flows*

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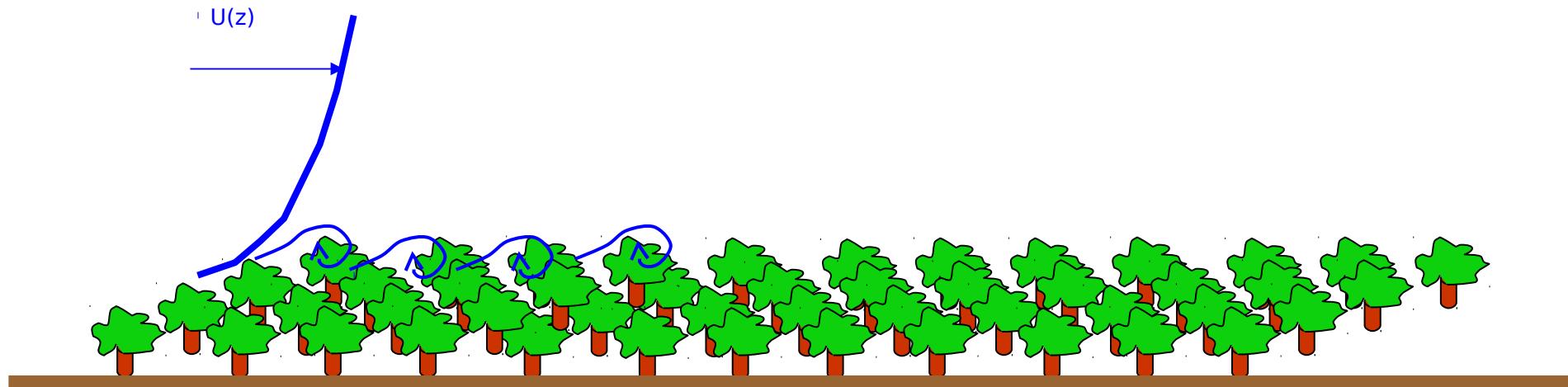
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# Context & Motivation

## Flow over vegetation canopy in near-neutral configuration



- Mixing layer analogy explaining most of the statistical features (Finnigan, 2000)
- Model of the eddy organization in the canopy and RSL based on a double-hairpin structure (Finnigan, Shaw & Patton, 2009)
- But also presence of coherent structures in the atmospheric boundary layer (Lin et al, 1996, Drobinski et al, 2004)



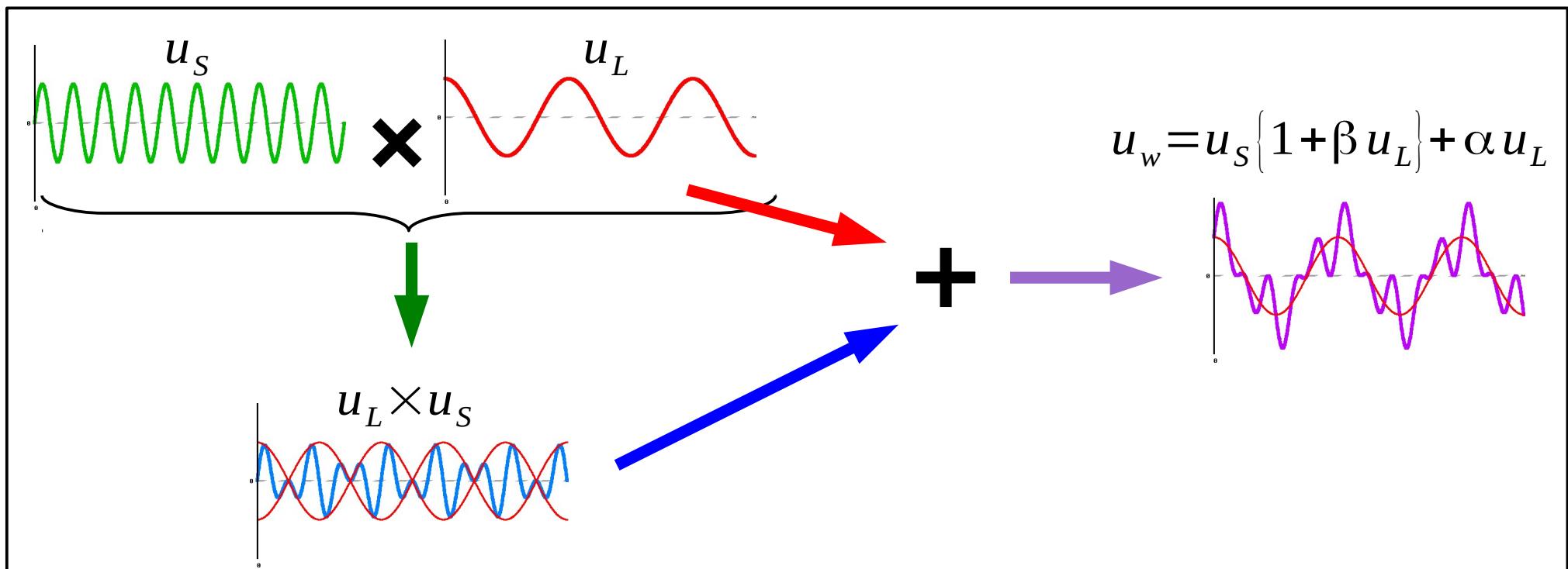
Interaction, coupling mechanism ?

# Context & Motivation

Recent finding in smooth-wall boundary layer and channel flows

Mathis, Hutchins & Marusic, JFM, 2009, 2011;

→ Amplitude modulation of the near-wall turbulence by the larger-scales



→ Same mechanism in atmospheric flow over vegetation canopy ?

# Methodology

Analysis based on a 3d volume corresponding to a time instance of a LES (Patton et al. 2012) with the parameters:

- Vegetation specified by a height-dependent foliage area density and an element drag coefficient;
- Canopy height:  $h = 20\text{m}$ , 10 grid points;
- Domain dimensions: 
$$\begin{cases} L_x \times L_y \times L_z = 5120 \times 5120 \times 2048 \text{ m}^3 \\ N_x \times N_y \times N_z = 2048 \times 2048 \times 1024 \end{cases}$$
- Main parameters ( $u^*$ ,  $Q^*$ ,  $L$  and  $w^*$  evaluated at canopy top): *weakly convective*

| $U_g$<br>( $\text{m s}^{-1}$ ) | $V_g$<br>( $\text{m s}^{-1}$ ) | $u_*$<br>( $\text{m s}^{-1}$ ) | $Q_*$<br>( $\text{m K s}^{-1}$ ) | $z_i$<br>(m) | $L$<br>(m) | $-z_i/L$ | $w_*$<br>( $\text{m s}^{-1}$ ) |
|--------------------------------|--------------------------------|--------------------------------|----------------------------------|--------------|------------|----------|--------------------------------|
| 10                             | 0                              | 0.86                           | 0.2                              | 998          | -226       | 3        | 1.92                           |

→ Development of methods based on third-order statistics:  
Use of auto- and cross-bispectra and bicoherence

# Auto-Bispectrum: definition

- Auto-bispectrum of  $u(t)$  defined as:

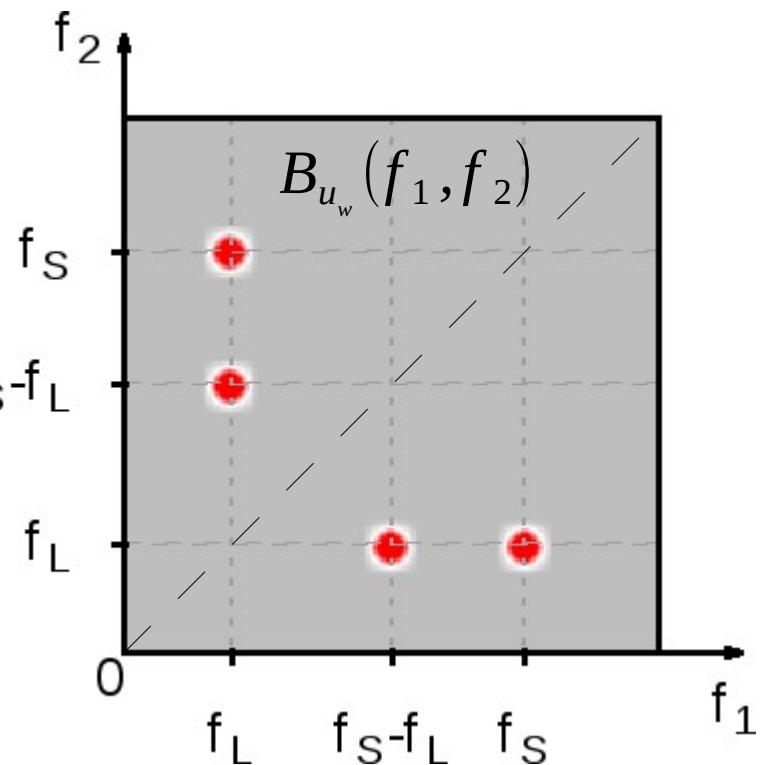
$$B_u(f_1, f_2) = \langle \hat{U}(f_1) \hat{U}(f_2) \hat{U}^*(f_3) \rangle$$

- Account for *non-linear coupling* between 3 frequencies linked by

$$\begin{cases} f_1 + f_2 = f_3 \\ \varphi_1 + \varphi_2 - \varphi_3 = Cst \end{cases}$$

- If  $u_s$  and  $u_L$  are pure sine waves:

$$u_w = u_s (1 + \beta u_L) + \alpha u_L \quad \rightarrow$$



where  $\hat{U}(f) = |\hat{U}(f)| e^{i\varphi(f)}$  with  $|\hat{U}(f)|$ : amplitude of the wave of frequency  $f$   
 $\varphi(f)$ : phase of the wave of frequency  $f$

# Auto-Bispectrum: properties

- $B_u(f_1, f_2) = 0$  if no coupling between  $f_1$ ,  $f_2$  and  $f_3$
- Directly linked to the skewness by:  $\langle u^3(t) \rangle = \sum_{f_1, f_2} \Re(B_u(f_1, f_2))$

- *Cross-bispectrum* can be defined as well

$$B_{uvv}(f_1, f_2) = \langle \hat{U}(f_1) \hat{V}(f_2) \hat{V}^*(f_3) \rangle$$

*Interaction between  
u(t) and v(t)*

- *Bicoherence*: normalized bispectrum

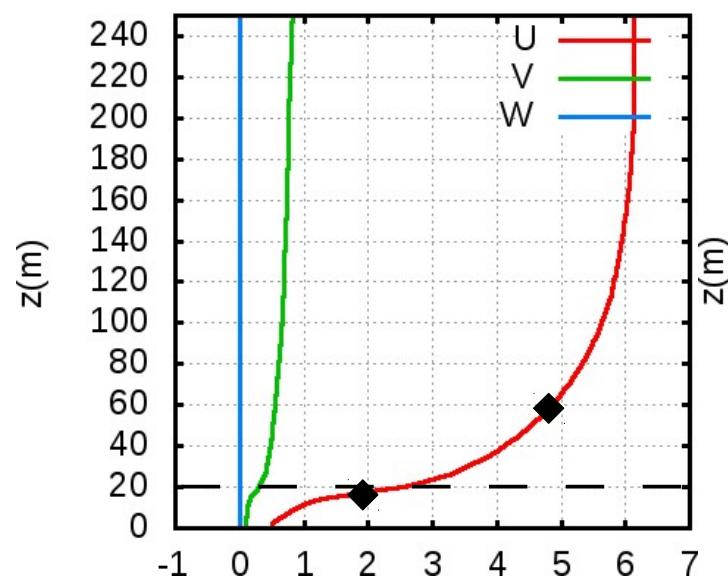
$$b_{uvv}(f_1, f_2) = \frac{|B_{uvv}(f_1, f_2)|}{\left( \langle |U(f_1)V(f_2)|^2 \rangle \cdot |V(f_3)V^*(f_3)| \right)^{1/2}}$$

→ Use of wavelet transform (*Morlet mother wavelet*, Milligen et al., 1995)  
→ Scale decomposition in the longitudinal direction x

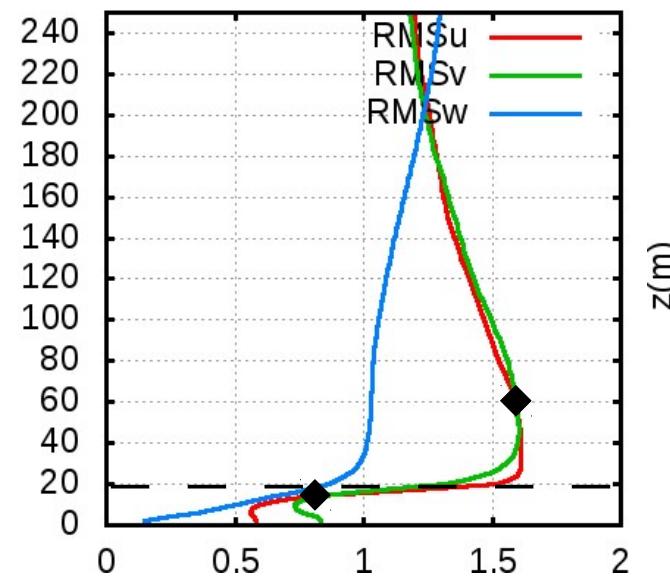
# Results: one-point statistics

Velocity statistics: Averages over the horizontal plane

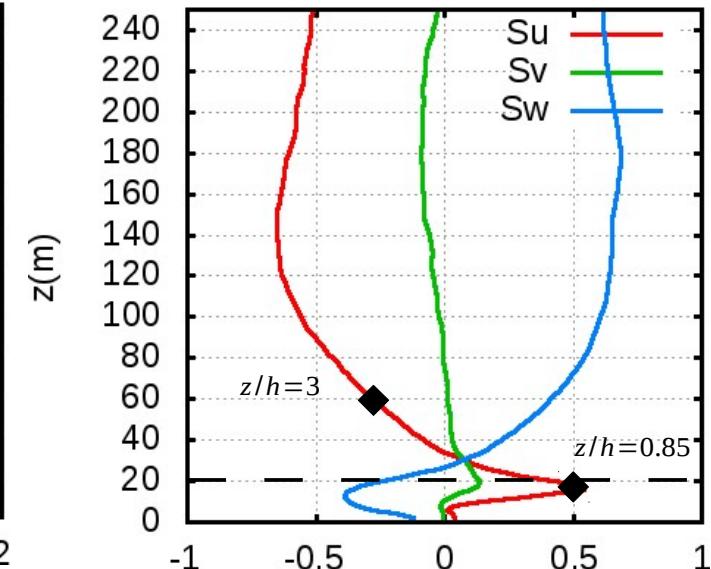
Mean velocity (m/s)



Velocity rms (m/s)

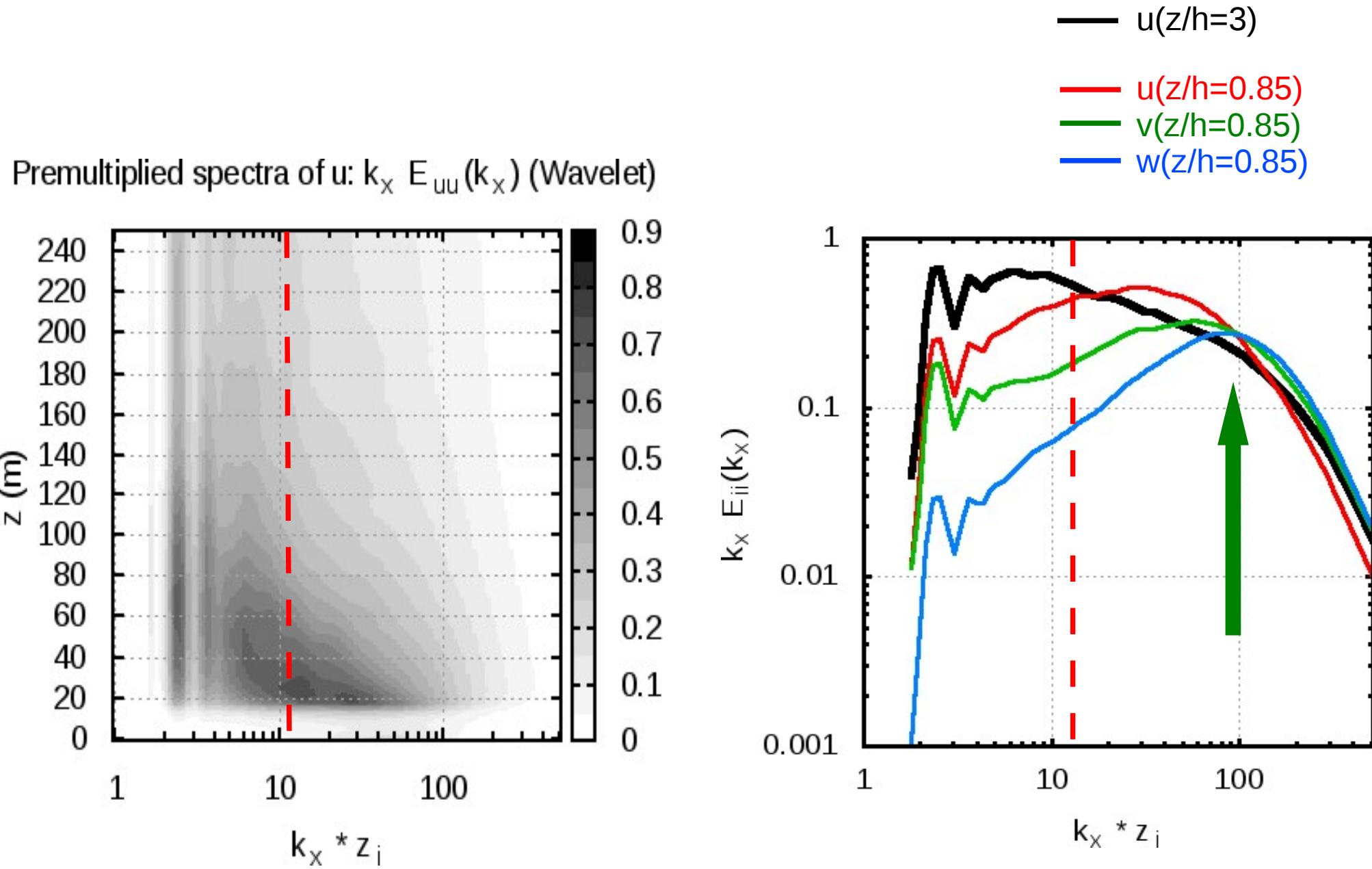


Velocity skewness

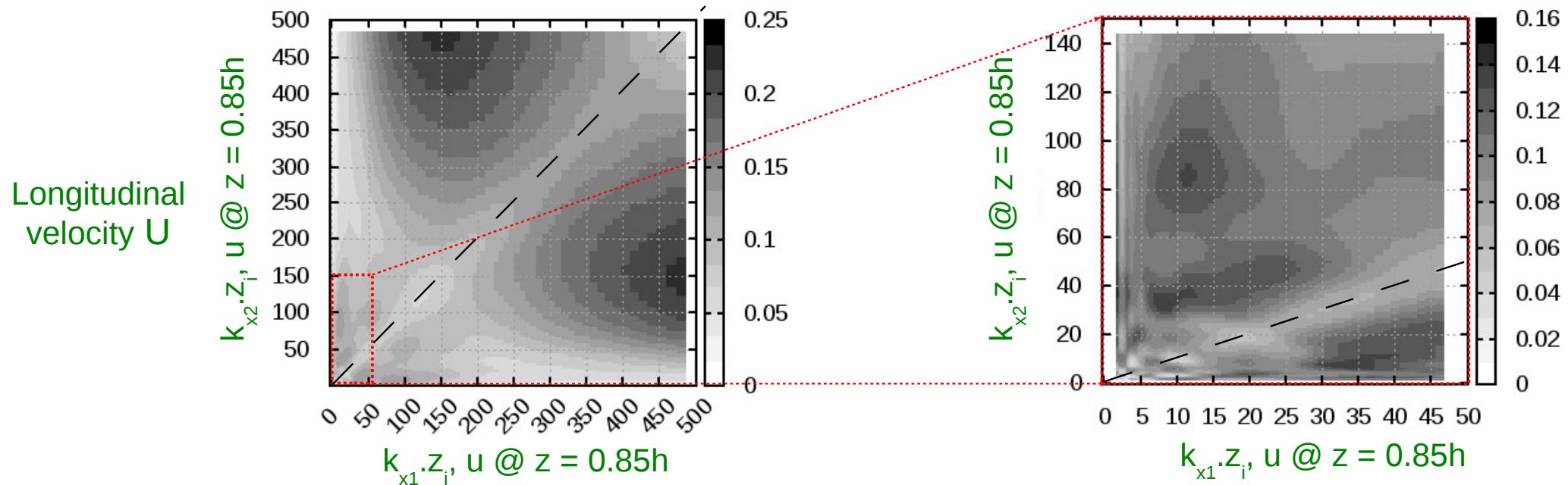


- Longitudinal velocity  $U$
- Transversal velocity  $V$
- Vertical velocity  $W$

# Wavelet energy spectra of velocity

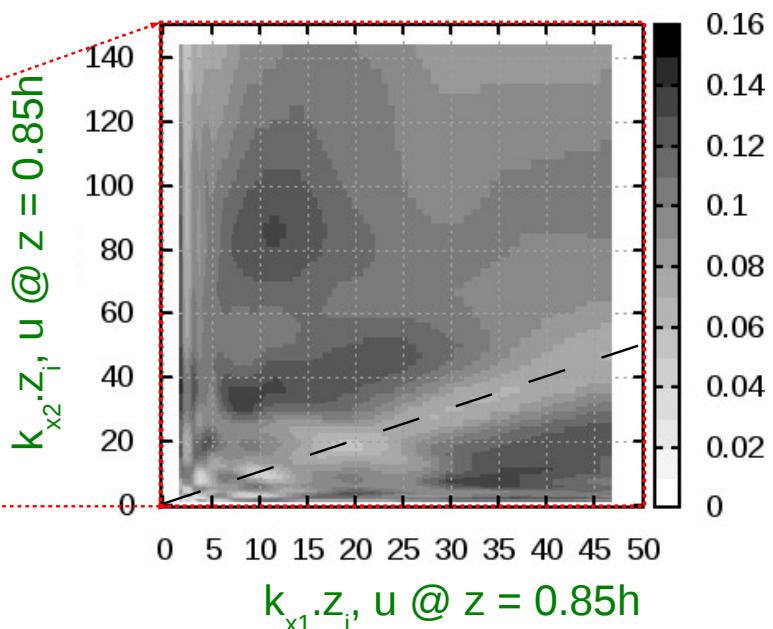
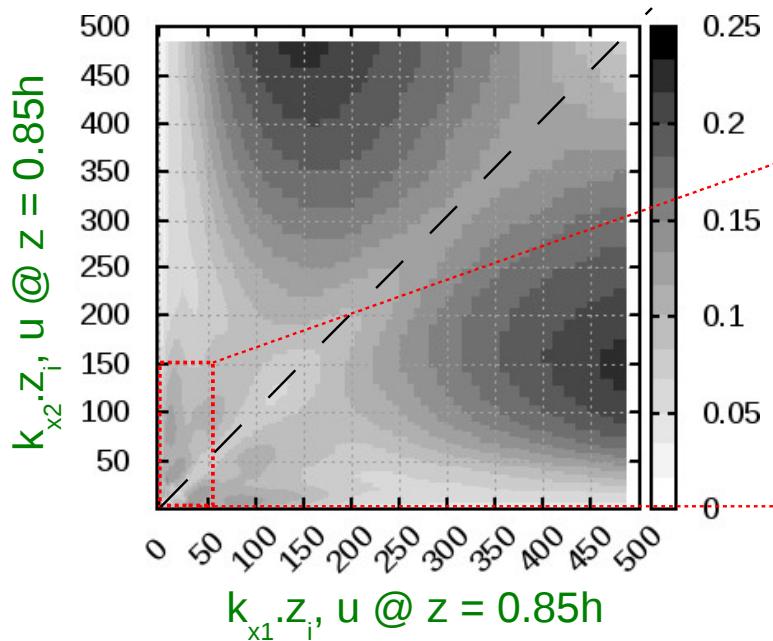


# Auto-Bicoherence @ $z/h = 0.85$

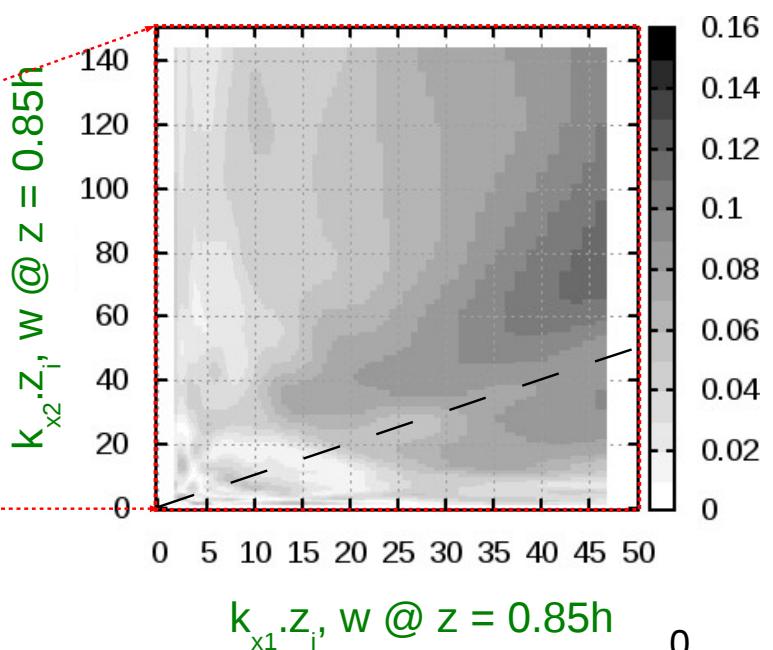
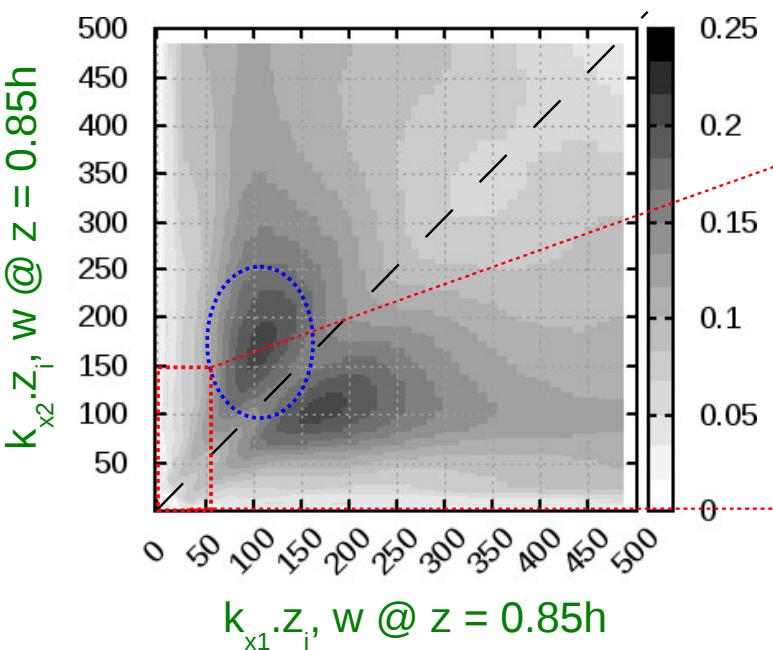


# Auto-Bicoherence @ $z/h = 0.85$

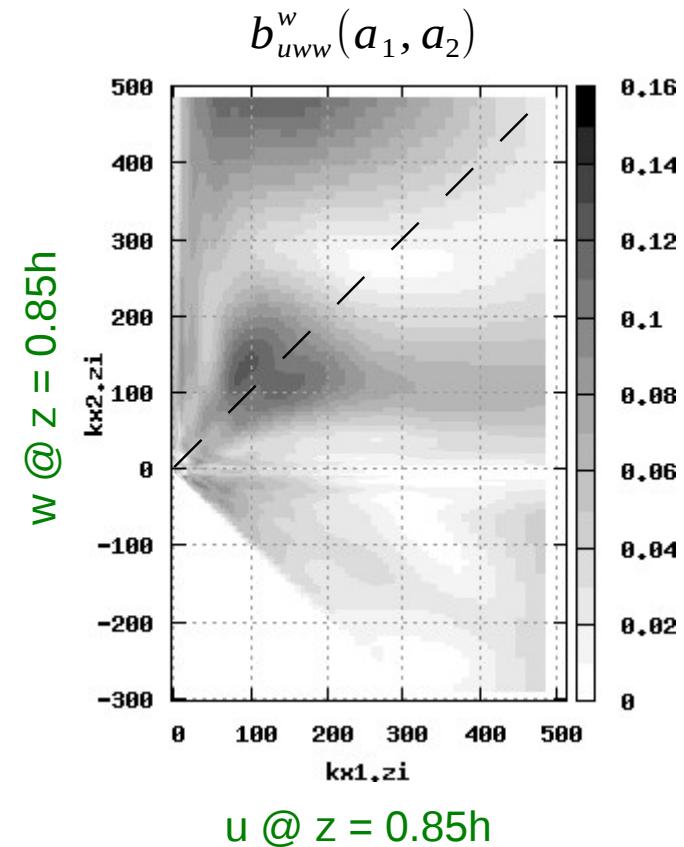
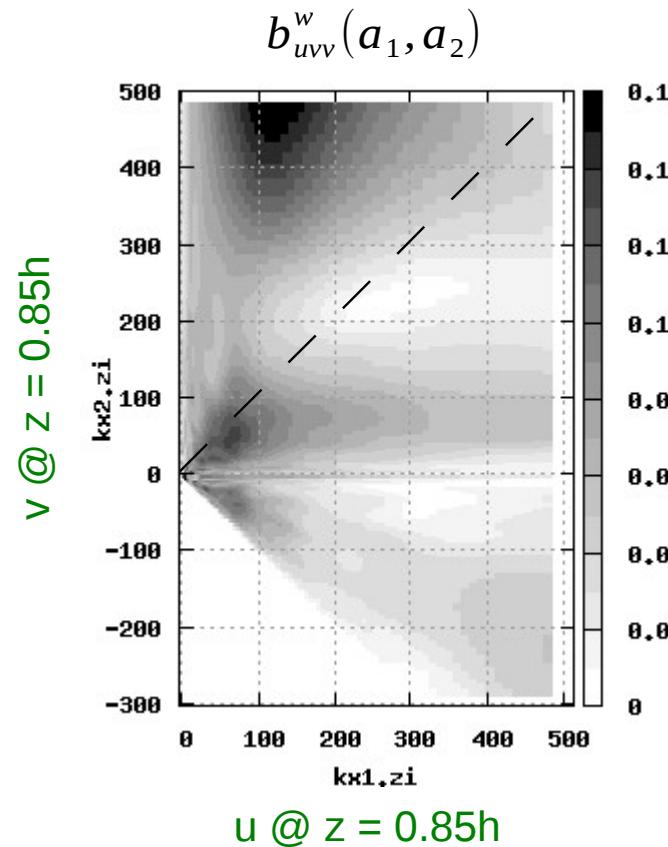
Longitudinal  
velocity  $U$



Vertical  
velocity  $W$



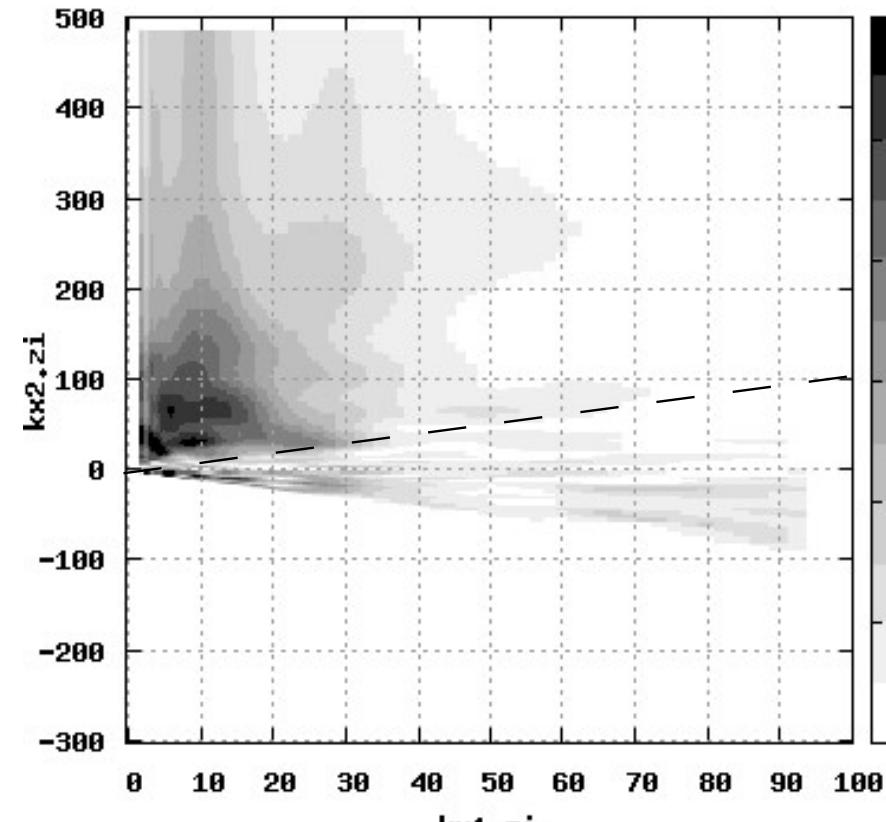
# One-point cross-Bicoherence @ $z = 0.85h$



- For the 3 components: non-linear interactions among smaller-scales
- Non-linear interactions between large- and smaller-scales within  $u$
- Non-linear interactions between canopy-scales within  $w$
- Non-linear interactions between large-scales of  $u$  and smaller-scales of  $w$

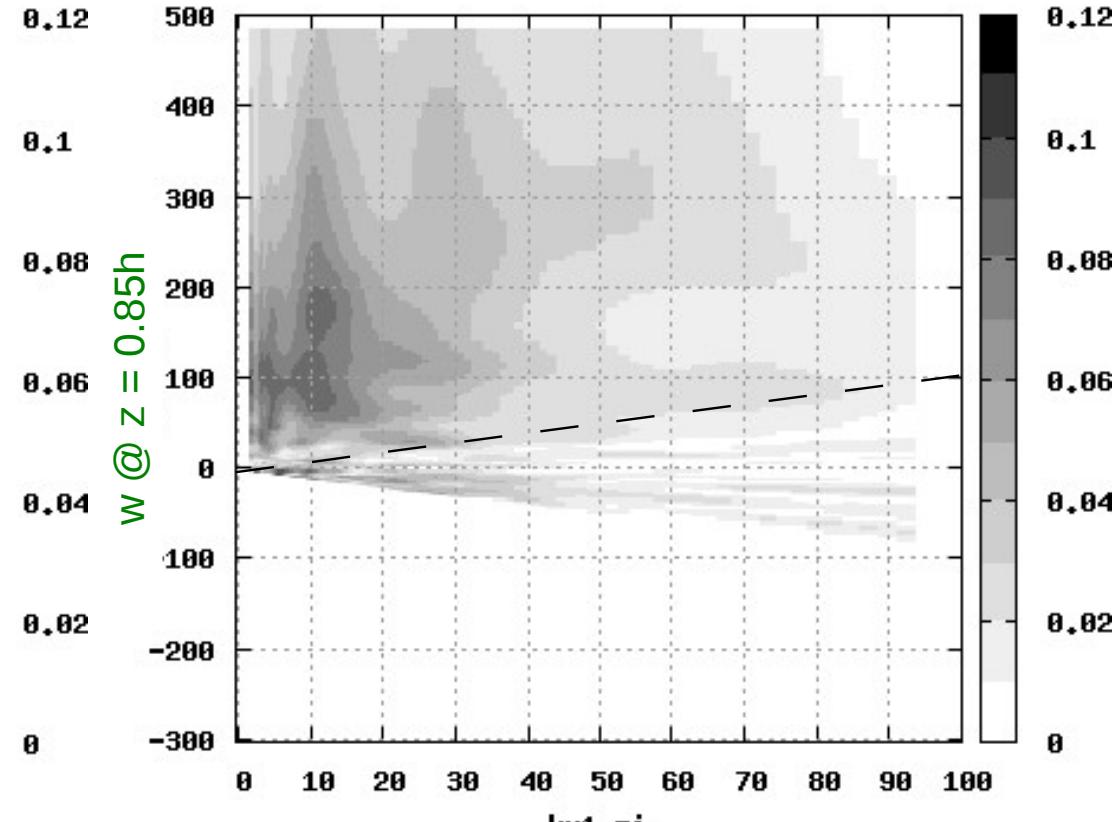
# Two-point Cross-Bicoherence: $u @ z = 3h$

with  $u @ z = 0.85h$



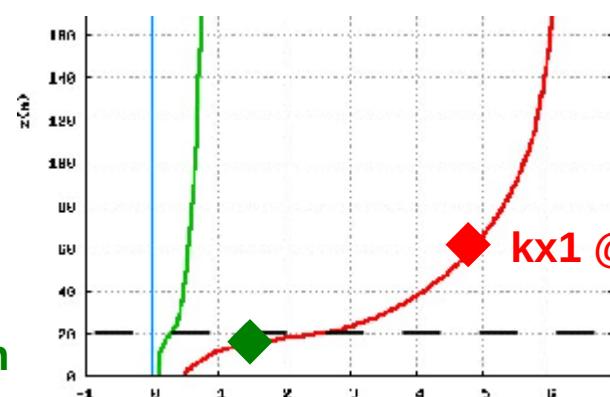
$u @ z = 3h$

with  $w @ z = 0.85h$



$u @ z = 3h$

$kx2$  &  $kx3$   
@  $z = 0.85h$



# Conclusions and perspectives

## Conclusion from the bispectral analysis:

- Non-linear interactions among all scales;
- $w$  bears the footprint of canopy-scale interaction;
- Non-linear interactions between larger-scales of  $u$  and smaller-scales of the 3 components;
- Coupling associated to modes of large vertical extent.

## Future plans:

- Diagnostic tool for non-linear interaction detection;
- Influence of the stability condition on the non-linear interactions;
- Quantitative estimation of non-linear coupling and energy transfer and modeling;
- Extension to experimental data from the CHATS campaign



# Thank you for your attention