



Non-linear interaction between the lower-atmosphere and vegetation canopy flows

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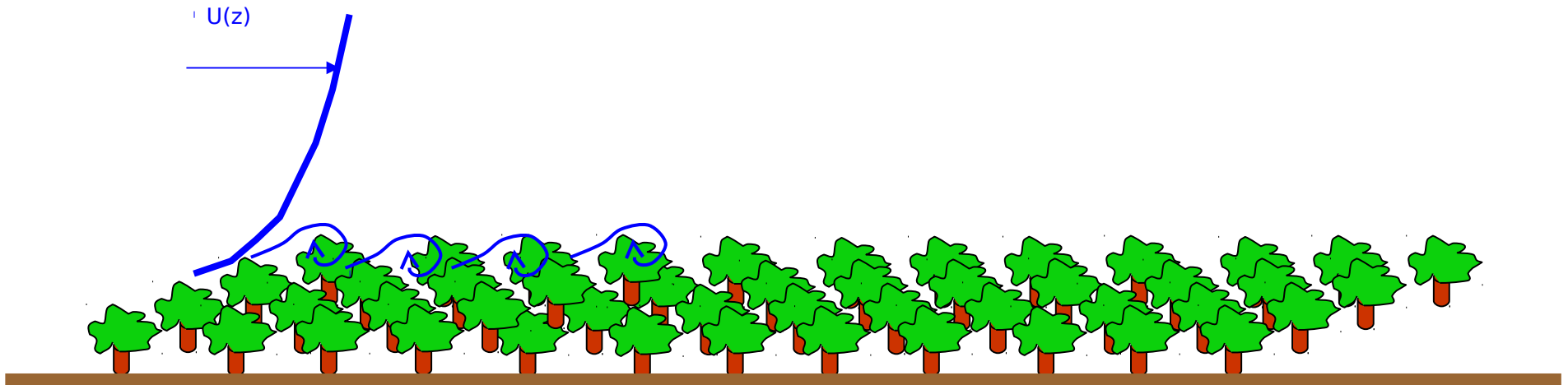
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Context & Motivation

Flow over vegetation canopy in near-neutral configuration



- Mixing layer analogy explaining most of the statistical features (Finnigan, 2000)
- Model of the eddy organization in the canopy and RSL based on a double-hairpin structure (Finnigan, Shaw & Patton, 2009)
- But also presence of coherent structures in the atmospheric boundary layer (Lin et al, 1996, Drobinski et al, 2004)

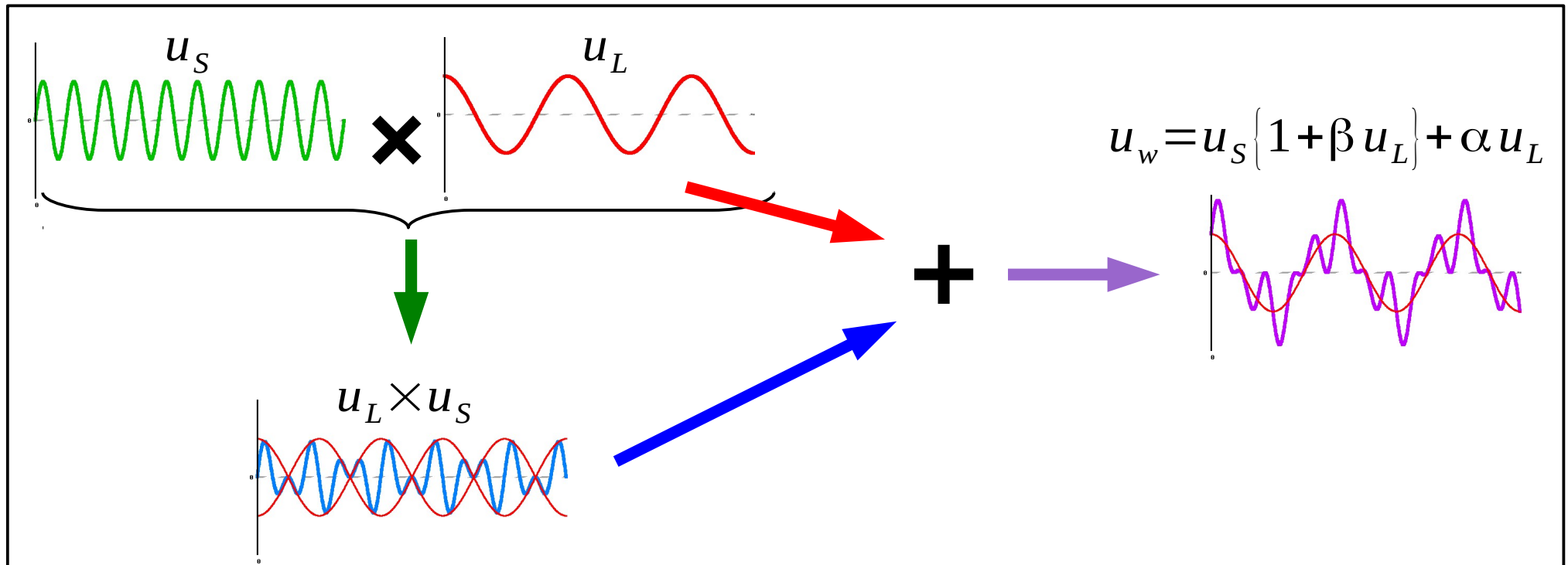
➔ Interaction, coupling mechanism ?

Context & Motivation

Recent finding in smooth-wall boundary layer and channel flows

Mathis, Hutchins & Marusic, JFM, 2009, 2011;

➔ Amplitude modulation of the near-wall turbulence by the larger-scales



➔ Same mechanism in atmospheric flow over vegetation canopy ?

Methodology

Analysis based on a 3d volume corresponding to a time instance of a LES (Patton et al. 2012) with the parameters:

- Vegetation specified by a height-dependent foliage area density and an element drag coefficient;
- Canopy height: $h = 20\text{m}$, 10 grid points;
- Domain dimensions:
$$\begin{cases} L_x \times L_y \times L_z = 5120 \times 5120 \times 2048 \text{ m}^3 \\ N_x \times N_y \times N_z = 2048 \times 2048 \times 1024 \end{cases}$$
- Main parameters (u^* , Q^* , L and w^* evaluated at canopy top): *weakly convective*

U_g	V_g	u_*	Q_*	z_i	L	$-z/L$	w_*
(m s^{-1})	(m s^{-1})	(m s^{-1})	(m K s^{-1})	(m)	(m)		(m s^{-1})
10	0	0.86	0.2	998	-226	3	1.92



Development of methods based on third-order statistics:

Use of auto- and cross-bispectra and bicoherence

Auto-Bispectrum: definition

- Auto-bispectrum of $u(t)$ defined as:

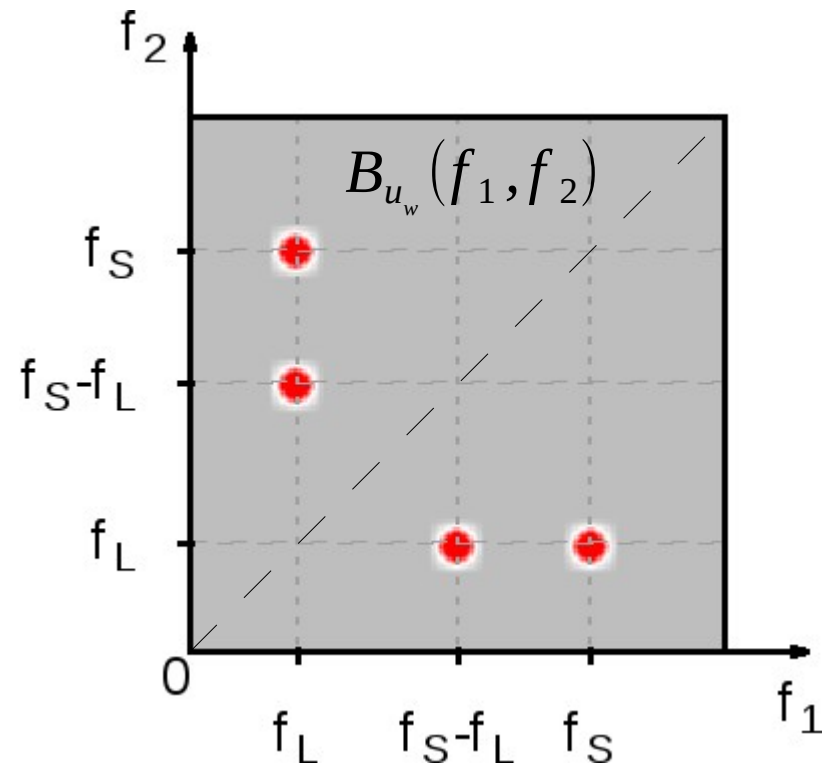
$$B_u(f_1, f_2) = \langle \hat{U}(f_1) \hat{U}(f_2) \hat{U}^*(f_3) \rangle$$

- Account for *non-linear coupling* between 3 frequencies linked by

$$\begin{cases} f_1 + f_2 = f_3 \\ \varphi_1 + \varphi_2 - \varphi_3 = Cst \end{cases}$$

- If u_s and u_L are pure sine waves:

$$u_w = u_s \{1 + \beta u_L\} + \alpha u_L \quad \longrightarrow$$



where $\hat{U}(f) = |\hat{U}(f)| e^{i\varphi(f)}$ with $\begin{cases} |\hat{U}(f)|: \text{amplitude of the wave of frequency } f \\ \varphi(f): \text{phase of the wave of frequency } f \end{cases}$

Auto-Bispectrum: properties

- $B_u(f_1, f_2) = 0$ if no coupling between f_1 , f_2 and f_3
- Directly linked to the skewness by: $\langle u^3(t) \rangle = \sum_{f_1, f_2} \Re(B_u(f_1, f_2))$
- *Cross-bispectrum* can be defined as well

$$B_{uvv}(f_1, f_2) = \langle \hat{U}(f_1) \hat{V}(f_2) \hat{V}^*(f_3) \rangle$$

*Interaction between
u(t) and v(t)*

- *Bicoherence*: normalized bispectrum

$$b_{uvv}(f_1, f_2) = \frac{|B_{uvv}(f_1, f_2)|}{\left(\langle |U(f_1)V(f_2)|^2 \rangle \cdot |V(f_3)V^*(f_3)| \right)^{1/2}}$$

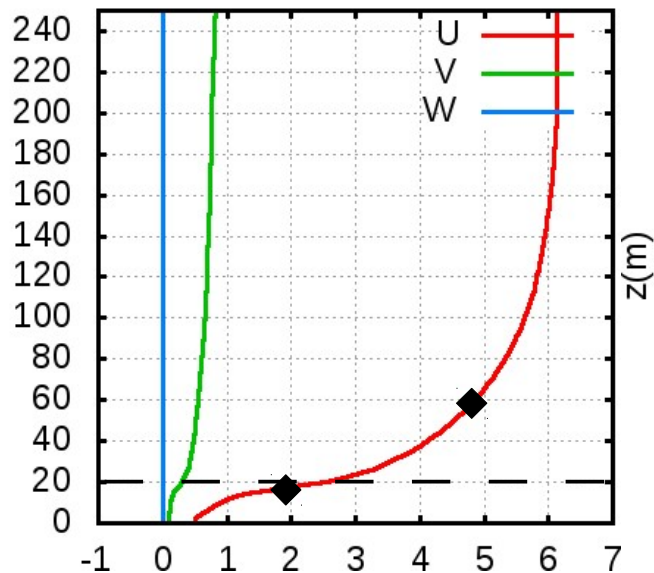


- Use of wavelet transform (*Morlet mother wavelet*, Milligen et al., 1995)
- Scale decomposition in the longitudinal direction x

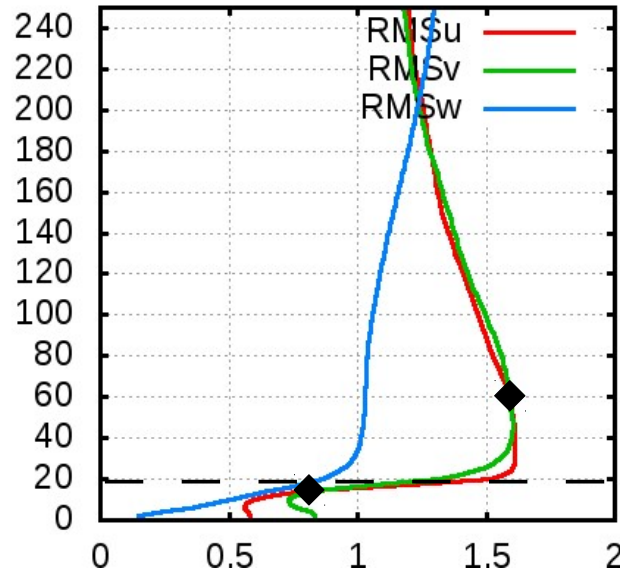
Results: one-point statistics

Velocity statistics: Averages over the horizontal plane

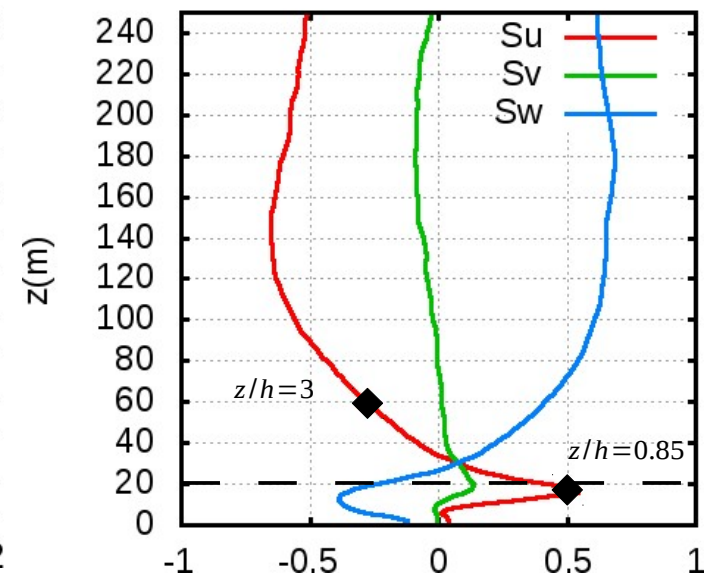
Mean velocity (m/s)



Velocity rms (m/s)



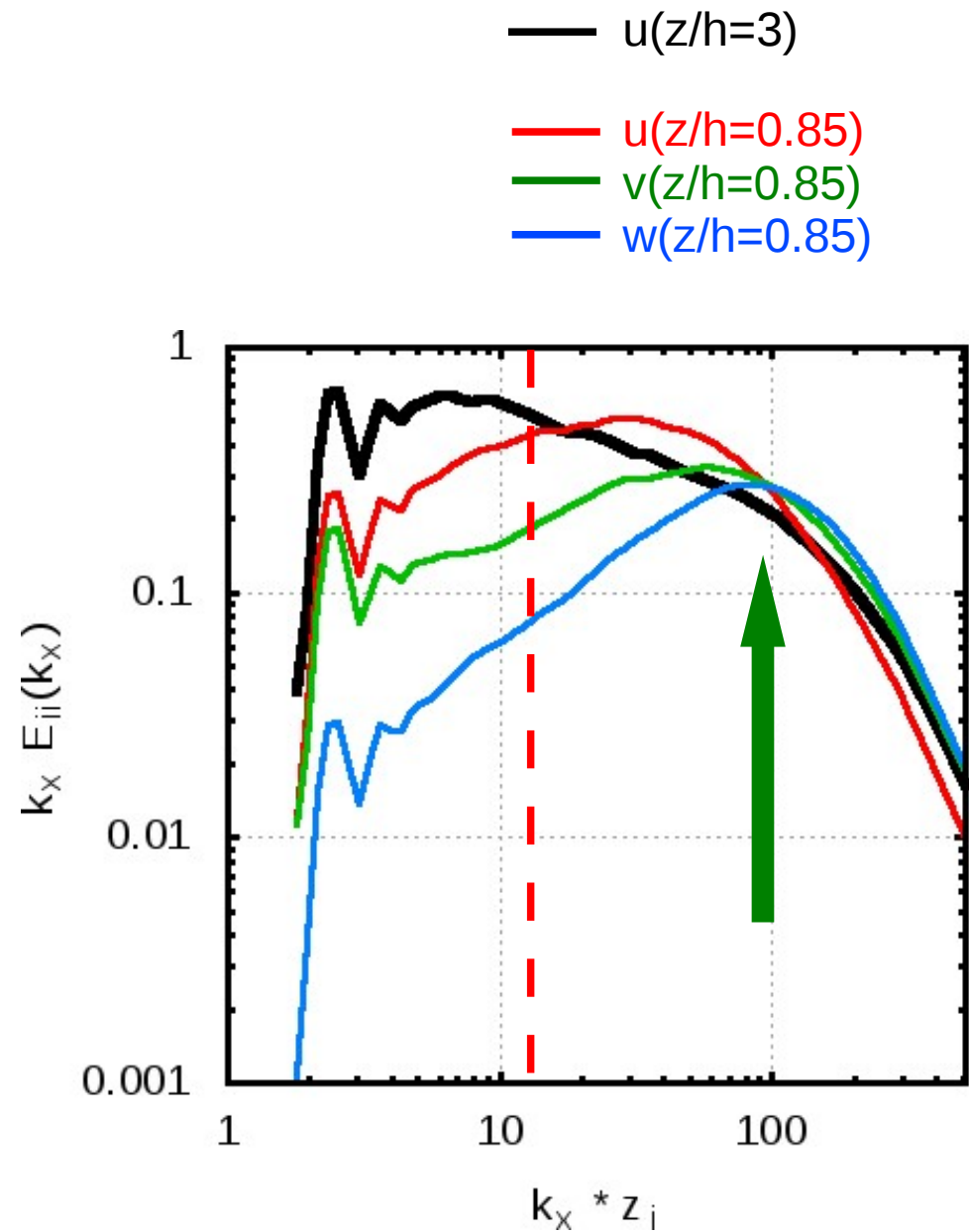
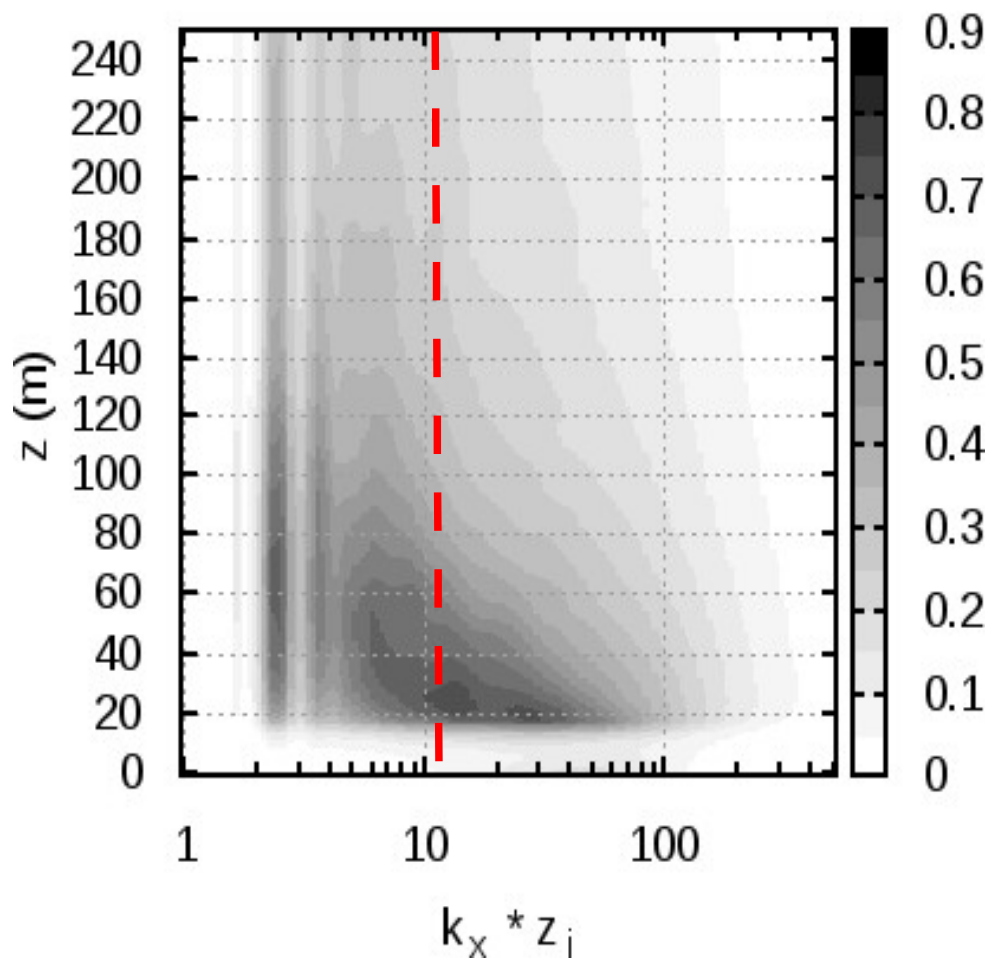
Velocity skewness



- Longitudinal velocity U
- Transversal velocity V
- Vertical velocity W

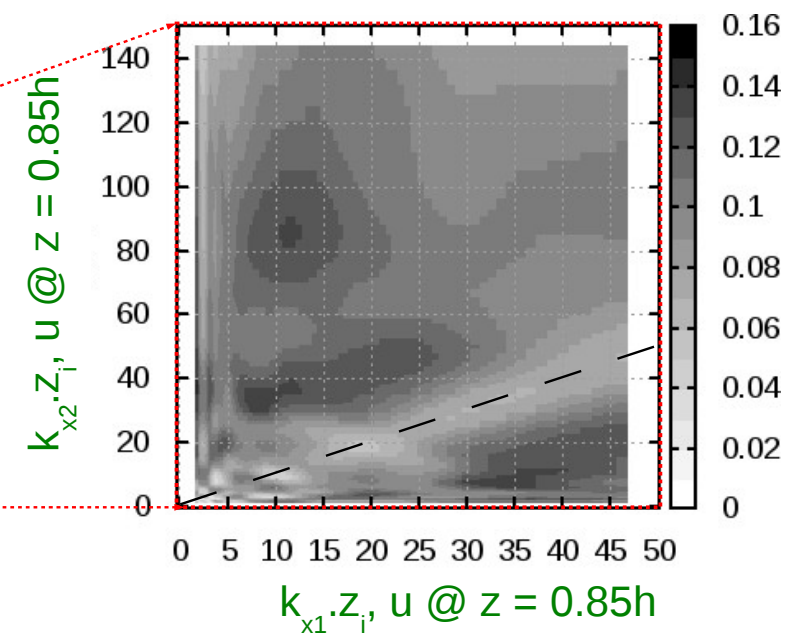
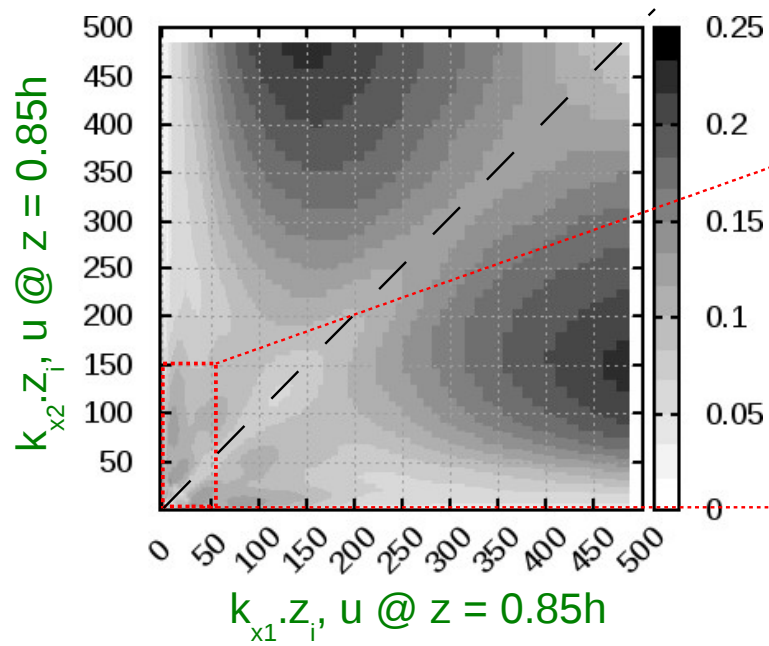
Wavelet energy spectra of velocity

Premultiplied spectra of u: $k_x E_{uu}(k_x)$ (Wavelet)



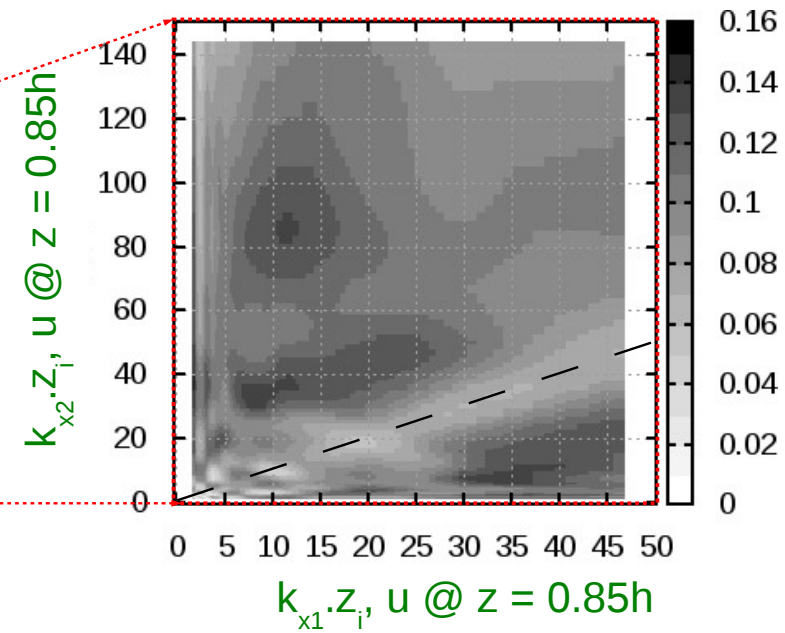
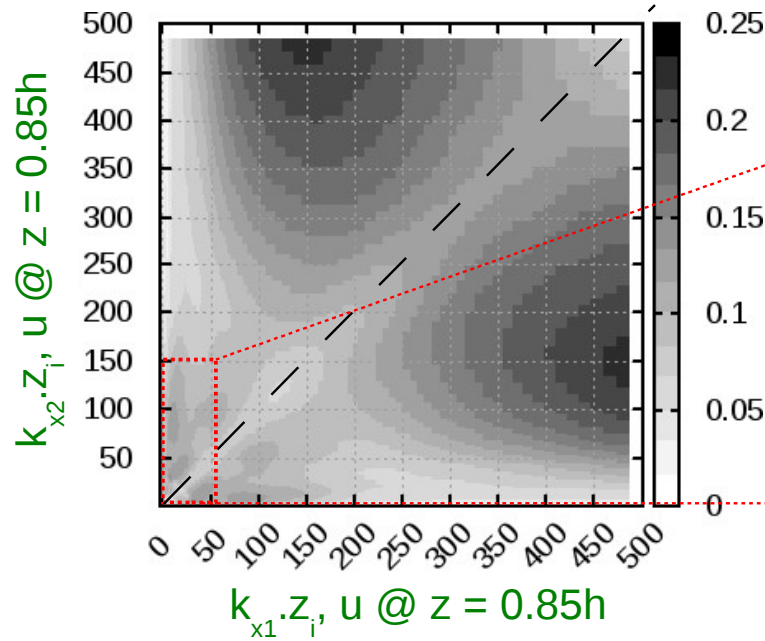
Auto-Bicoherence @ $z/h = 0.85$

Longitudinal
velocity U

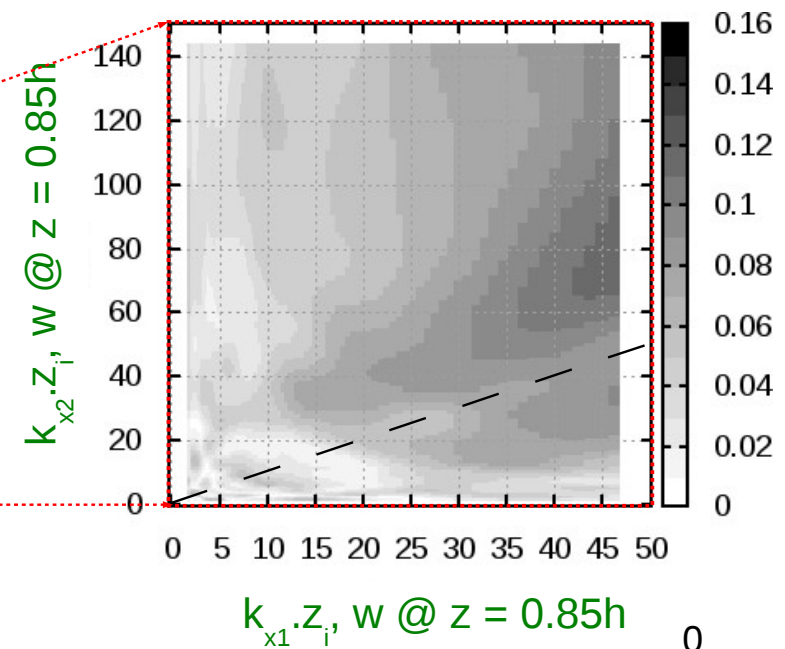
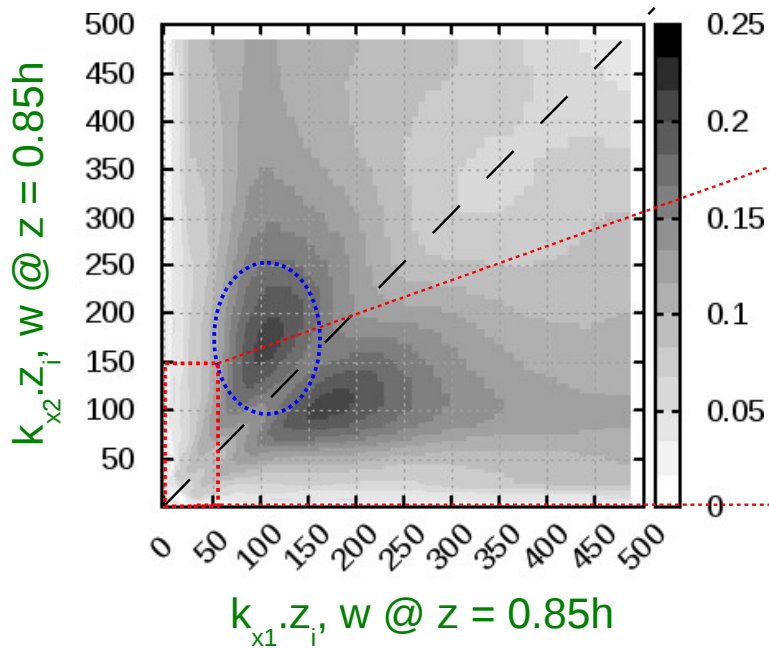


Auto-Bicoherence @ $z/h = 0.85$

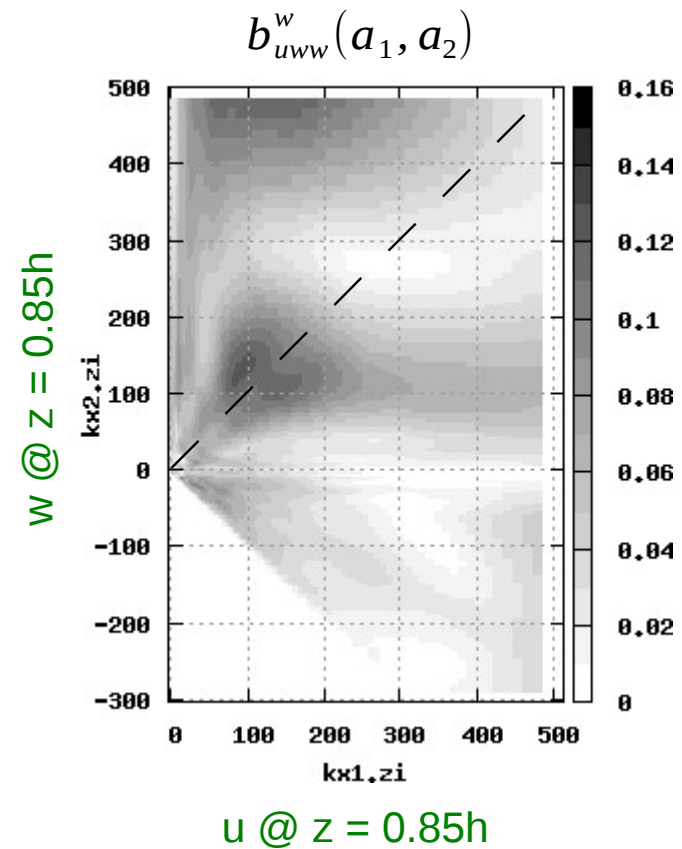
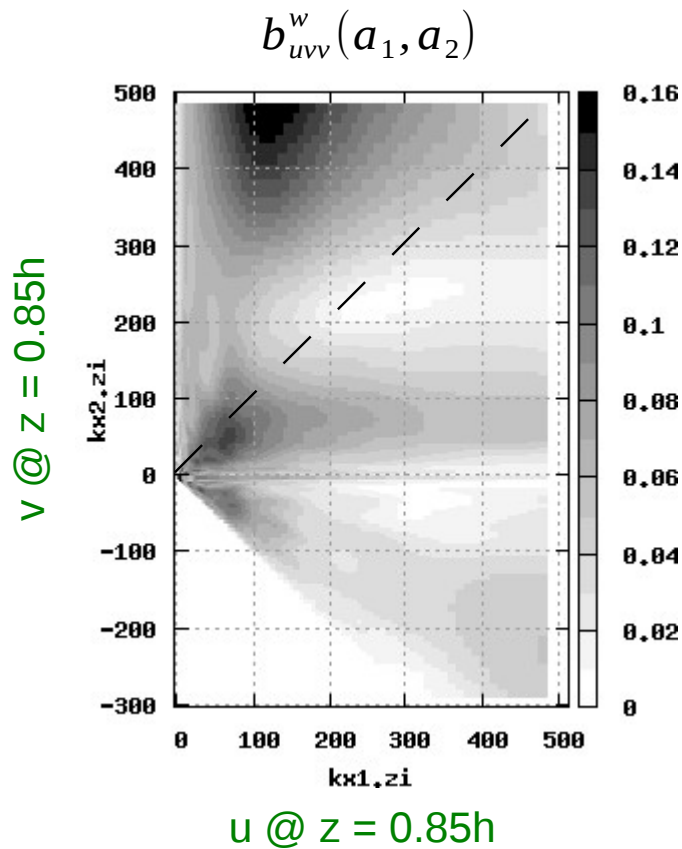
Longitudinal velocity U



Vertical velocity W



One-point cross-Bicoherence @ $z = 0.85h$

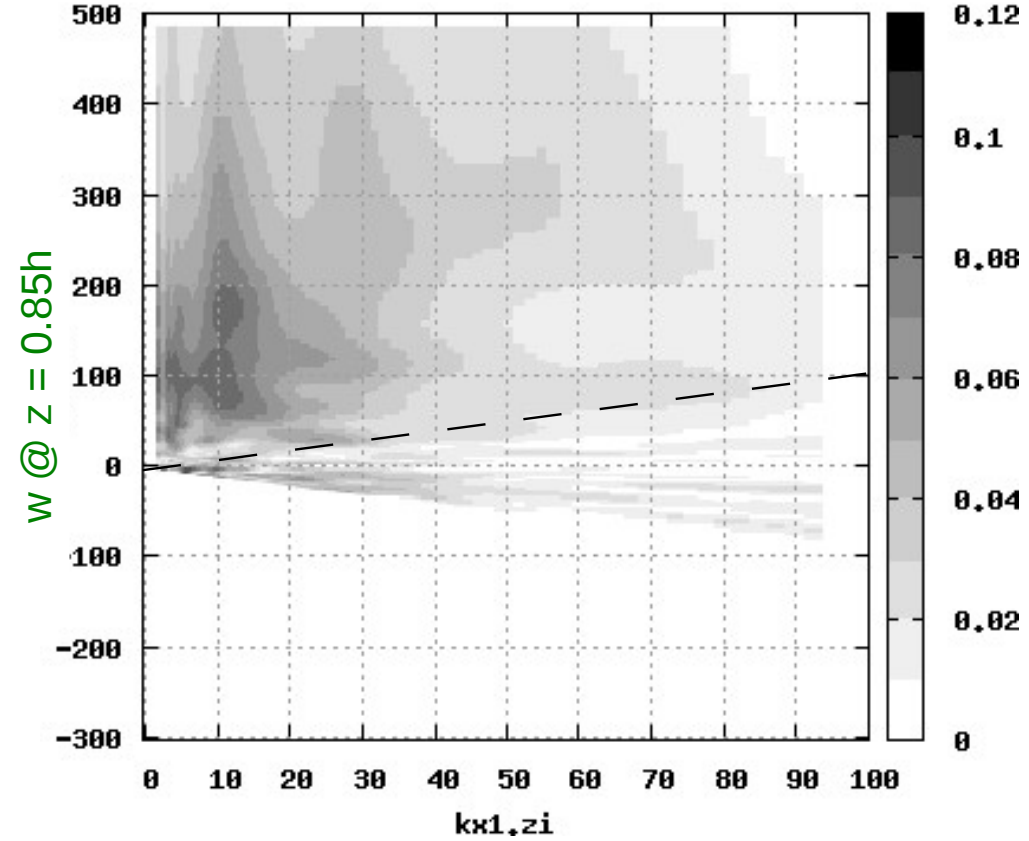
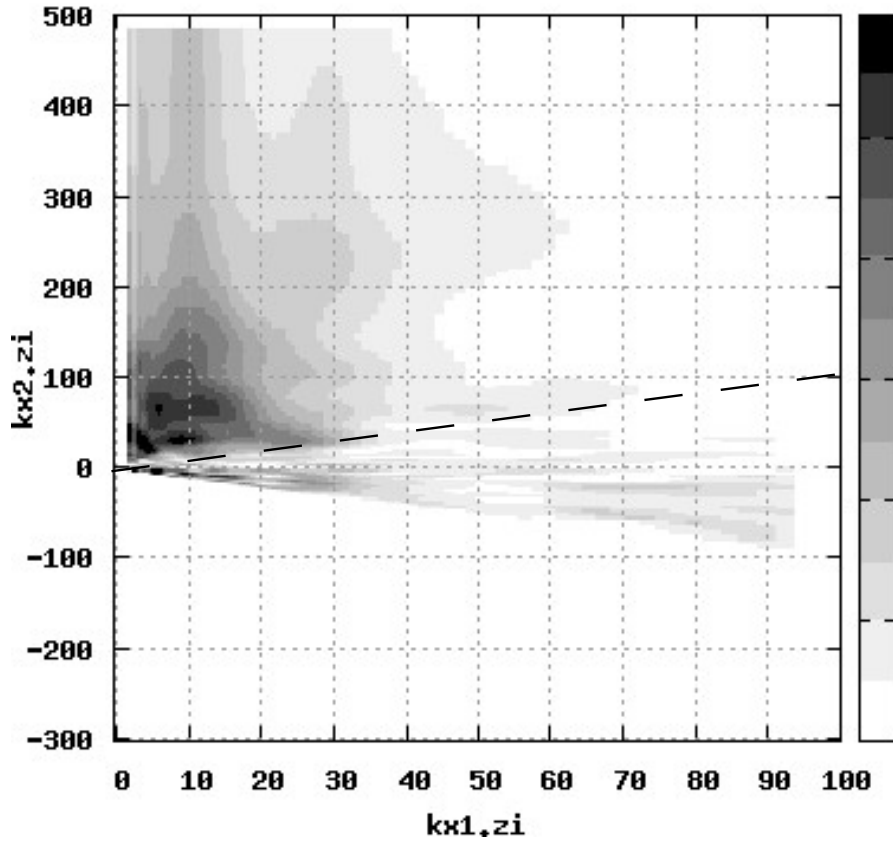


- For the 3 components: non-linear interactions among smaller-scales
- Non-linear interactions between large- and smaller-scales within u
- Non-linear interactions between canopy-scales within w
- Non-linear interactions between large-scales of u and smaller-scales of w

Two-point Cross-Bicoherence: $u @ z = 3h$

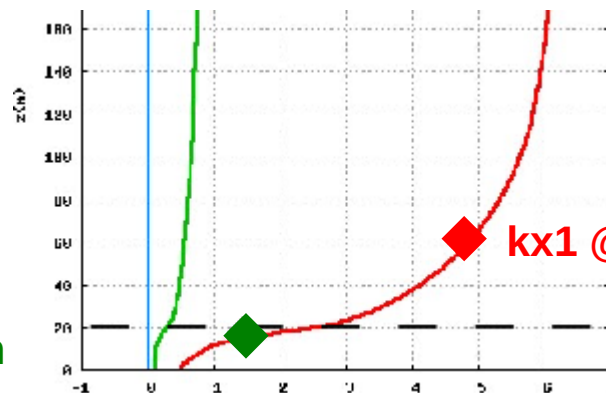
with $u @ z = 0.85h$

with $w @ z = 0.85h$



$u @ z = 3h$

$u @ z = 3h$



$kx2 \ \& \ kx3$
 $@ \ z = 0.85h$

Conclusions and perspectives

Conclusion from the bispectral analysis:

- Non-linear interactions among all scales;
- w bears the footprint of canopy-scale interaction;
- Non-linear interactions between larger-scales of u and smaller-scales of the 3 components;
- Coupling associated to modes of large vertical extent.

Future plans:

- Diagnostic tool for non-linear interaction detection;
- Influence of the stability condition on the non-linear interactions;
- Quantitative estimation of non-linear coupling and energy transfer and modeling;
- Extension to experimental data from the CHATS campaign



Thank you for your attention