

Research Overview

- Goal is to understand the sill-controlled circulation in an idealized ice shelf cavity.
- Posed as a 2-layer lock-exchange problem with boundary interface height forcing.
- We explore the dynamics using analytical uniform PV theory and a numerical model.

Pine Island Glacier

- Topographic sill under Pine Island Glacier modulates inflow of warm Circumpolar Deep Water (CDW) into the shelf cavity (Ref. 1,2,3).
- Warm, salty water in bottom layer flows over sill and is transformed into cold, fresh water as it comes into contact with ice shelf and exits in top layer (Ref. 1,2,3).
- Pine Island Glacier (PIG) is one of the most rapidly retreating glaciers due to warm CDW modulated by topography.



Figure 1: Pine Island Glacier location and geometry. Credit: Rignot et al. 2002 (Ref. 1) and NASA (Ref. 4).

Cavity Parameters

Cavity Size= 50km x 100km x 700m (W x L x H) Sill Height = 400m $\rho = 1027.47$ to 1027.75 kg/m³ $f = -1.41 \cdot 10^{-4} s^{-1}$ Flow rate $\sim 300 \text{ mSv}$ Internal Baroclinic Def. Radius= 5km

Sill-Controlled Circulation in Ice Shelf Cavities

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Uniform PV theory

Semigeostrophic approx. (L >> W) for two layers h_1, h_2 above bottom topography *B*: $fv_i = \frac{\partial p_i}{\partial x}$ $Q_i = \frac{f}{H_i} = \frac{f + \frac{\partial v_i}{\partial x}}{h_i}$ **3** Solutions: $h_i(x) = A_i e^{k_d x} + B_i e^{-k_d x} + C_i$ $u_i(x) = D_i e^{k_d x} + E_i e^{-k_d x} + F_i x + G_i$

Important Result

In the wide channel limit ($L_d << W$), uniform PV is only a reasonable assumption within the lateral boundary layers. An imposed upstream-downstream PV difference necessarily forms a PV gradient in the domain. This carries cross-sill flow via mean or eddy advection and is strongly influenced by sill height.

About the Model

- Back of the Envelope Ocean Model (BEOM) is a numerical shallow water isopycnal model (see ref. 5).
- Simulates rotating basins with a free surface/rigid lid, wetting/drying, and hydrostatic layered stratification.
- Setup includes 2 layers with bottom topography, a rigid lid and upstream/downstream buoyancy forcing.



Figure 2: Example of model setup geometry.

Theoretical Predictions/Limitations

- Uniform PV predicts boundary layer structure that depends on the flow rate.
- For wide channels, theory predicts boundary current separation.
- Numerical solutions show uniform PV does not provide a complete picture i.e. flow has PV gradients instead of boundary layer separation.

Numerical Results



Figure 4: Same as fig. 3 for top layer PV.





 Presence of a sill weakens overall circulation strength and increases baroclinicity. Results show lateral boundary eddies contribute significantly to total transport in low drag regime.

Figure 5: Flow rate vs. drag and sill height.

Summary and Future Work

• A rich range of behavior is observed in 2-layer exchange flows depending on **cavity shape** and **drag**.

 Circulation strength is strongly sill-controlled, but rather insensitive to drag.

• Future work will explore these dynamics in hydraulically-controlled and layer-outcropping regimes.

References

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