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# Evolution of Hurricane-like Eyewall Structures Using a Divergent, Normal-Mode, Spectral Model

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## The Model

Model based on shallow water equations in rotational form:

$$\begin{aligned} \frac{\partial u}{\partial t} - (f + \zeta)v + \frac{\partial}{\partial x} \left[ \phi + \frac{1}{2}(u^2 + v^2) \right] &= \mu \nabla^2 u \\ \frac{\partial v}{\partial t} + (f + \zeta)u + \frac{\partial}{\partial y} \left[ \phi + \frac{1}{2}(u^2 + v^2) \right] &= \mu \nabla^2 v \\ \frac{\partial \phi}{\partial t} + c^2 \left( \frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} \right) + \frac{\partial(u\phi)}{\partial x} + \frac{\partial(v\phi)}{\partial y} &= \mu \nabla^2 \phi \end{aligned}$$

## Solution Technique:

- Equations solved using the normal mode method presented in Guinn and Schubert (1993)
- Method allows easy partitioning of rotational and gravity-inertia modes

## Model Details

- 600km x 600km doubly periodic domain
- 512 x 512 collocation points (170 modes)
- Ordinary diffusion with e-folding damping time of 60min for modes w/total wave number 170
- Undisturbed fluid depth of 2,000m giving  $c \approx 140\text{ms}^{-1}$
- $f = 5 \times 10^{-5}\text{s}^{-1}$ , or  $\sim 20^\circ\text{N}$

## Objective

Replicate classic non-divergent model hurricane-like eyewall simulations using a divergent (shallow-water), normal-mode model then partition linear terms into rotational and gravity-inertia modes to quantify the relative contribution of each.

## Cases

Case 1: Ivan-like eyewall (Henricks et al, 2010)

Case 2: Annulus (Schubert et all, 1999)

Case 3: Kirchoff Vortex

## References:

- Guinn, T.A., and W.H. Schubert, 1993: Hurricane spiral bands. *J. Atmos. Sci.*, **50**, 3380-3403.  
 Schubert, W.H., M.T. Montgomery, R.K. Taft, T.A. Guinn, S.R. Fulton, J.P. Kossin, and J.P. Edwards, 1999: Polygonal eyewalls, asymmetric eye contraction, and potential vorticity mixing in hurricanes. *J. Atmos. Sci.*, **56**, 1197-1223.  
 Hendricks, E.A., W.H. Schubert, S.R. Fulton, and B.D. McNoldy, 2010: Spontaneous-adjustment emission of inertia-gravity waves by unsteady vertical motion in the hurricane core. *Quart. J. Roy. Meteor. Soc.*, **136**, 537-548.

