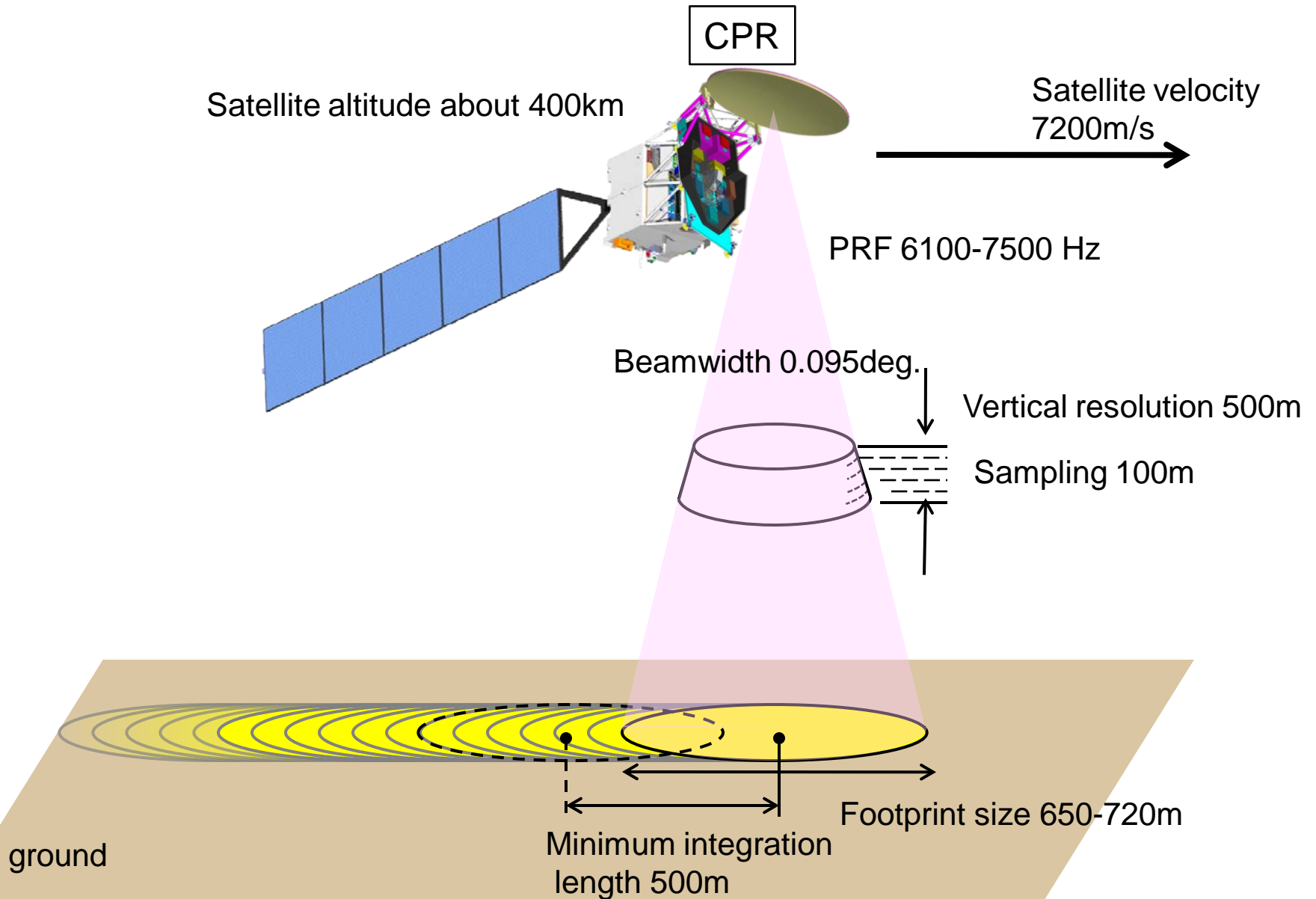


# **Doppler correction algorithm for EarthCAER Cloud Profiling Radar**

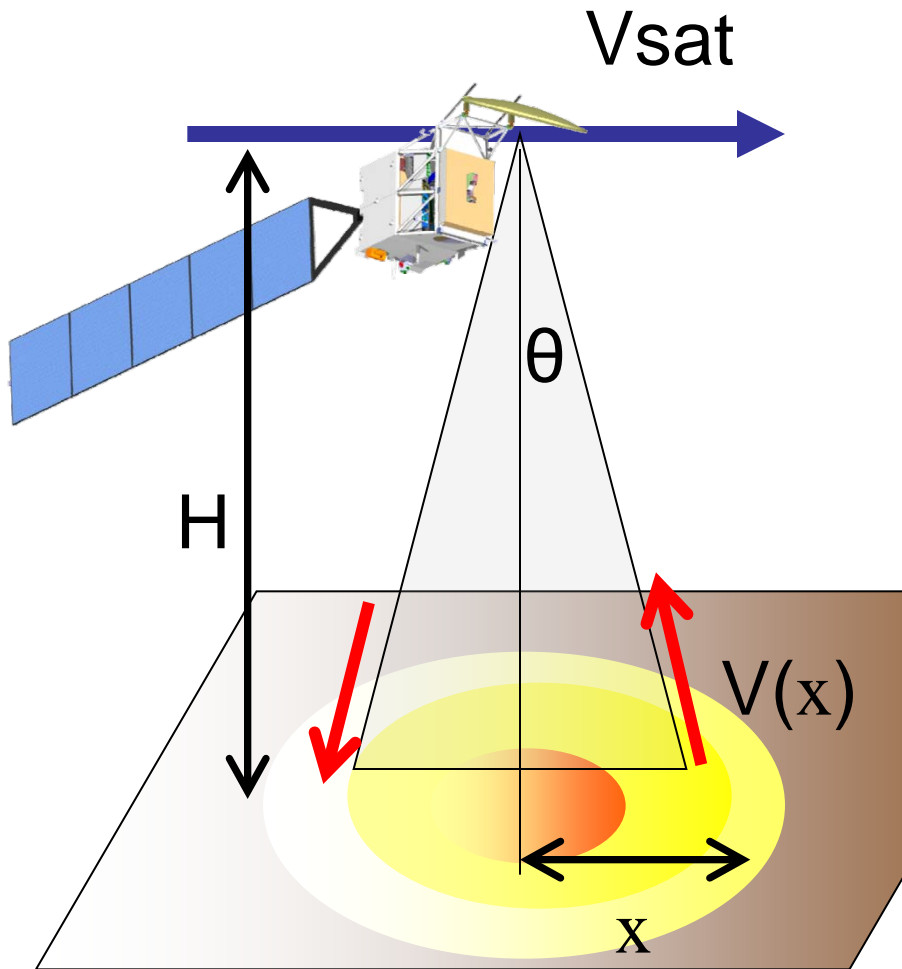
Y. Ohno, H. Horie, K. Sato, N. Takahashi,  
National Institute of Information and Communications  
Technology

36th Conference on Radar Meteorology  
17 Sep 2013

# Schematic view of EarthCARE CPR observation



# Doppler velocity error with non-uniform reflectivity



$\theta$ : angle from nadir

$$V(x) = V_{sat} \cdot \sin\theta = V_{sat} \cdot x/H$$

Ex.  $\theta = \text{beamwidth}/2$

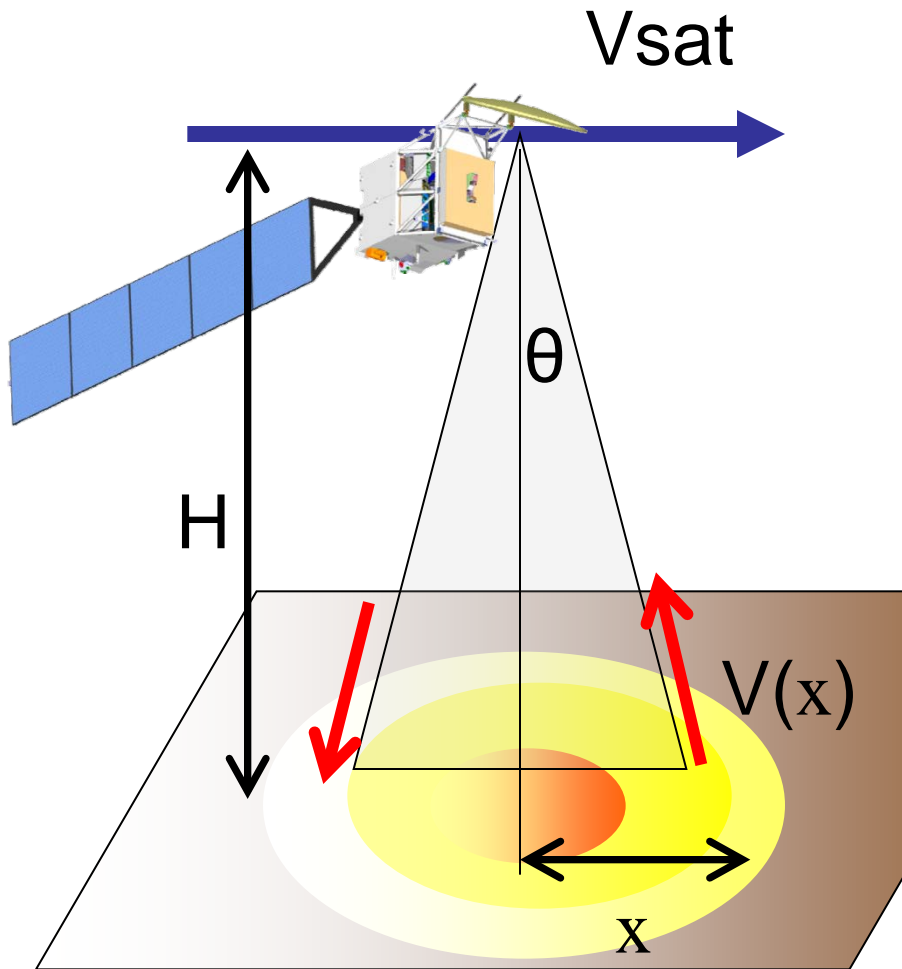
$$V_{bw} = V_{sat} \cdot \sin(\text{beamwidth}/2) = 5.97 \text{ m/s}$$

Doppler measured by CPR is reflectivity weighted velocity i.e.

$$V_{CPR} = \frac{\int (V(x) + w(x)) \cdot f(x) z(x) dx}{\int f(x) z(x) dx}$$

$z(x)$ : reflectivity  $w(x)$ : vertical wind  
 $f(x)$ : beam pattern

# Doppler velocity error with non-uniform reflectivity



**If non-uniform reflectivity**

$$V_{CPR} \neq \int w(x) (z(x) / \bar{z}) dx$$

$$V_{error} = V_{CPR} - \int w(x) (z(x) / \bar{z}) dx$$

**Doppler measured by CPR is reflectivity weighted velocity i.e.**

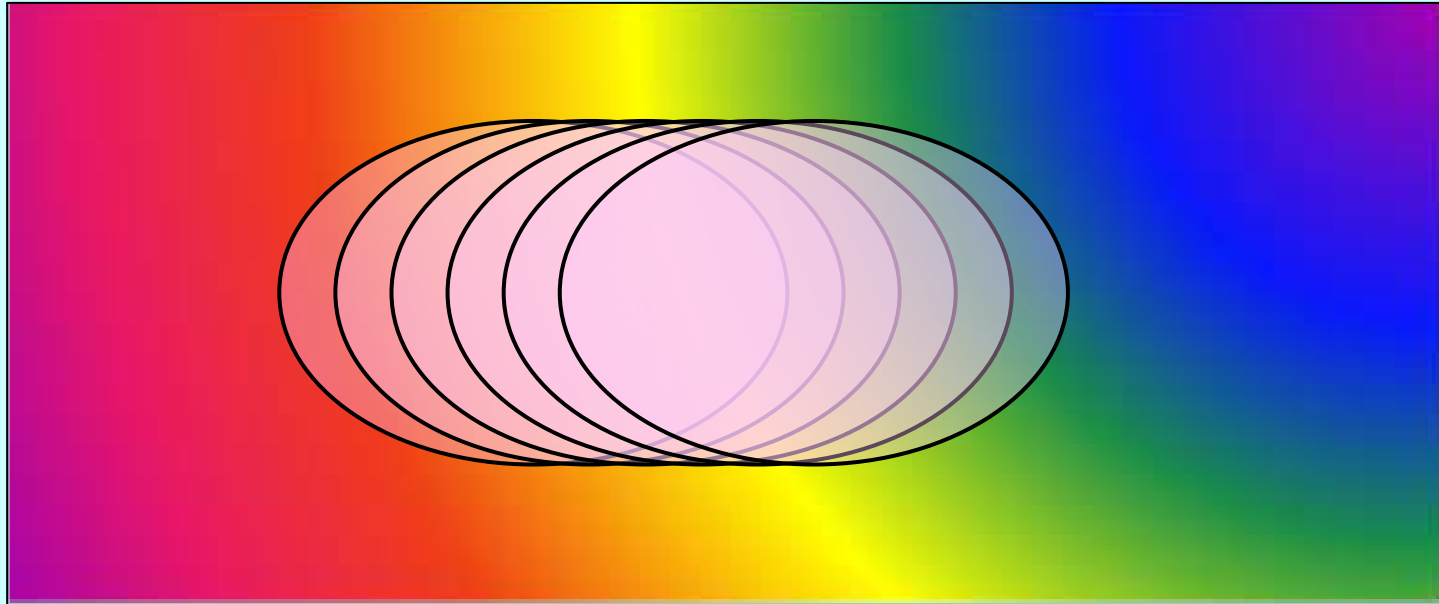
$$V_{CPR} = \frac{\int (V(x) + w(x)) \cdot f(x) z(x) dx}{\int f(x) z(x) dx}$$

**$z(x)$ : reflectivity  $w(x)$ : vertical wind  
 $f(x)$ : beam pattern**

# Topics

- 1. Reflectivity distribution & Doppler error after horizontal integration**
- 2. Doppler folding consideration**
- 3. Simulation of Doppler error using reflectivity data**

# 1. Reflectivity distribution & Doppler error after horizontal integration



# Doppler error formula after horizontal integration

$V_{error}(x_n)$ : one pulse Doppler error

$x_n$ : beam center location at n th pulse

$$V_{error}(x_n) = \frac{\int v(x - x_n) f(x - x_n) z(x) dx}{\int f(x - x_n) z(x) dx}$$

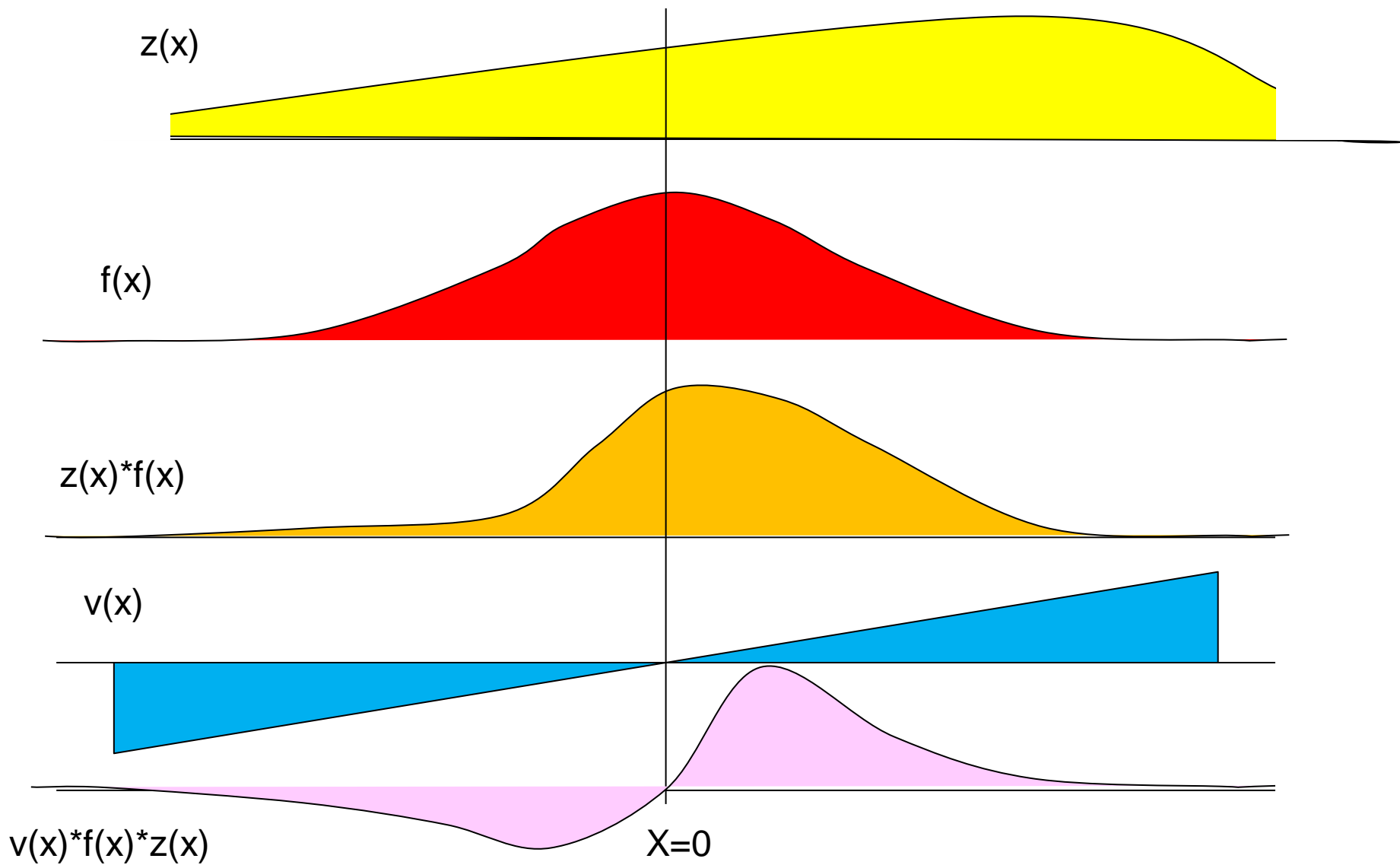
$\overline{V}_{error}(x_{00})$ : Pulse-integrated Doppler error

$x_{00}$ : Center of integration

$$\begin{aligned} \overline{V}_{error}(x_{00}) &= \frac{\sum_{-N/2}^{N/2} V(x_n) Z(x_n)}{\sum_{-N/2}^{N/2} Z(x_n)} \quad Z(x_n) = \int f(x - x_n) z(x) dx \\ &= \frac{\sum_{-N/2}^{N/2} \int v(x - x_n) f(x - x_n) z(x) dx}{\sum_{-N/2}^{N/2} Z(x_n)} \end{aligned}$$

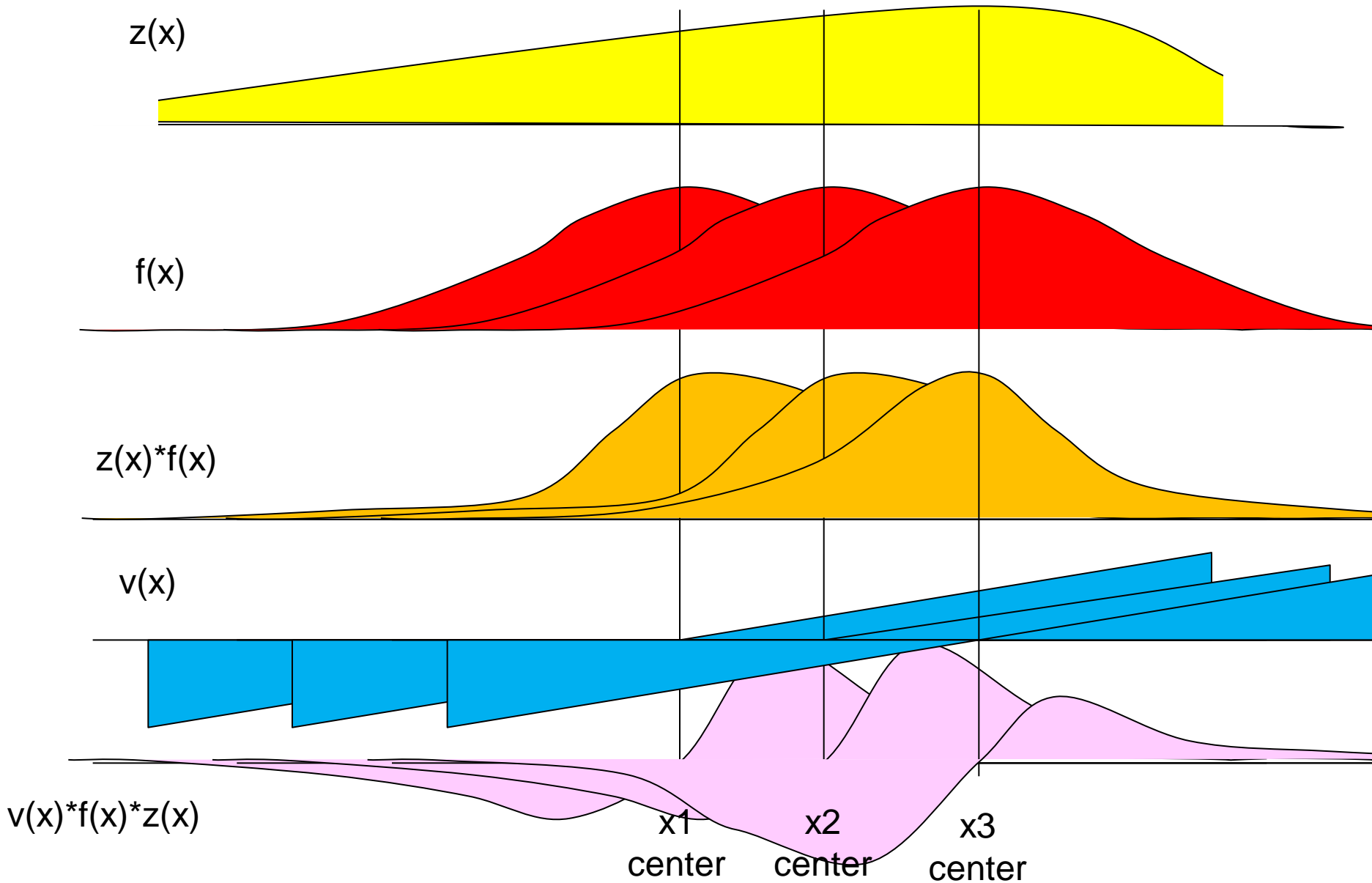
N: Pulse number with horizontal integration

# Doppler error integration within footprint





# Horizontal integration with satellite moving



# Doppler error formula after horizontal integration

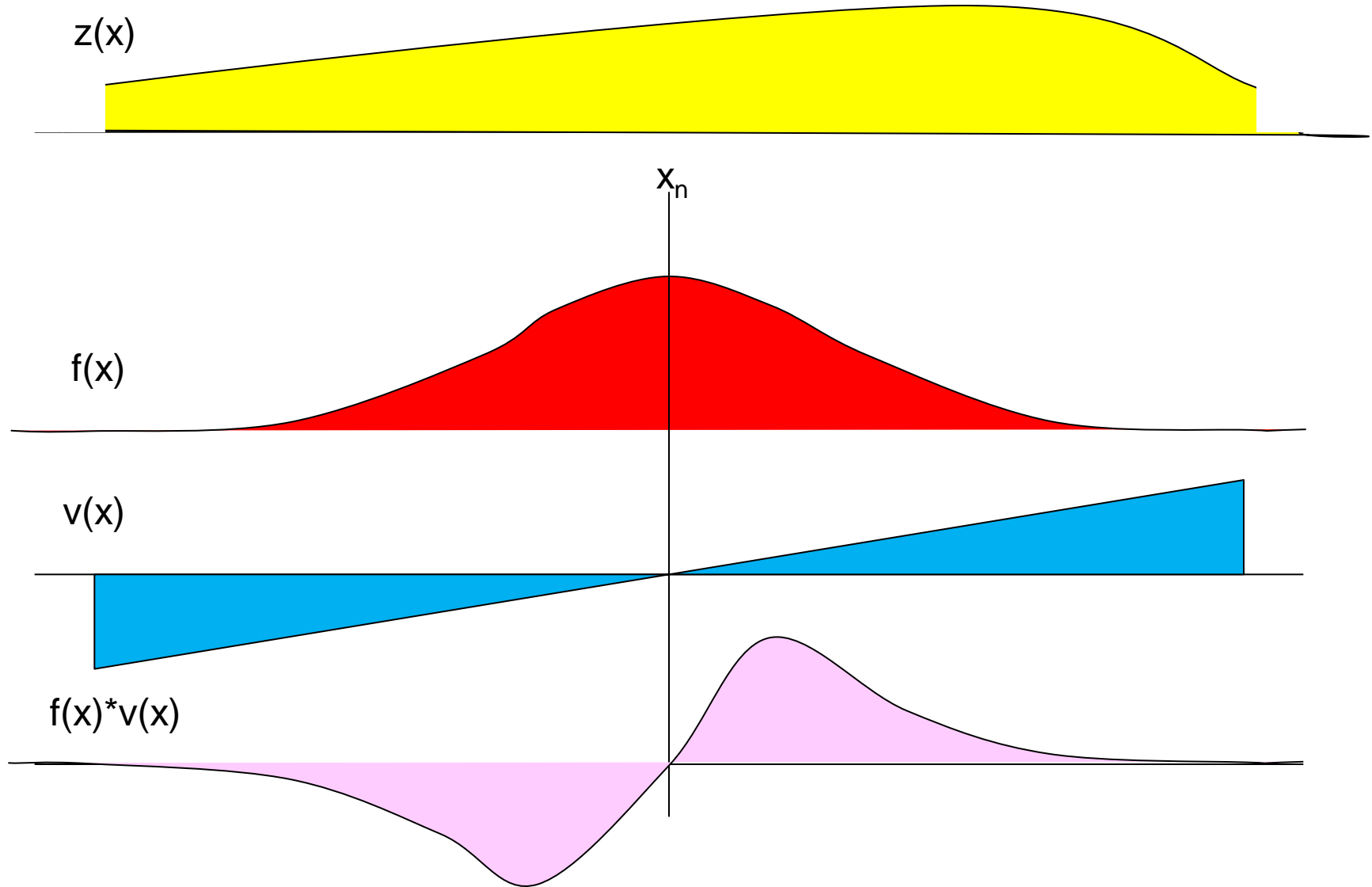
$V_{error}(x_n)$ : one pulse Doppler error

$$V_{error}(x_n) = \frac{\int v(x - x_n) f(x - x_n) z(x) dx}{\int f(x - x_n) z(x) dx}$$

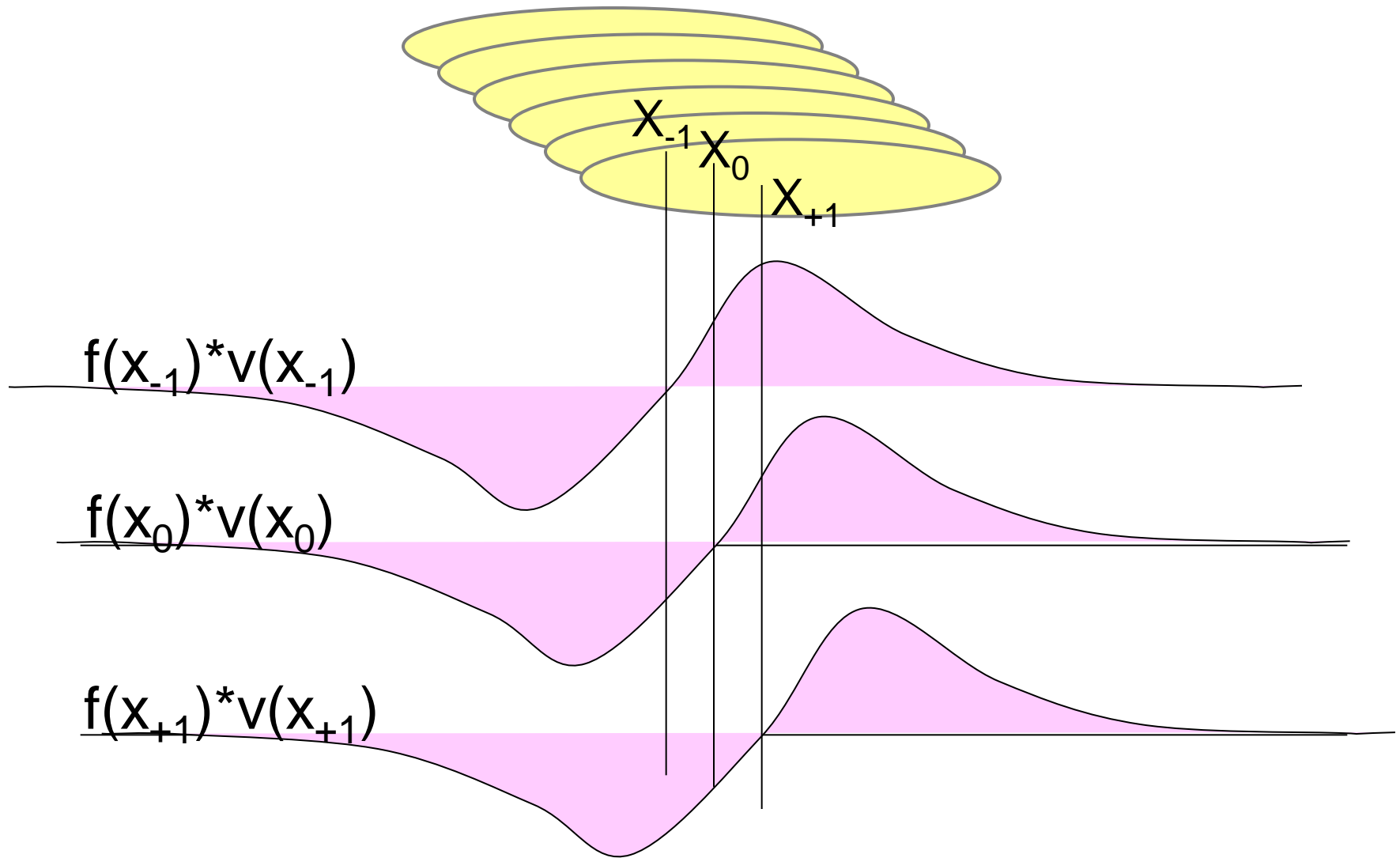
$\overline{V}_{error}(x_{00})$ : Pulse-integrated Doppler error

$$\begin{aligned} \overline{V}_{error}(x_{00}) &= \frac{\sum_{-N/2}^{N/2} V(x_n) Z(x_n)}{\sum_{-N/2}^{N/2} Z(x_n)} & Z(x_n) &= \int f(x - x_n) z(x) dx \\ &= \frac{\sum_{-N/2}^{N/2} \int v(x - x_n) f(x - x_n) z(x) dx}{\sum_{-N/2}^{N/2} Z(x_n)} \end{aligned}$$

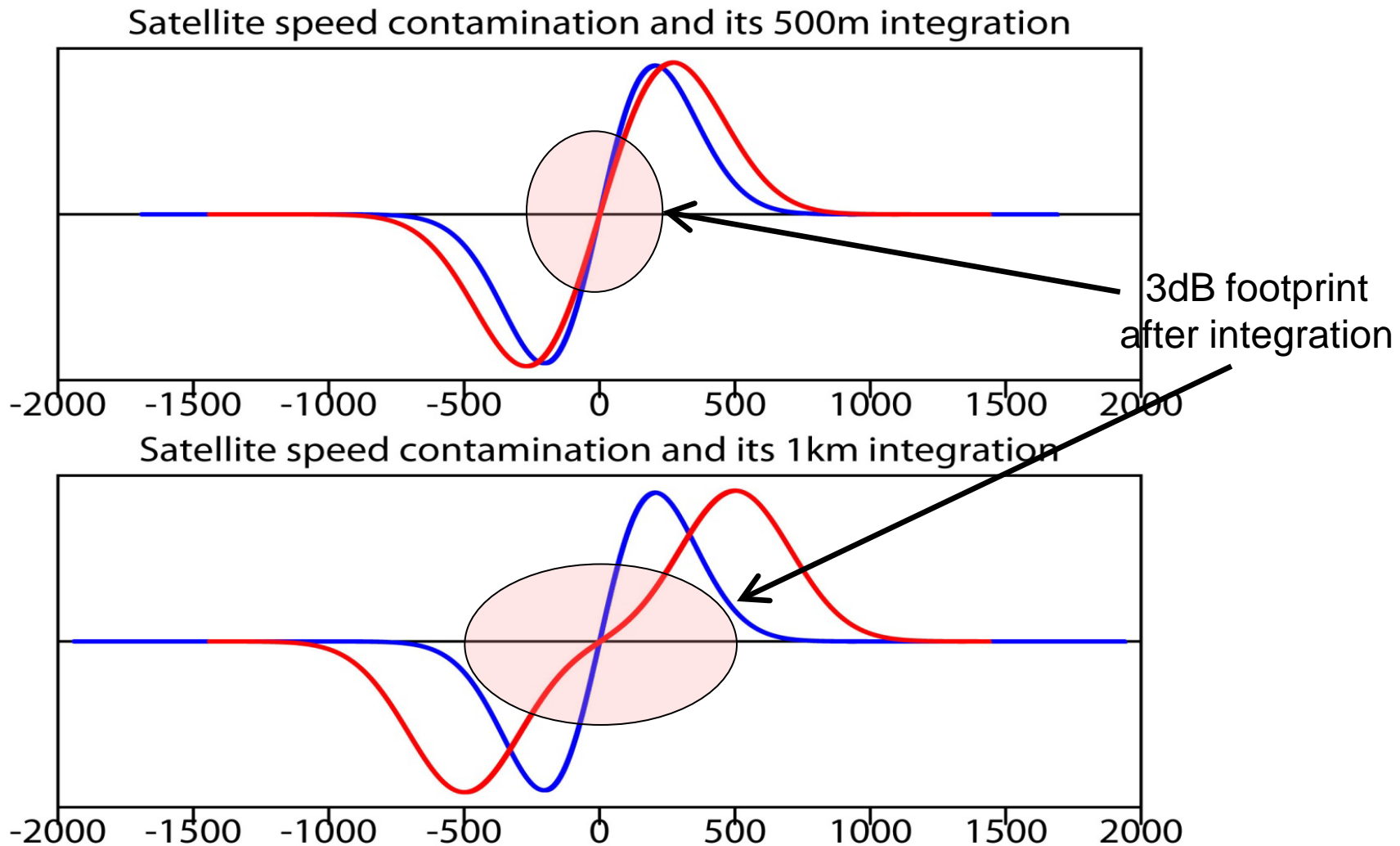
# Change order of multiplication for Doppler error



# $f(x) * v(x)$ pattern shift with satellite moving



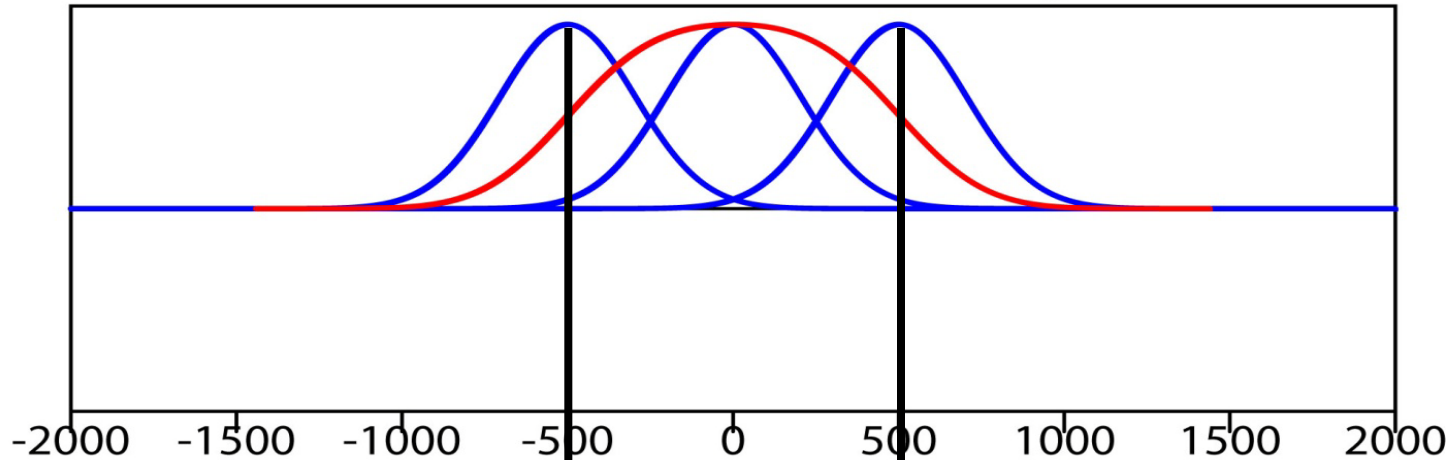
# $f(x) * v(x)$ pattern after 500m & 1km integration



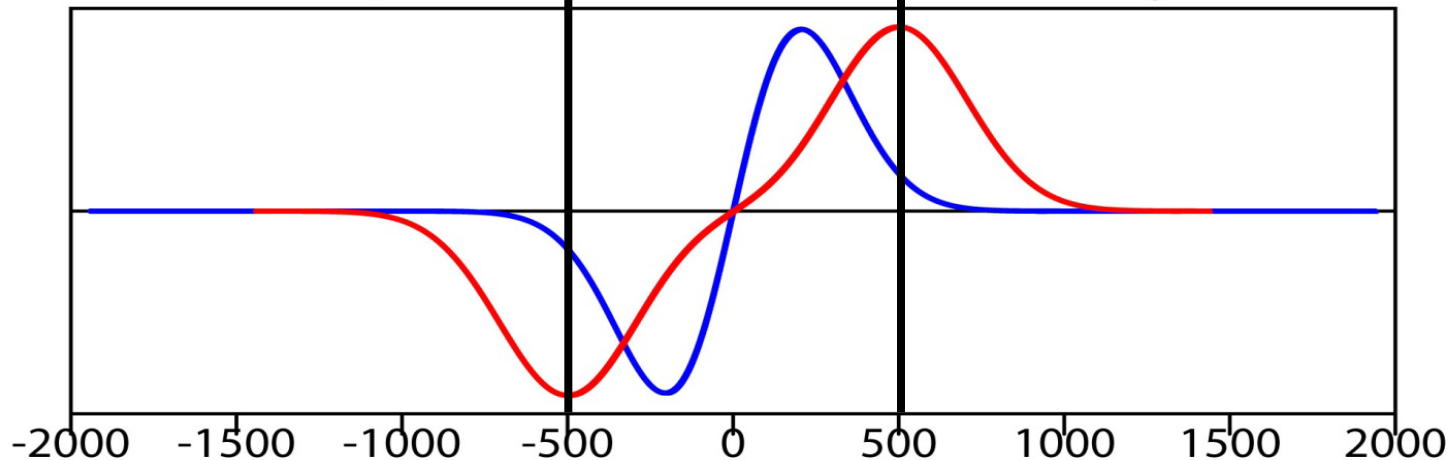
Red line:  $f(x) * v(x)$  after horizontal integration

# $f(x)$ & $f(x)*v(x)$ pattern after 1km integration

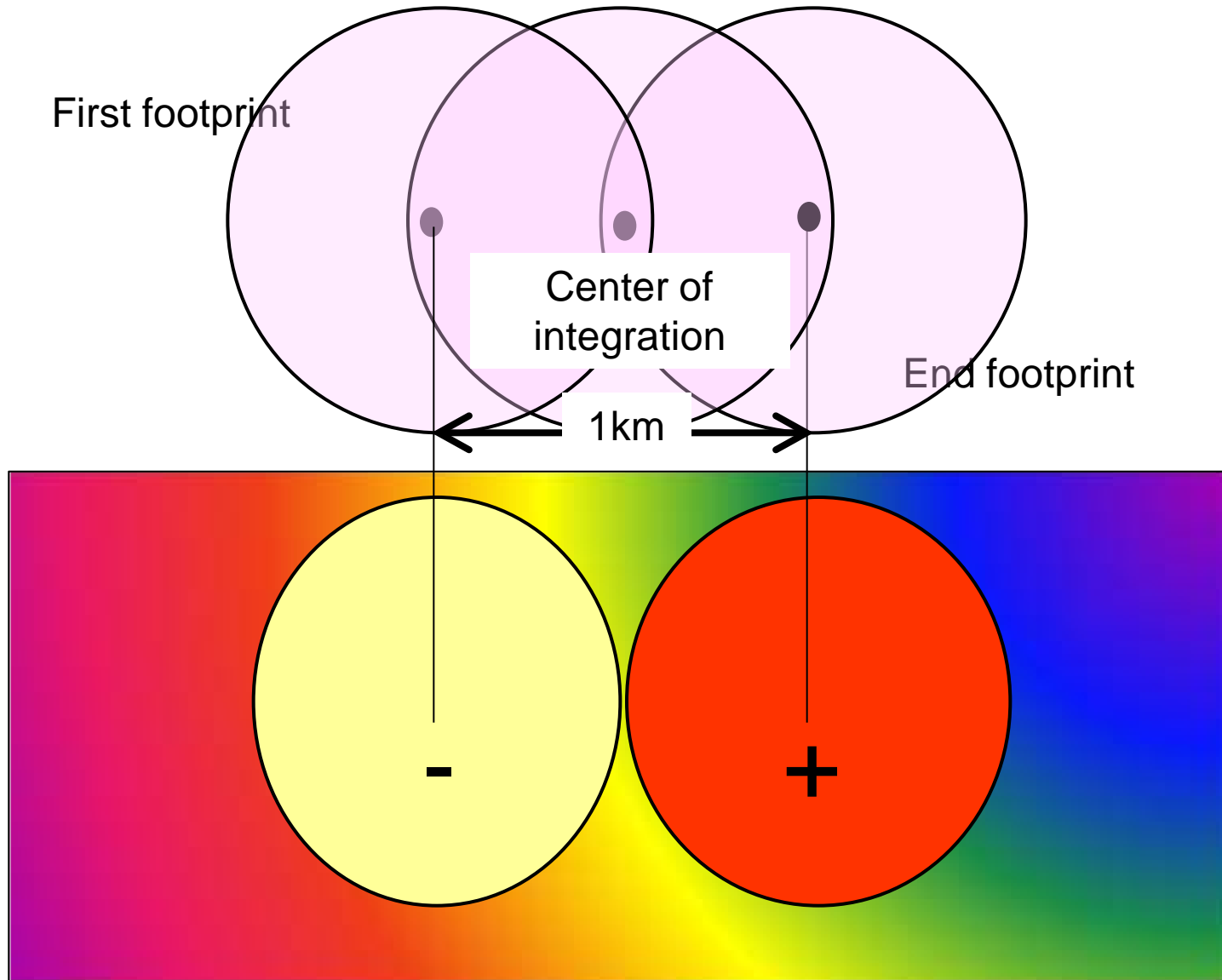
Gauss beam pattern and its 1km integration



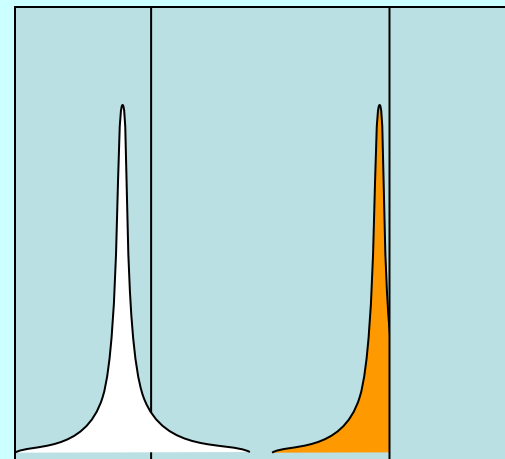
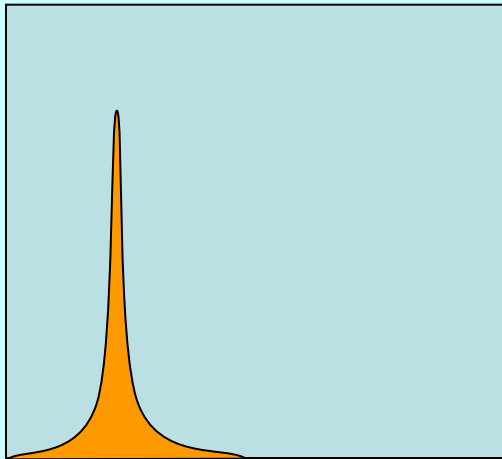
Satellite speed contamination and its 1km integration



# Footprint & $f(x)*v(x)$ pattern in horizontal view



## 2. Doppler folding consideration





## Doppler folding

$$V_{\max} = \frac{\lambda \cdot PRF}{4}$$

PRF: Pulse Repetition Frequency  
 $V_{\max}$ : Maximum velocity folding

$$V_{\max} = V_{sat} * x_{fold} / H$$

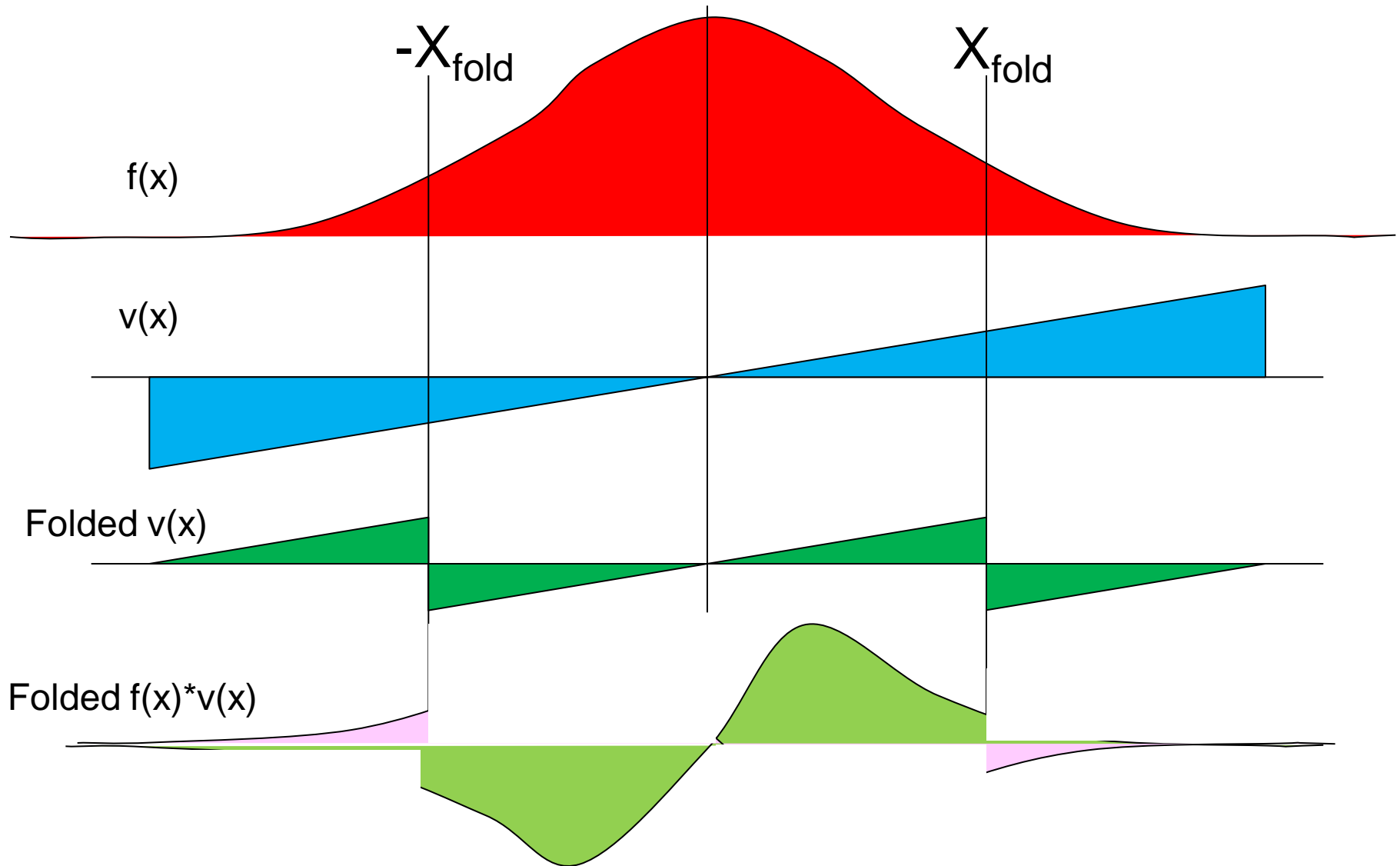
$$x_{fold} = \frac{\lambda \cdot PRF}{4} \bullet \frac{H}{V_{sat}}$$

$$= 332.3m(PRFF7500Hz)$$

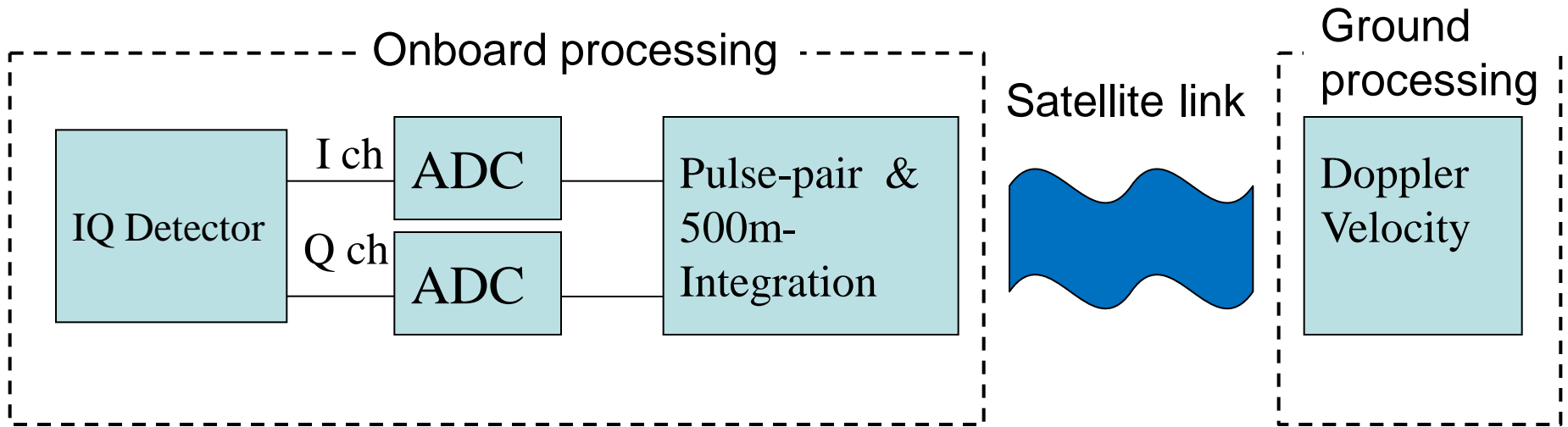
$$= 270.2m(PRFF6100Hz)$$

$x_{fold}$ : Doppler folding position from center

# Change order of multiplication for Doppler error



# Doppler processing using Pulse-pair (1)



$$w_k = I_k + iQ_k$$

$I_k$ : I ch time series

$Q_k$ : Q ch time series

k: pulse number

T: pulse interval

$$R(T) = \overline{w_k^* \cdot w_{k+1}}$$

$$= \text{Re } R(T) + i \text{Im } R(T)$$

$$\text{Re } R(T) = \sum (I_k I_{k+1} + Q_k Q_{k+1})$$

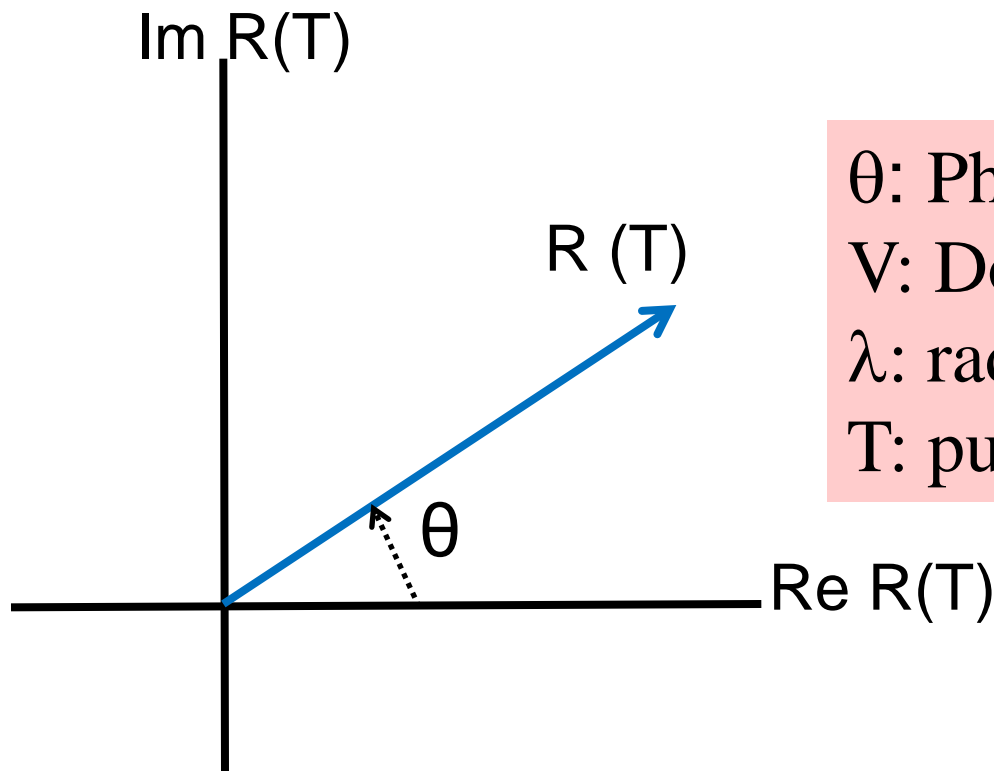
$$\text{Im } R(T) = \sum (Q_k I_{k+1} - I_k Q_{k+1})$$

R(T): Complex cross correlation PP

## Doppler processing using Pulse-pair (2)

$$\theta = 2\pi \frac{2TV}{\lambda}$$

$$V = \frac{\lambda}{4\pi T} \tan^{-1} \left( \frac{\text{Im } R(T)}{\text{Re } R(T)} \right)$$



$\theta$ : Phase change between pulses

$V$ : Doppler velocity

$\lambda$ : radio wave length

$T$ : pulse interval

# Formula of Doppler velocity error using PP

$c(x), q(x)$ : Real & imaginary part of  $R(T)$  function at  $x$

$$c(x) = \text{Re } R(T) = \cos(x / x_{\max} \cdot \pi)$$

$$q(x) = \text{Im } R(T) = \sin(x / x_{\max} \cdot \pi)$$

$x_{\max}$ : Doppler folding position  
from beam center

$C(x), Q(x)$ : Real & imaginary part of  $R(T)$  function at  $x_n$

$$C(x_n) = \int c(x - x_n) f(x - x_n) z(x) dx / Z(x_n)$$

$$Q(x_n) = \int q(x - x_n) f(x - x_n) z(x) dx / Z(x_n)$$

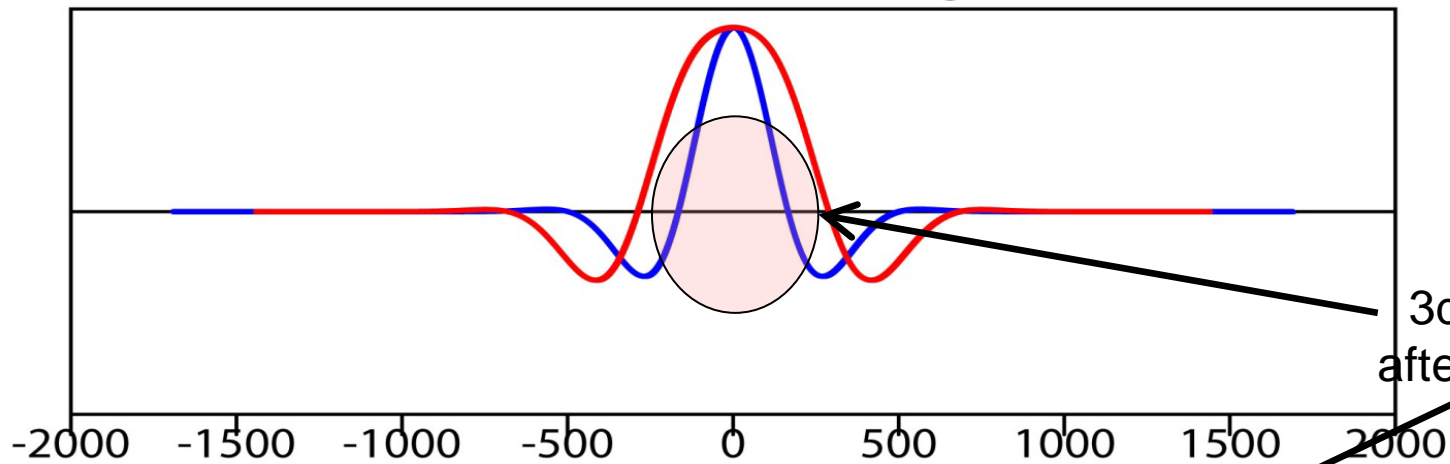
$$Z(x_n) = \int f(x - x_n) z(x) dx$$

$\bar{V}(x_{00})$ : Pulse-integrated Doppler error

$$\overline{V}_{error}(x_{00}) = \frac{\lambda \cdot PRF}{4\pi} \arctan\left( \frac{\sum_{-N/2}^{N/2} Q(x_n) Z(x_n)}{\sum_{-N/2}^{N/2} C(x_n) Z(x_n)} \right)$$

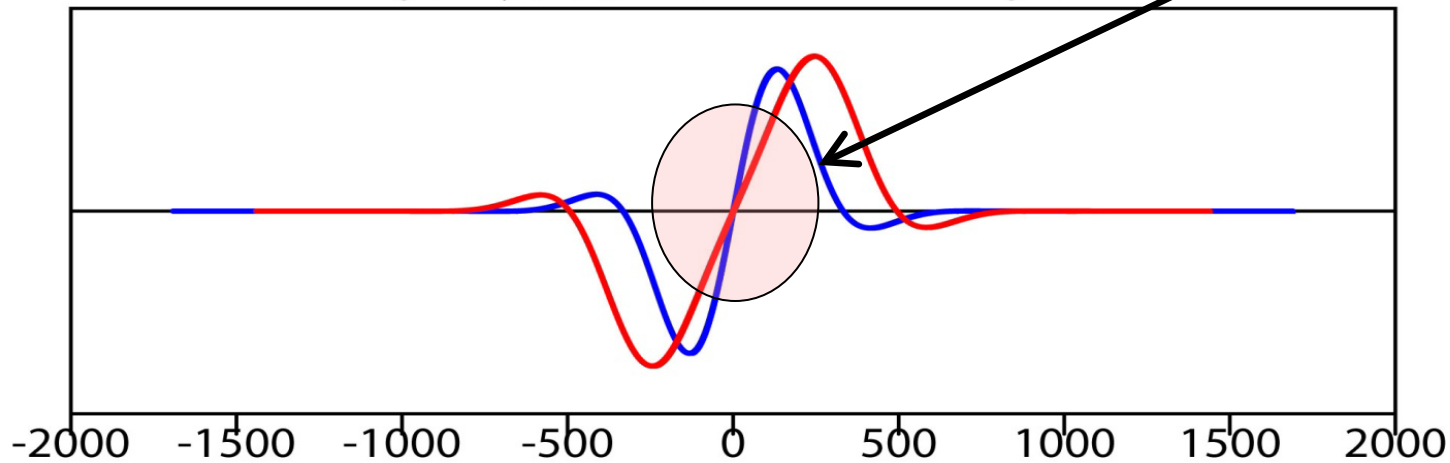
# $f(x) * c(x)$ & $f(x) * q(x)$ pattern with 500m integration

Real{R(t)} and its 500m integration



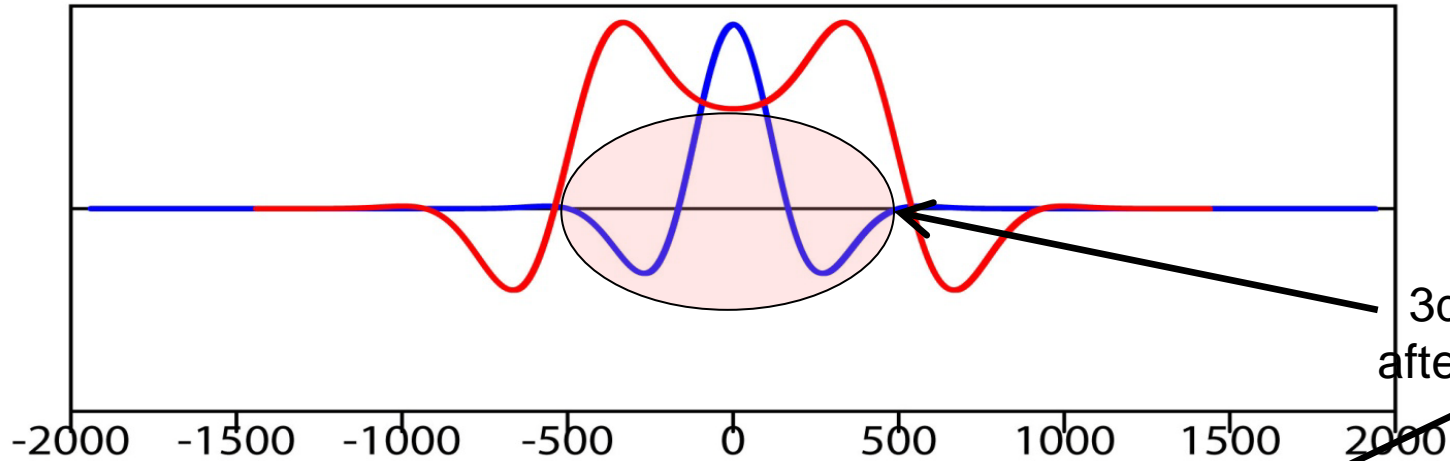
3dB footprint  
after integration

Imaginary{R(t)} and its 500m integration



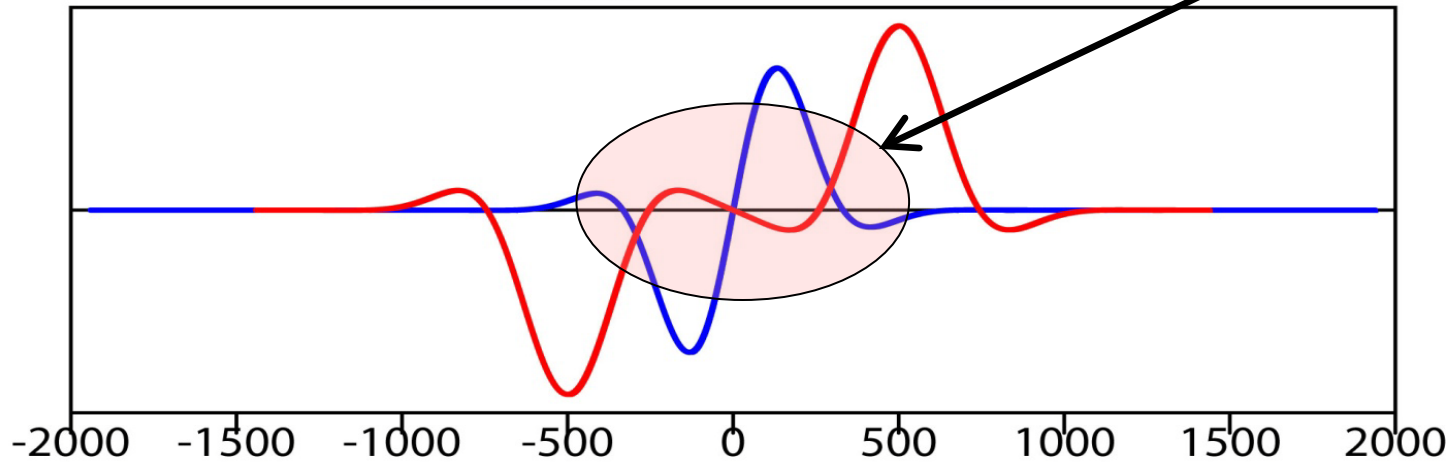
# $f(x) * c(x)$ & $f(x) * q(x)$ pattern with 1km integration

Real $\{R(t)\}$  and its 1km integration

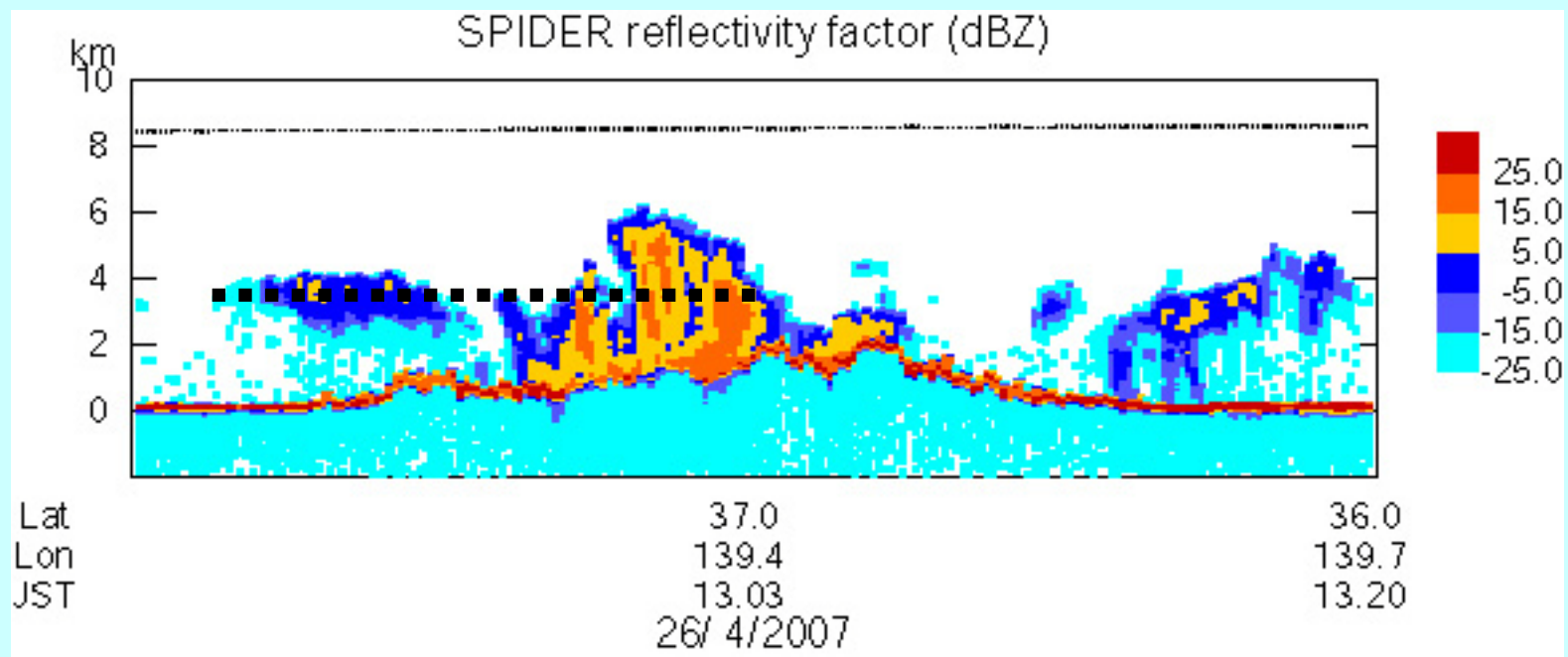


3dB footprint  
after integration

Imaginary $\{R(t)\}$  and its 1km integration



# 3. Simulation of Doppler error using real observation





dBZ

30

20

10

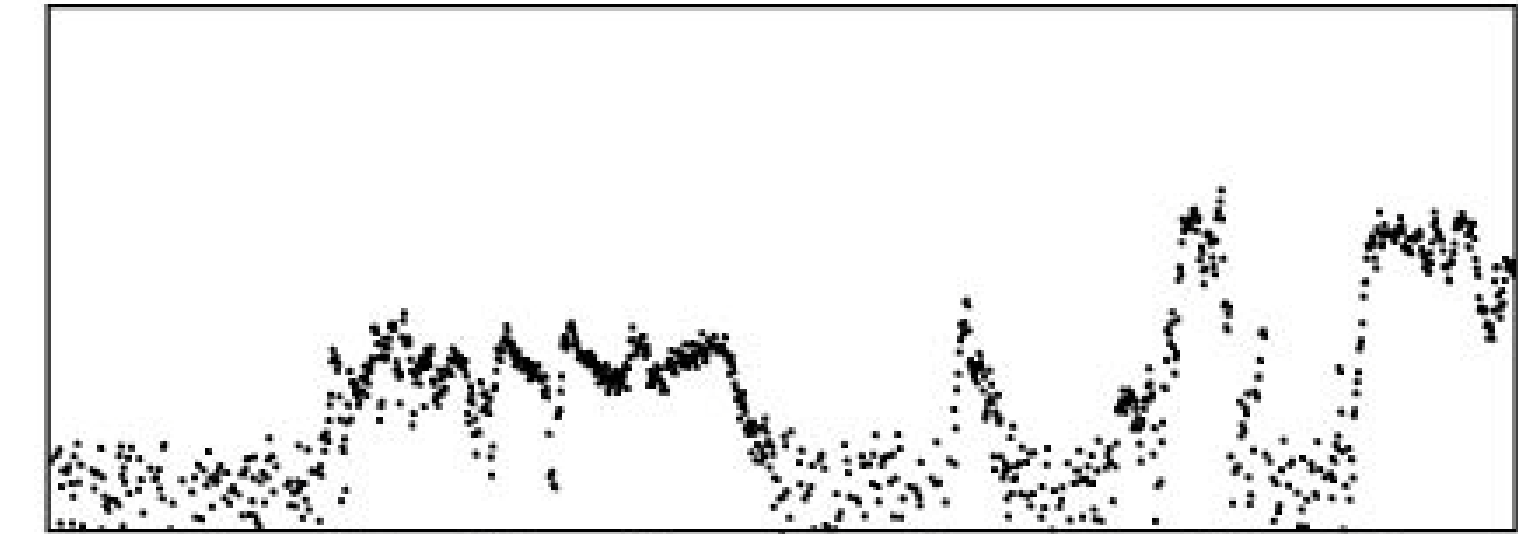
0

-10

-20

-30

km



-50

-40

-30

-20

-10

0

10

20

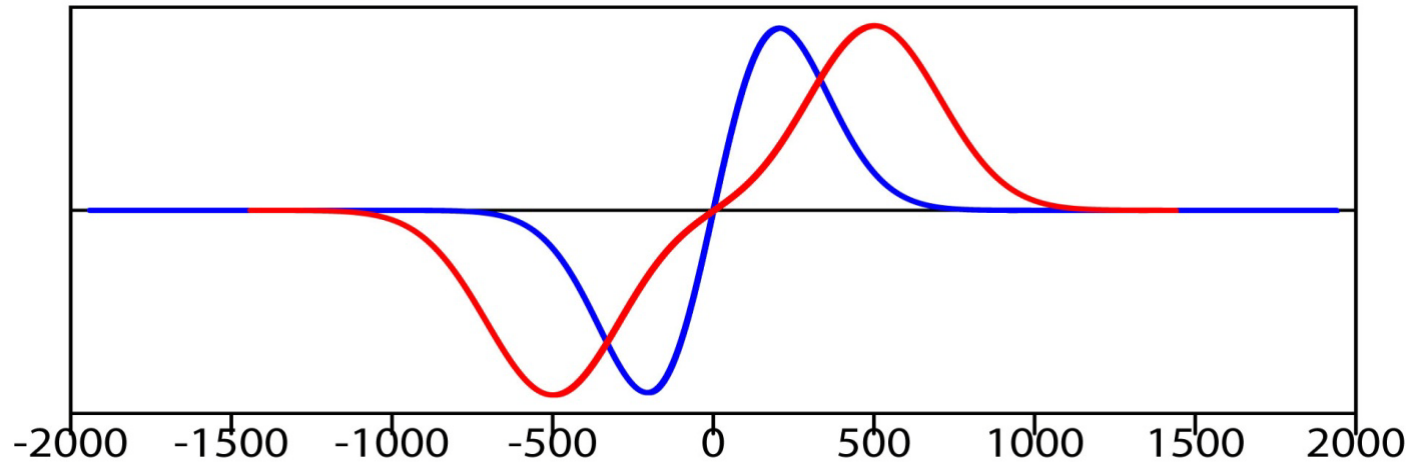
30

40

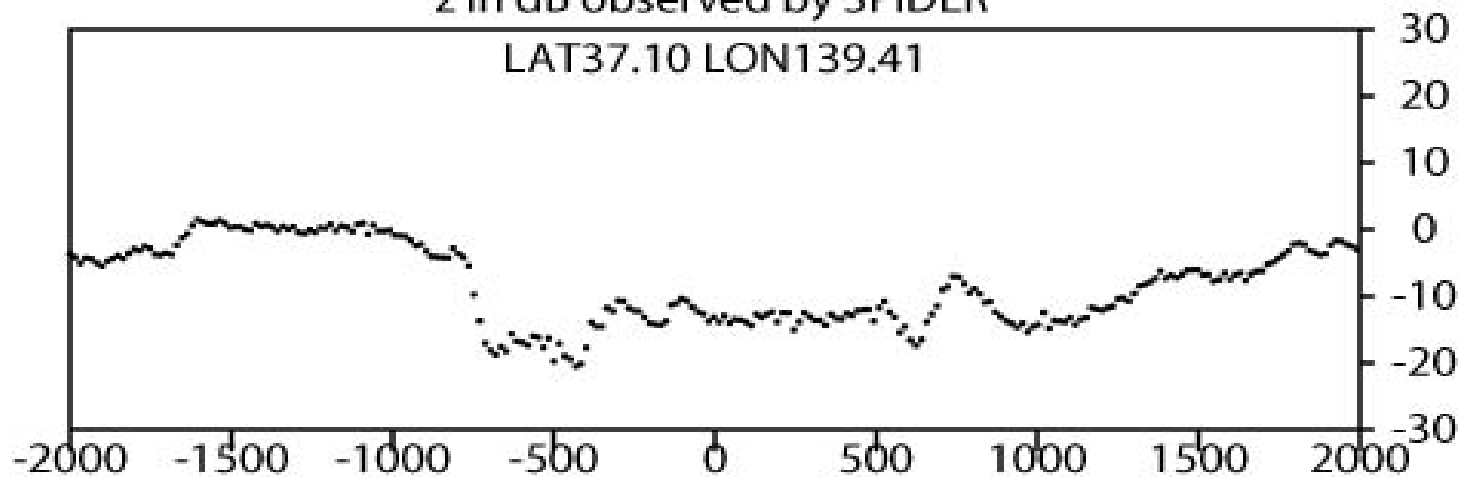
50

# $z(x)$ & $f(x)*v(x)$ pattern in dB

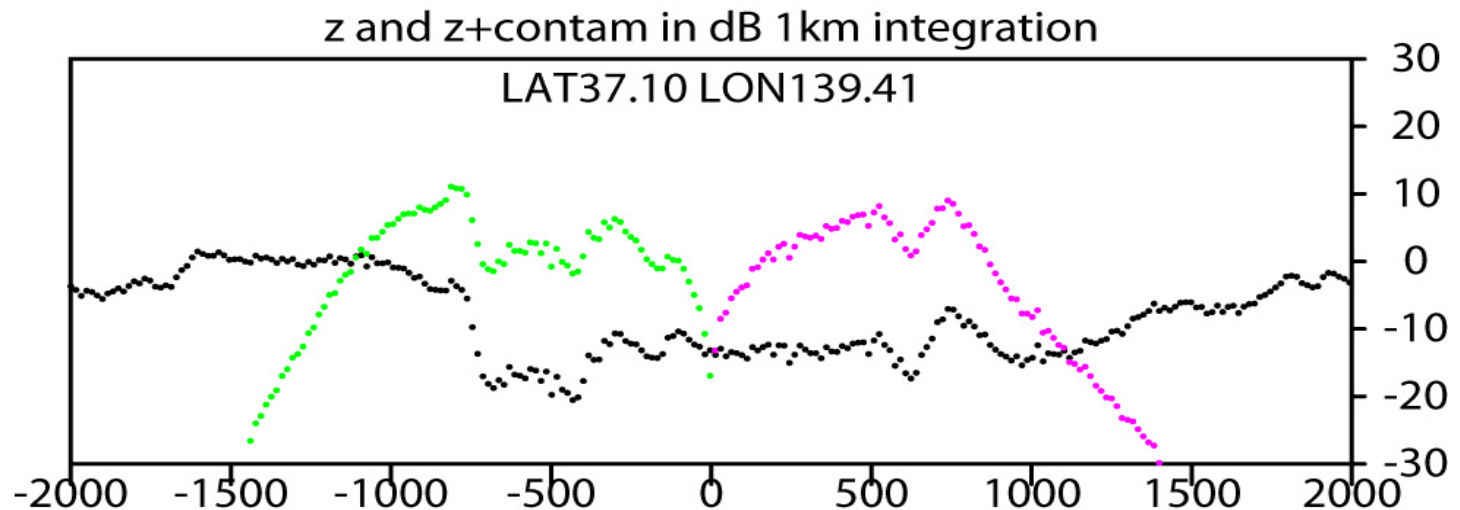
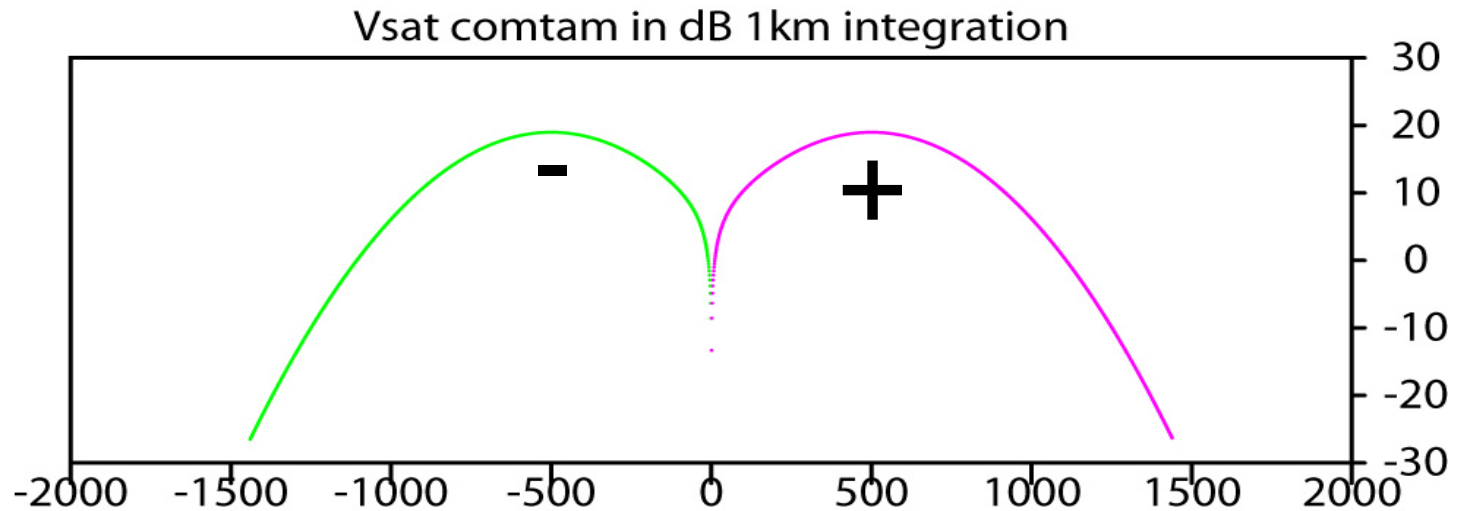
Satellite speed contamination and its 1km integration



$z$  in dB observed by SPIDER

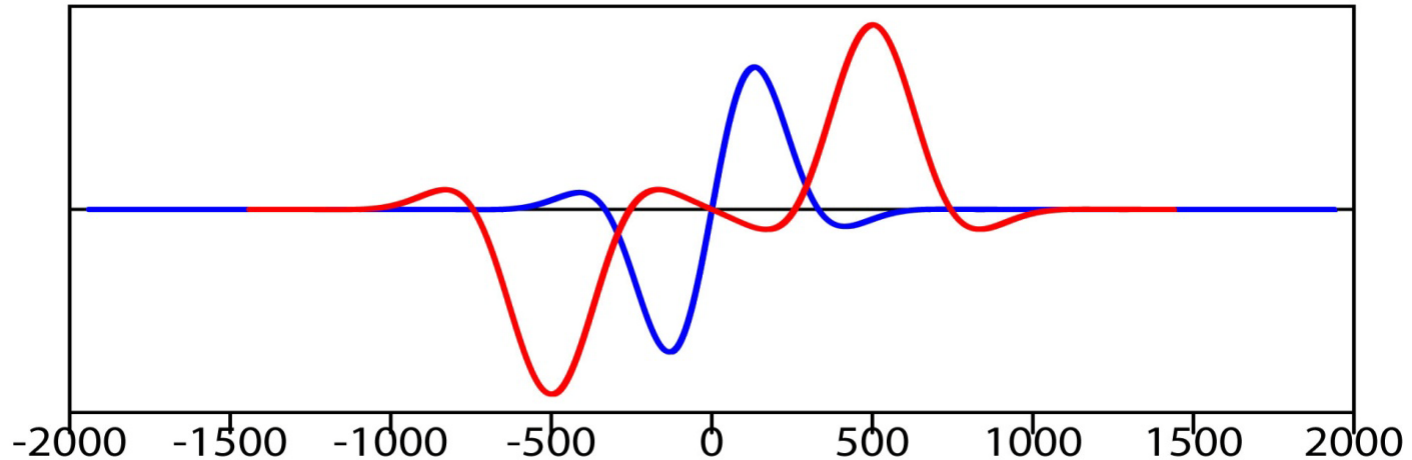


# $z(x)$ & $f(x)*v(x)$ pattern in dB

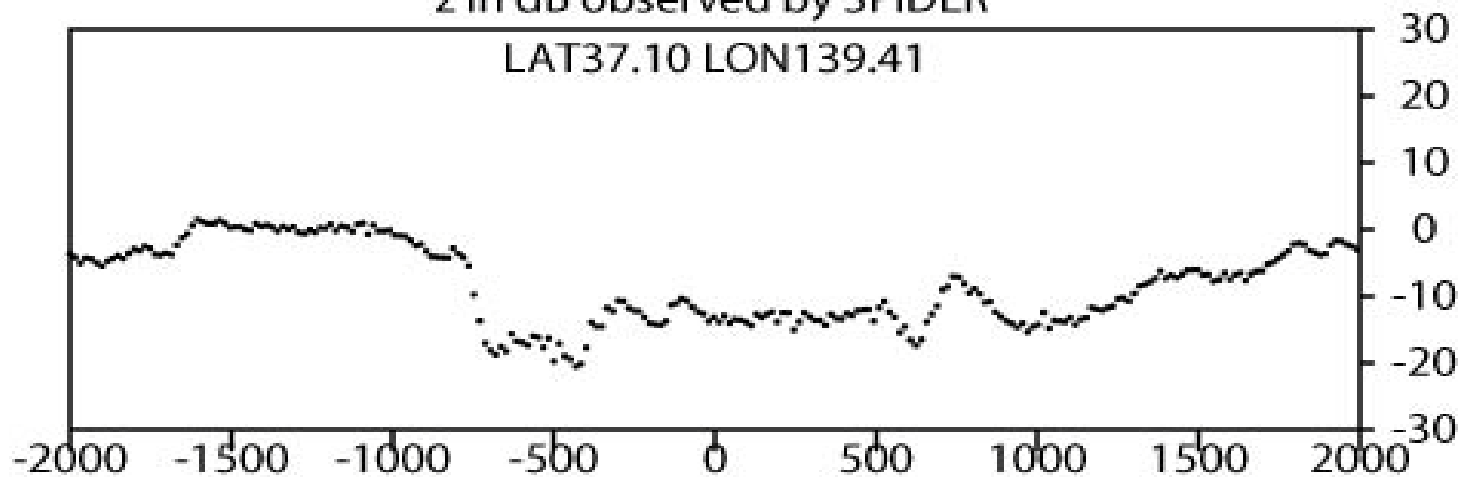


# $z(x)$ & $Q(x)$ pattern in dB

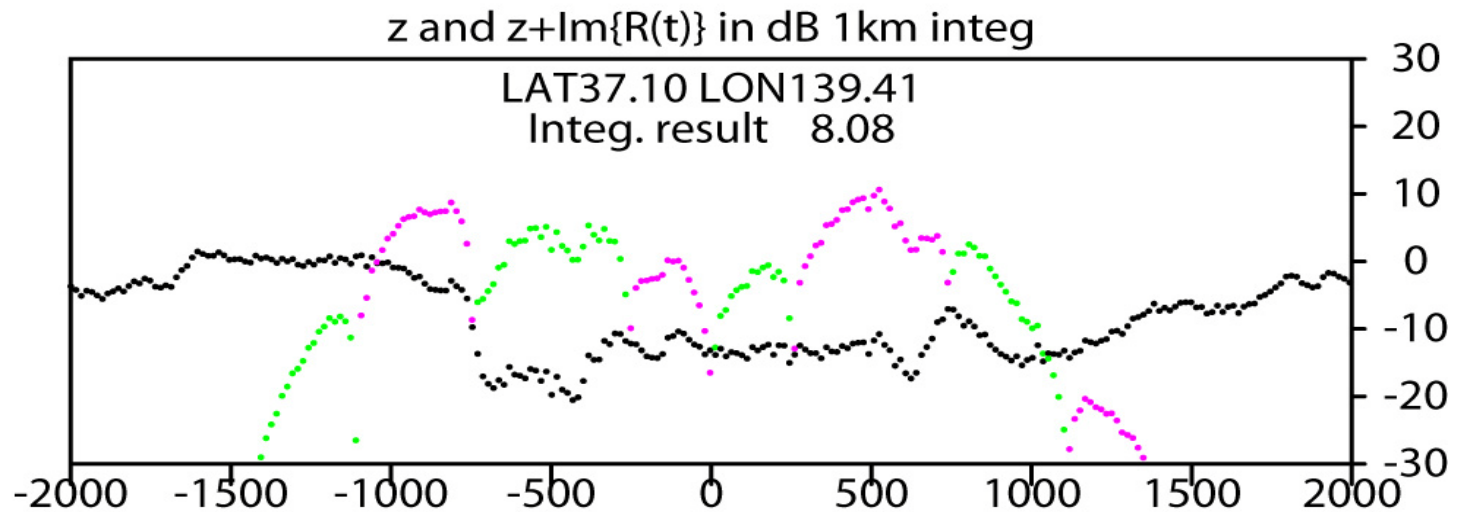
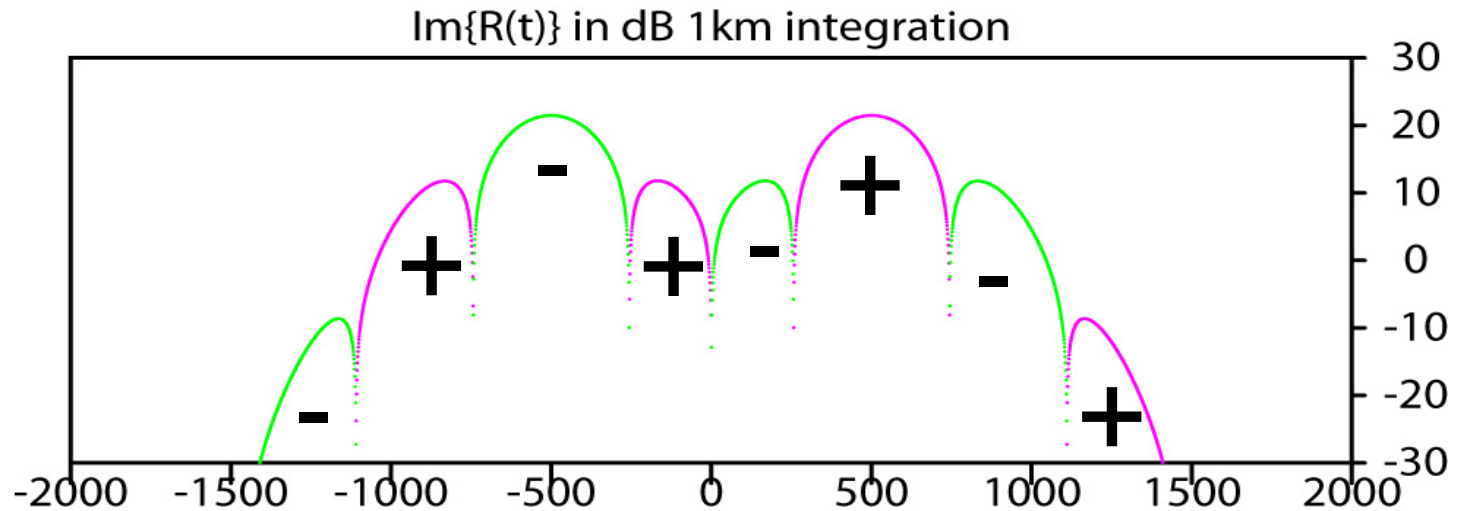
Imaginary{R(t)} and its 1km integration



$z$  in dB observed by SPIDER

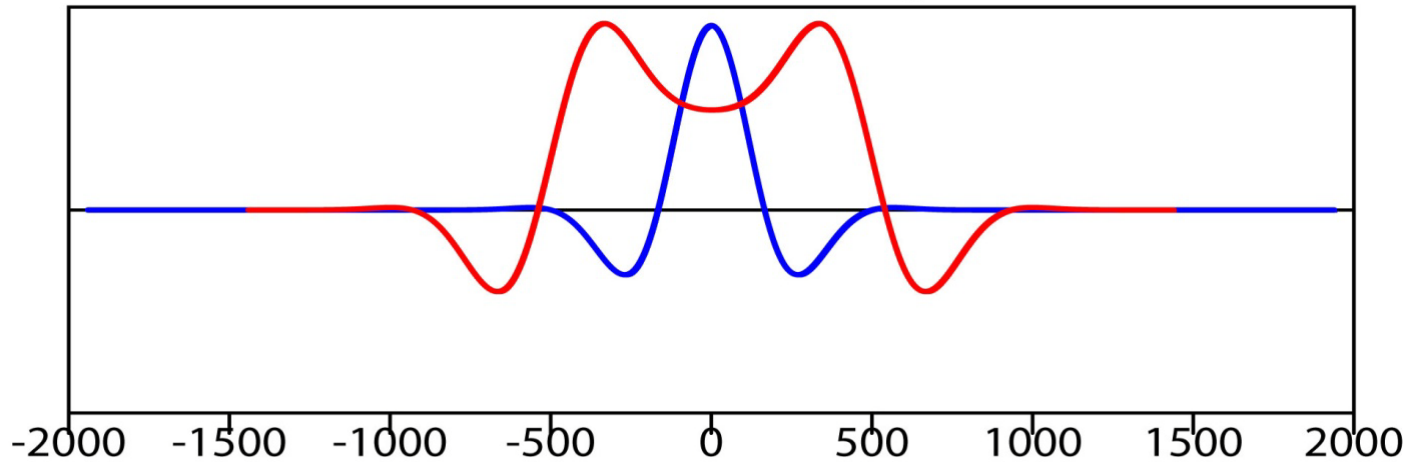


# $z(x)$ & $Q(x)$ pattern in dB

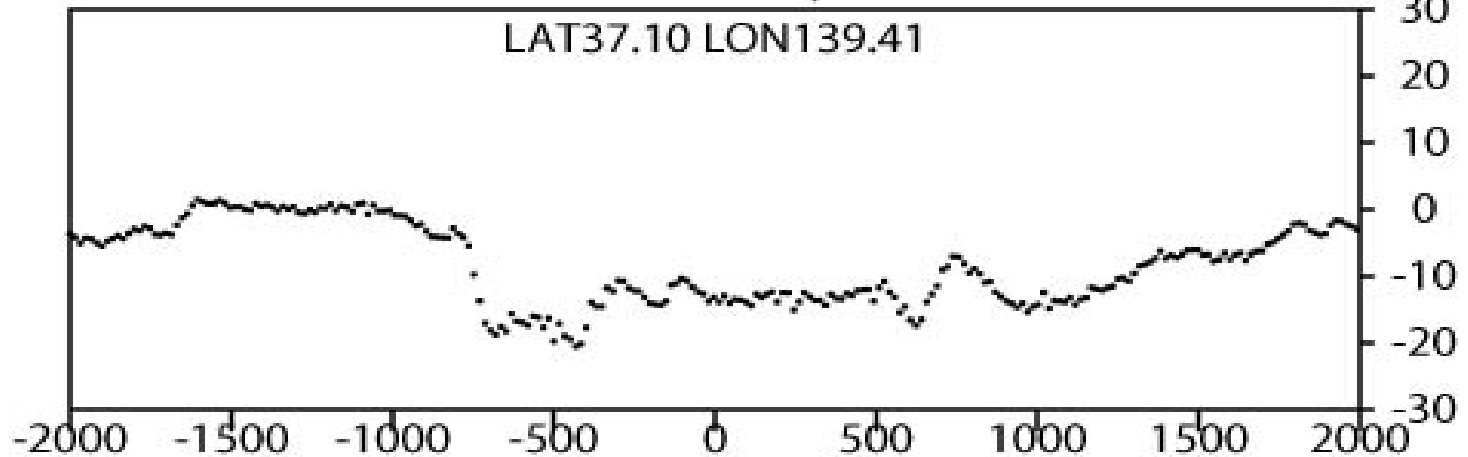


# $z(x)$ & $C(x)$ pattern in dB

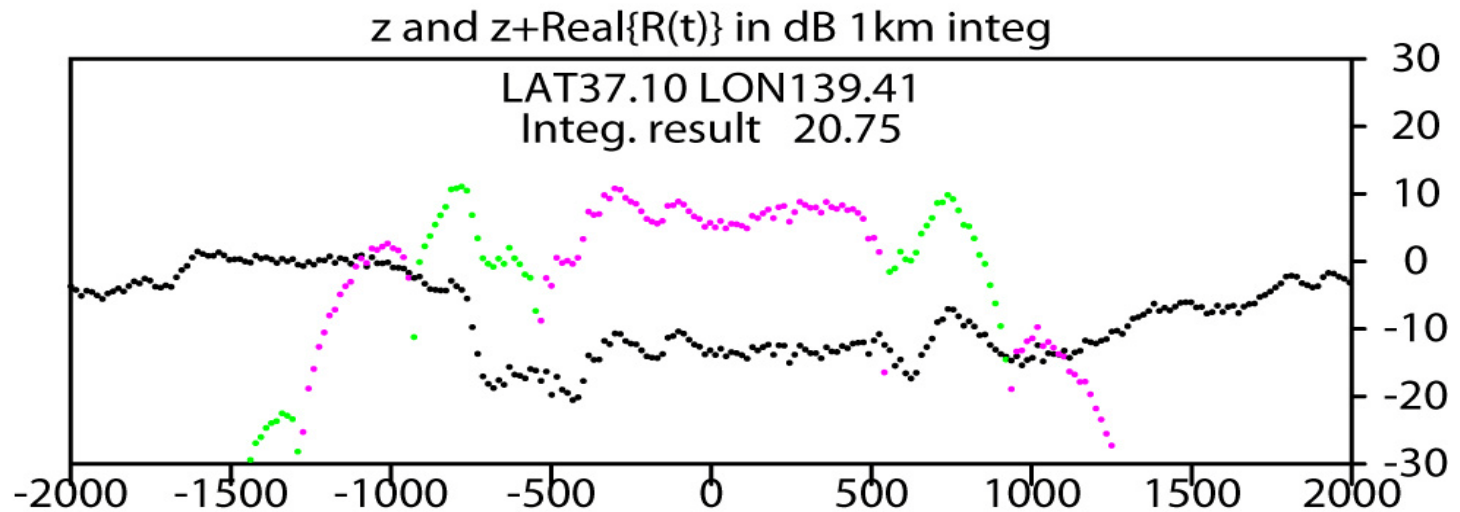
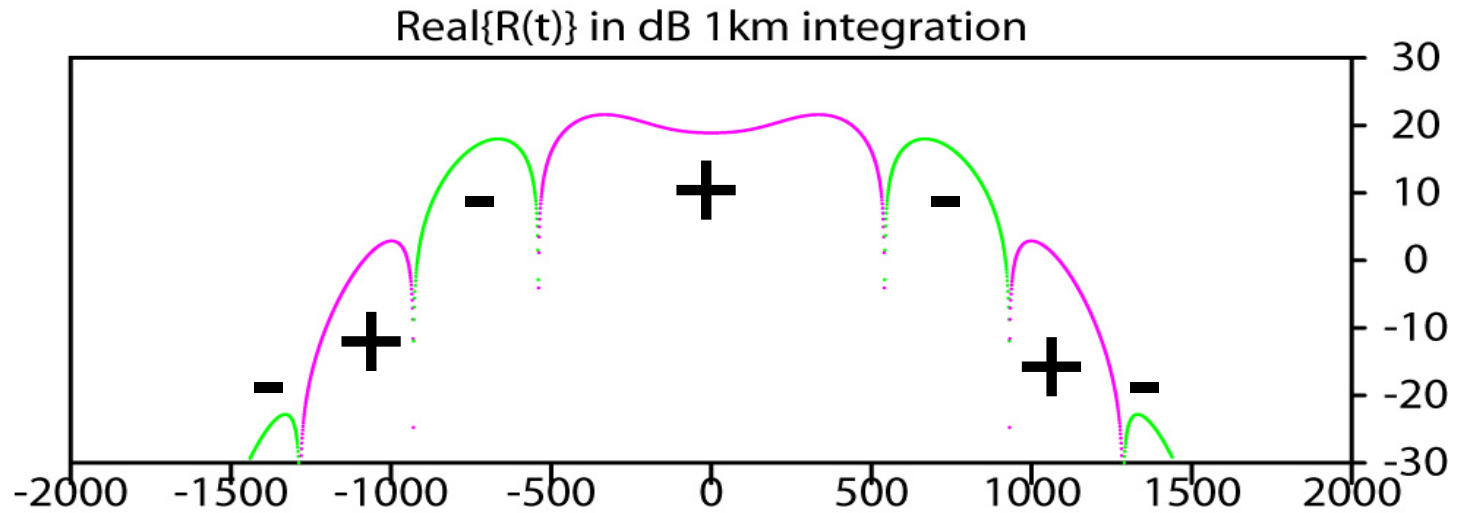
Real{R(t)} and its 1km integration



$z$  in dB observed by SPIDER



# $z(x)$ & $C(x)$ pattern in dB



## Pulse-pair to Doppler error

$$\begin{aligned}\overline{V_{error}}(x_{00}) &= \frac{\lambda \cdot PRF}{4} \arctan\left(\frac{\sum_{-N/2}^{N/2} Q(x_n)Z(x_n)}{\sum_{-N/2}^{N/2} C(x_n)Z(x_n)}\right) \\ &= \frac{3.19E^{-3} \bullet 7500}{4\pi} \tan^{-1}\left(\frac{8.08}{20.75}\right) \\ &= 0.70\end{aligned}$$



# Summary

- 1. Doppler error can be estimated from reflectivity referring first and end footprint**
- 2. Integrated real and imaginary part of  $R(t)$  is useful to considering Doppler error with folding**
- 3. Doppler error value is demonstrated using SPIDER observation**