

# Turbulence intensity retrieval in precipitation via optimal estimation using polarimetric radar

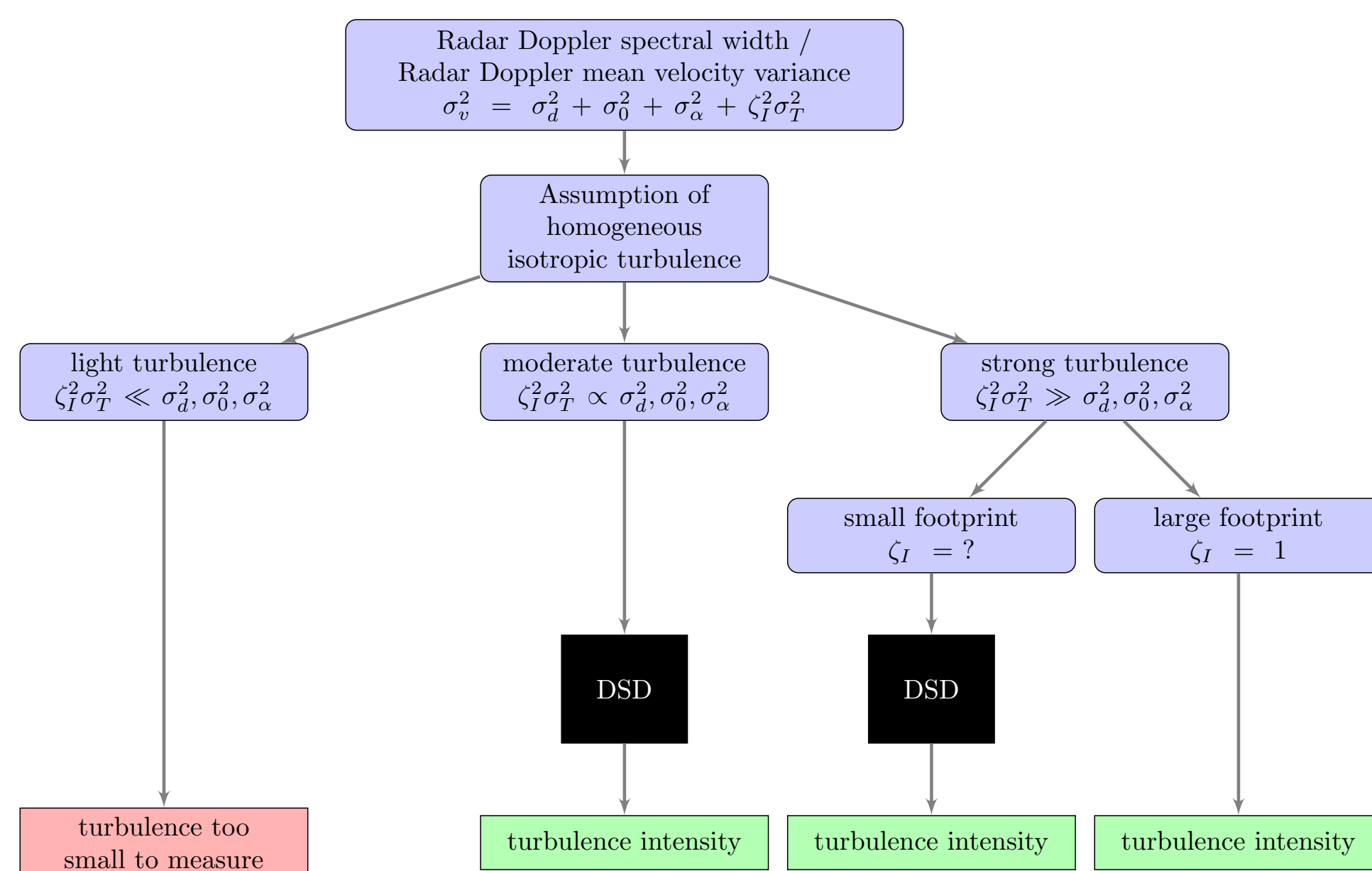
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## Objectives

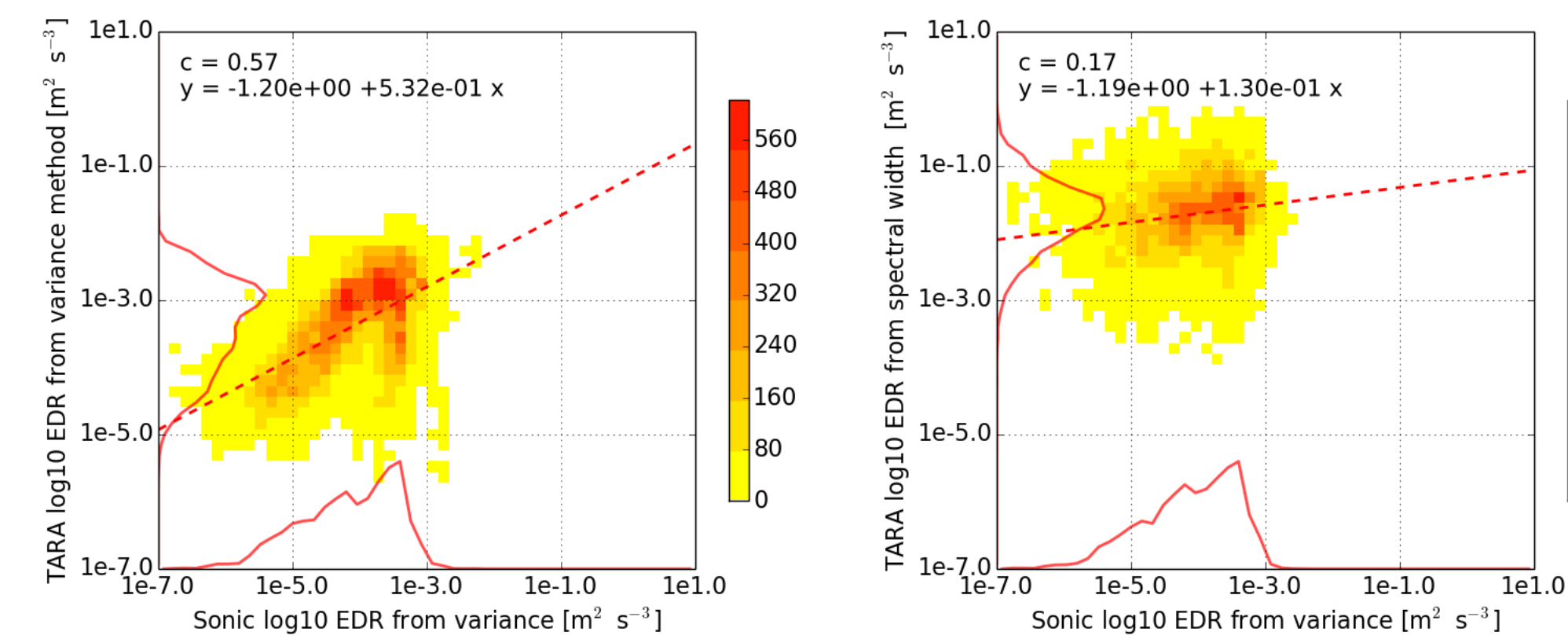
- Develop a radar forward model, where as a function of turbulence intensity, a parametric or stochastic solution can be chosen.
- Develop a generalized methodology to retrieve the turbulence intensity from polarimetric radar data.

## Introduction

- The polarimetric profiling radar at a slant elevation angle is a promising sensor for remote sensing of particle characteristics (Bringi and Chandrasekar, 2004).
- For an accurate turbulence intensity retrieval in rain, often the drop size distribution is crucial.



**Relevance of the DSD on turbulence intensity retrievals.** In this schematic  $\sigma_v$ , the Doppler spectral width or the velocity standard deviation, is the measurement. The contributors to this measurement are antenna motion  $\sigma_a$ , hydrometeor fall speeds  $\sigma_b$ , hydrometeor orientations and vibrations  $\sigma_c$  and turbulence  $\sigma_T$ , where  $\zeta_I$  is the hydrometeor inertia correction. Note that the turbulence contribution scales with the spatial scale  $\sigma \propto L^{1/3}$ .



**Scatter density plots of eddy dissipation rate (EDR) from profiling radar (TARA) versus a sonic anemometer.** left) EDR from 10 min. of mean Doppler velocities and right) EDR from spectral width, with a correction for fall speed width (Yanovsky et al., 2015). In these retrievals no polarimetric information is used.

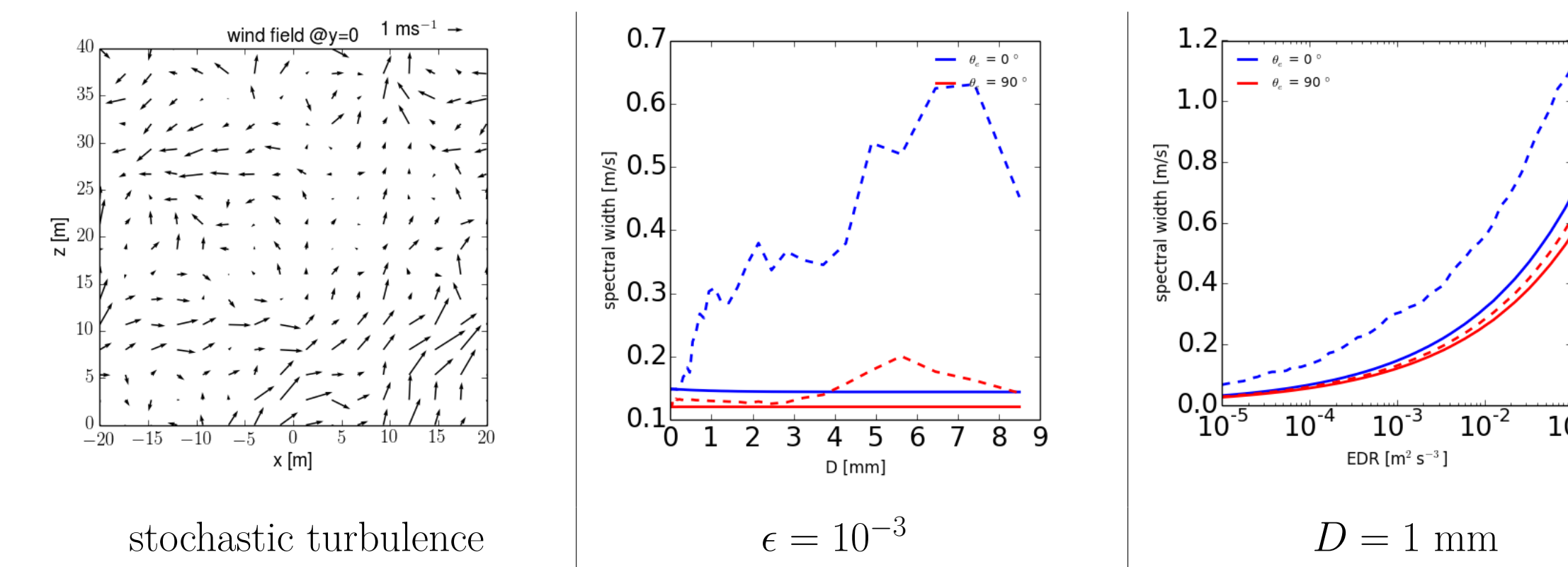
## Simulation of the inertia effect

- We estimate the effect of droplet inertia on the radar measurements by solving the equations of motion for an ensemble of droplets for a backward trajectory.
- We use 3D stochastic turbulence from Mann (1998).
- The inertial velocity term  $\vec{v}_p'$  is assumed to be small in comparison to the total particle velocity.
- The particle velocity is written as:

$$\vec{v}_p = \vec{v}_t + \vec{v}_a + \vec{v}_p' \quad (1)$$

where  $\vec{v}_t$  is the terminal fall velocity and  $\vec{v}_a$  the air velocity. The solution is found by solving the equations of motion for a small trajectory, e.g. for the z-direction:

$$\frac{dv_{p,z}}{dt} = F_g - F_b - F_{d,z} = \eta_{I,z} v_t^2 - \eta_{I,z} (v_{p,z} - v_{a,z})^2 \quad (2)$$



stochastic turbulence simulation of inertia Doppler spectral width with (striped) and without (line) the inertia effect.

## Relevance of inertia

- The inertia effect can double the spectral width.
- The inertia effect is more relevant for horizontally pointed radar.

## Forward model

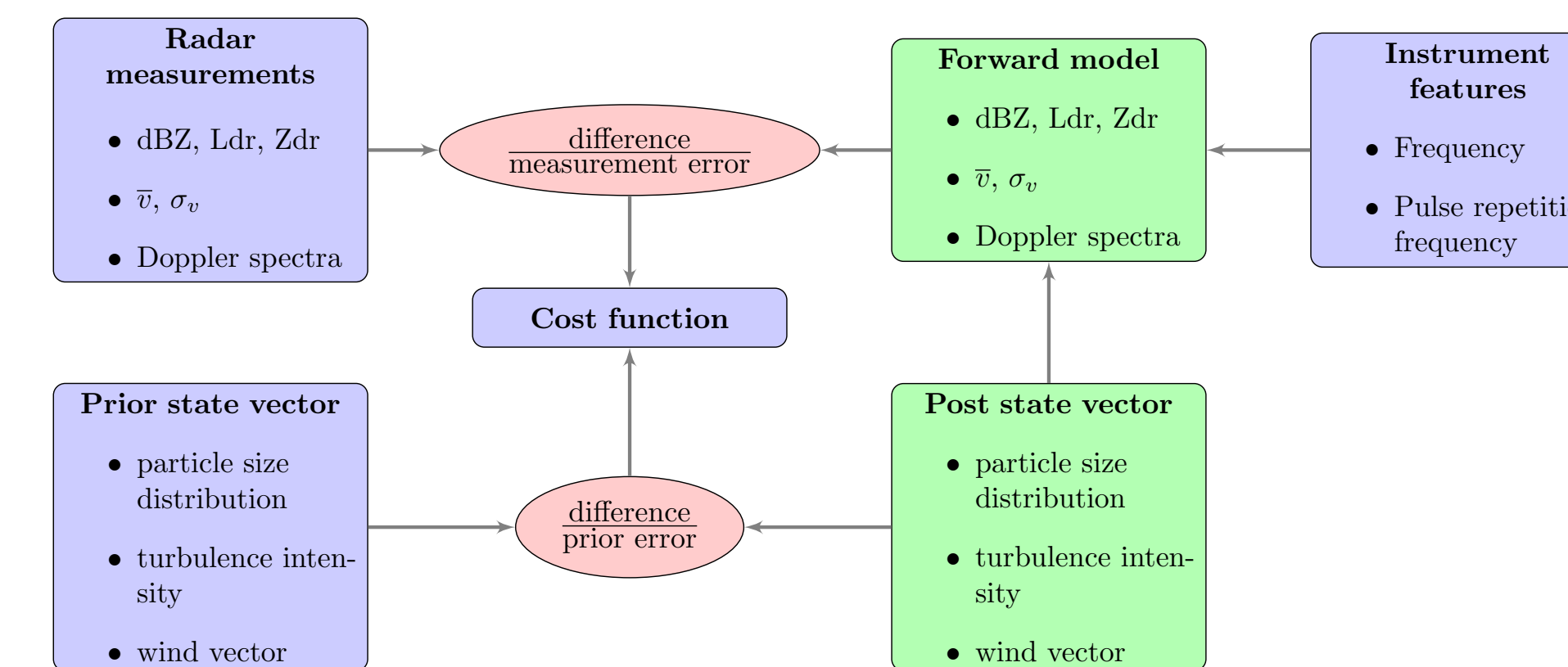
- An ensemble of particles is used to cover a spatial distribution, matching the radar resolution volume and a size distribution.
- Cross sections from Mishchenko (2000) and terminal fall velocities from Khvorostyanov and Curry (2005) are used.
- The particle symmetry axis is oriented parallel to the particle motion.
- Turbulence is modelled as an ensemble of isotropic vectors, with the standard deviation of radials speed from White et al. (1999).

	0.1 mm	1.0 mm	5.0 mm
<b>light turbulence,</b> $\sigma = 0.1 \text{ ms}^{-1}$ .			
<b>heavy turbulence,</b> $\sigma = 2.0 \text{ ms}^{-1}$ .			

**An ensemble of isotropic vectors.** Shown are the orientations of the ensemble, which depend on the relative sizes of the terminal fall speed, air velocity and turbulence velocity.

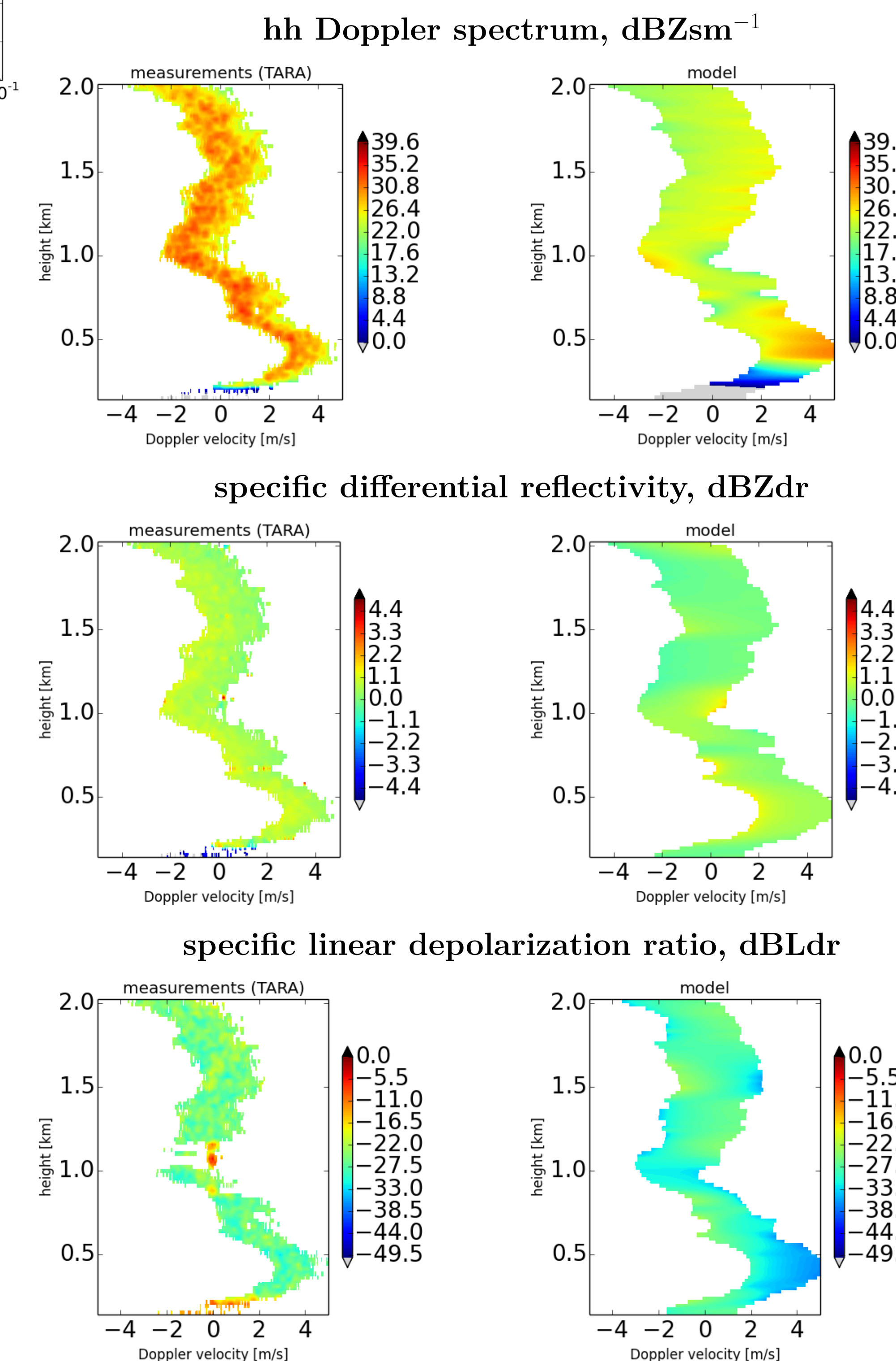
## Optimal estimation

- In optimal estimation the model parameters are fitted to the measurements via minimization of the cost function.
- The cost function consists of differences in measurements space and parameter space. We use the NLOpt package for minimization.

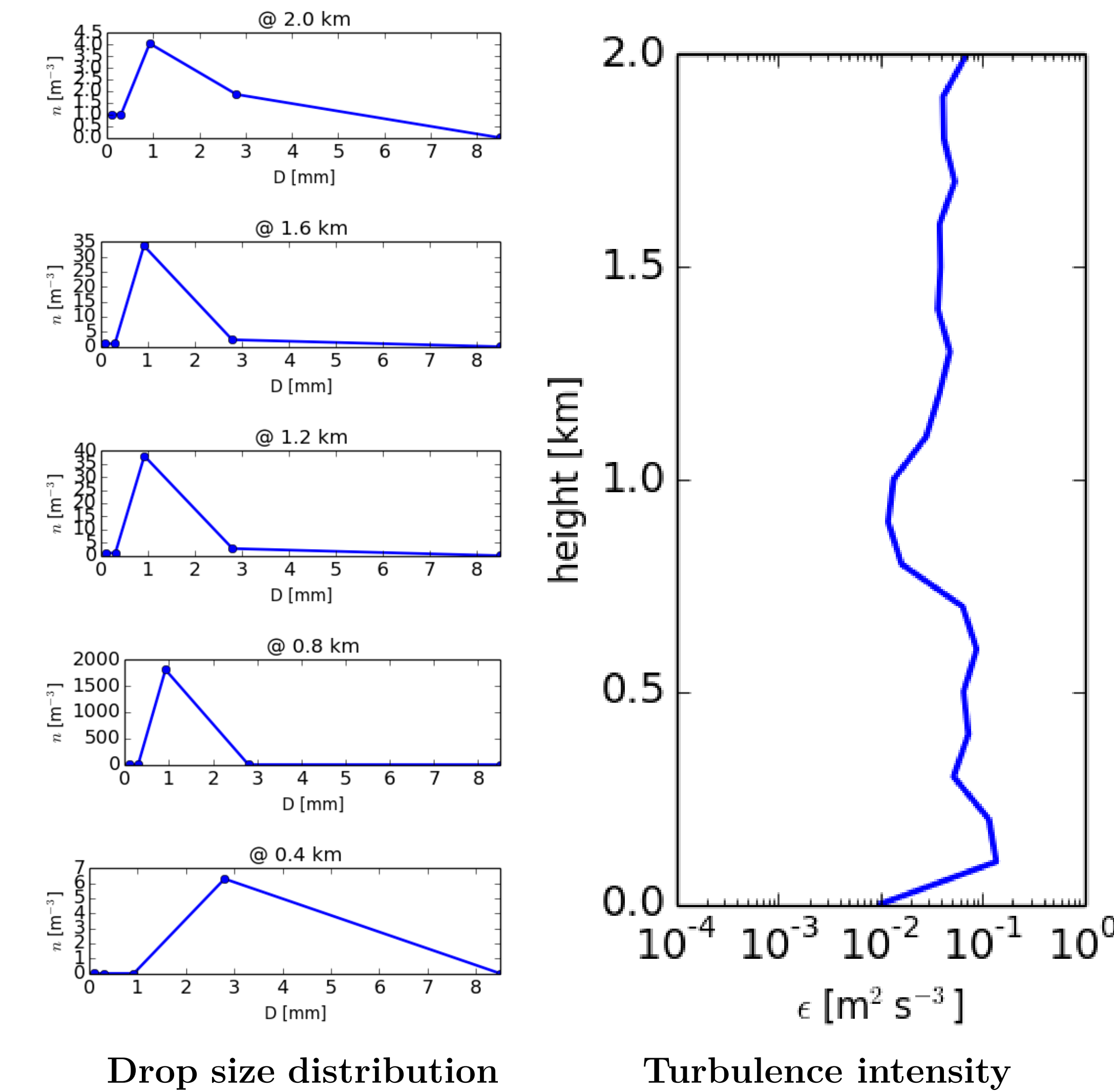


## Optimal estimation retrieval technique

## Measurements vs. forward model



## Retrieved profiles



## Discussion

- A novel forward model is proposed for retrievals of turbulence intensity profiles, which takes the orientations of particles into account.
- The inertia effect increases the Doppler spectral width.
- Error estimation of the posterior size distribution will improve the interpretation of radar measurements.

## Additional Information

**Download** The model Zephyros, a package for radar simulations and retrievals of wind and turbulence, under development, is written in C with interfaces to Python and Matlab and can be downloaded from: <https://github.com/albertoudenijhuis/zephyros0.4>

## References

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