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# Development of a 4DVAR version of GSI at NCEP

*Miodrag Rancic, EMC/NCEP/IMSG*  
*Daryl Kleist, EMC/NCEP*  
*Ricardo Todling, GMAO/NASA*

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[miodrag.rancic@noaa.gov](mailto:miodrag.rancic@noaa.gov)



# Content

- ▶ Development of a 4DVAR version of GSI
- ▶ A single observation test
- ▶ Example of a single analysis
- ▶ Improving efficiency of the perturbation model
- ▶ Other developments and future work

# 1. Development of a 4DVAR version of GSI at NCEP

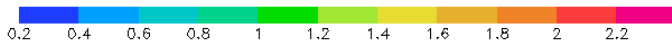
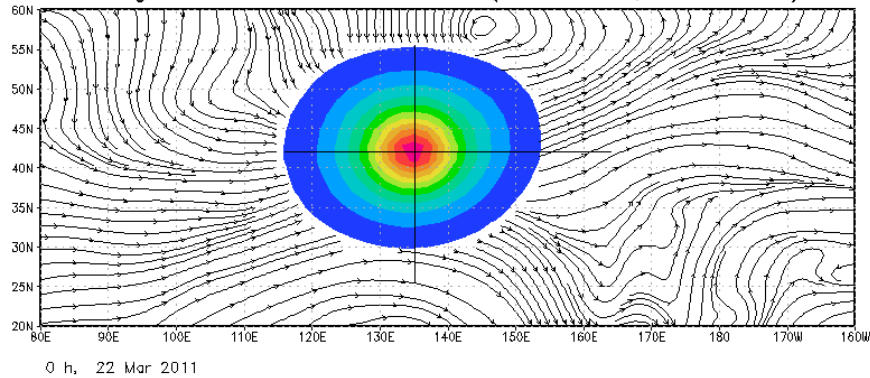
- ▶ Contemporary observations of the atmosphere (such as those coming from the geostationary, polar orbiting and GPS satellites) are spread through the analysis window
- ▶ In the classical 3DVAR we knowingly introduce error in the estimation of the innovation vector (observation minus background) by comparing observations with the background at the analysis time
- ▶ **FGAT** (First Guess at Appropriate Time) 3DVAR improves this situation to some extent, by introducing more than one background field

- ▶ At NCEP, we tried to increase a “temporal awareness” of our data assimilation system *GSI* (Grid-point Statistical Interpolation) by a simple method **FOTO** (First Order interpolations To Observations)
- ▶ An **ensemble based 4-dimensional** data assimilation method has been recently finished, which prescribes the time evolution through ensemble perturbations
- ▶ A **classical**, weak constraint **4DVAR**, where innovation is propagated in time using a tangent linear model, **M** (TLM), and its adjoint, **M<sup>T</sup>** (ADM), is arguably still capable to satisfy most criteria (a full rank method, long assimilation window, inclusion of model error, etc.)

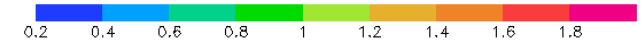
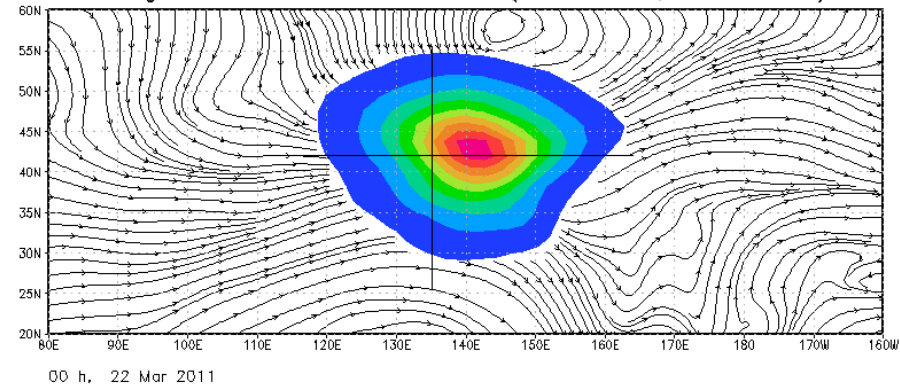
- ▶ The **model based 4DVAR** has been recently **merged with the Hybrid EnKF** within GSI, which we expect to further advance the realism of the analysis
- ▶ **A 4DVAR option**, with several appropriate minimization and preconditioning algorithms (Lanczos, sqrtB, etc.), has been introduced in GSI through **collaboration with GMAO/NASA**
- ▶ **Perturbation model** for driving 4DVAR has been derived by readjusting a pre-existing tendency model, used in 3DVAR for formulation of the dynamical constraints
- ▶ It maintains **the same vertical structure as GFS** (Global Forecasting System - Global model at NCEP), but horizontal gradients are derived using high-order compact differencing

# 2. Single Observation Tests

Single Obs 3DVAR: T inc XY (anal=0 h ; obs=-3 h)

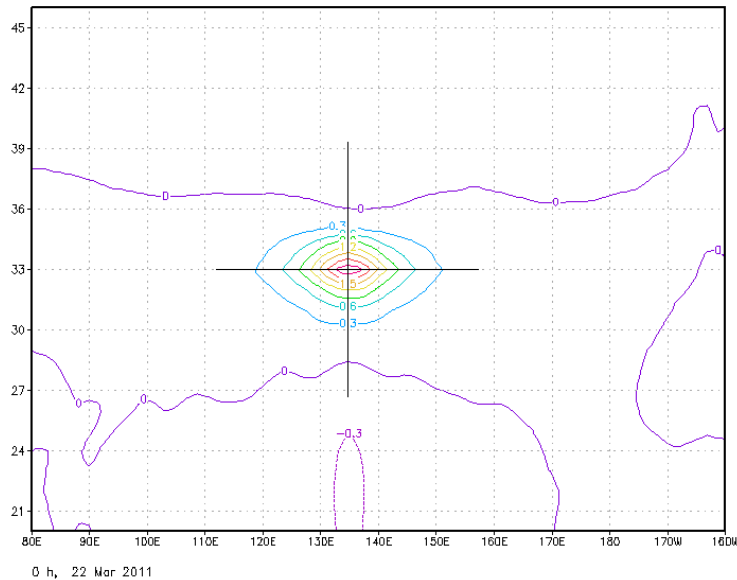


Single Obs 4DVAR: T inc XY (anal=0 h ; obs=-3 h)



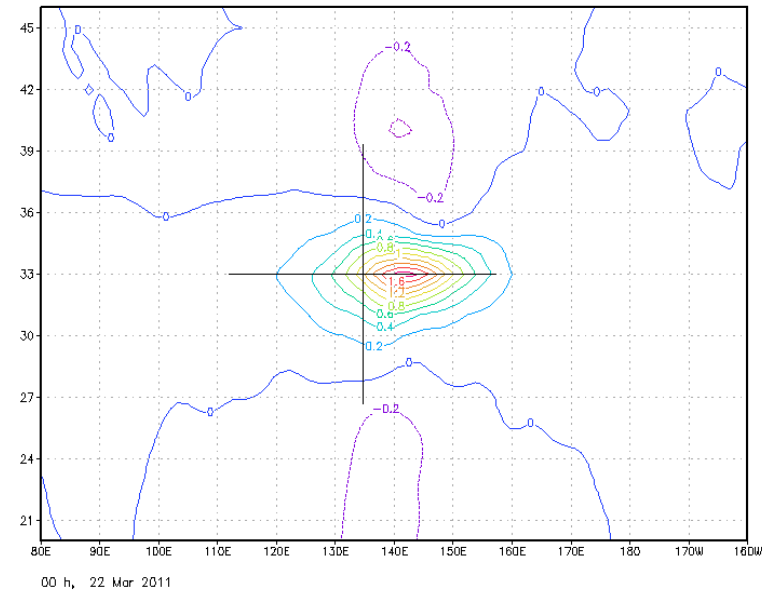
Single Obs 3DVAR: T inc XZ (anal=0 h ; obs=-3 h)

2-13:14

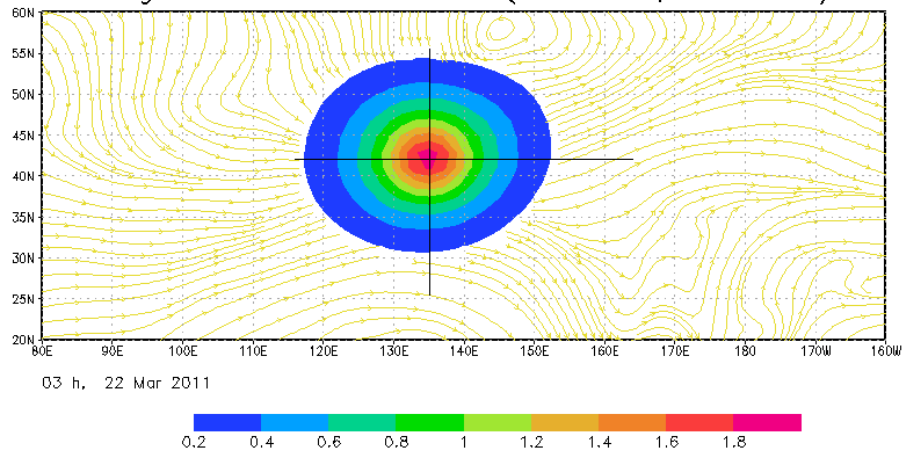


Single Obs 4DVAR: T inc XZ (anal=0 h ; obs=-3 h)

grADS:  $\alpha$



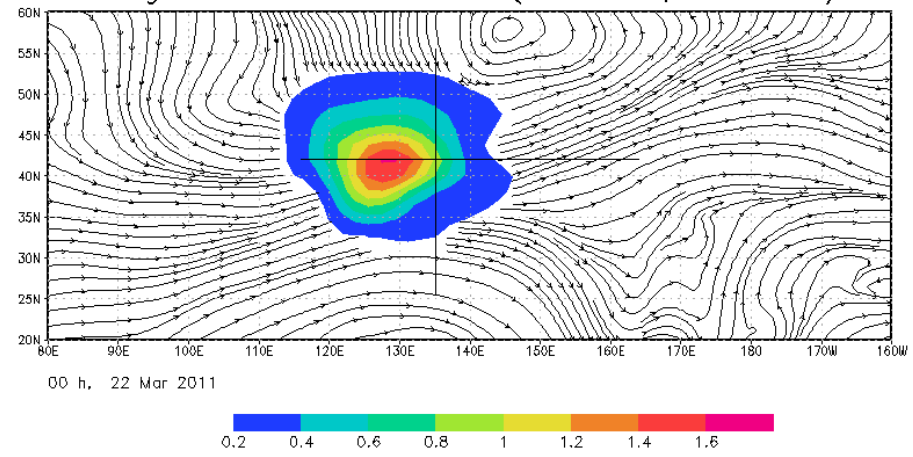
Single Obs 3DVAR: T inc XY (anal=0 h ; obs=+3 h)



GRADS: COLA/IGES

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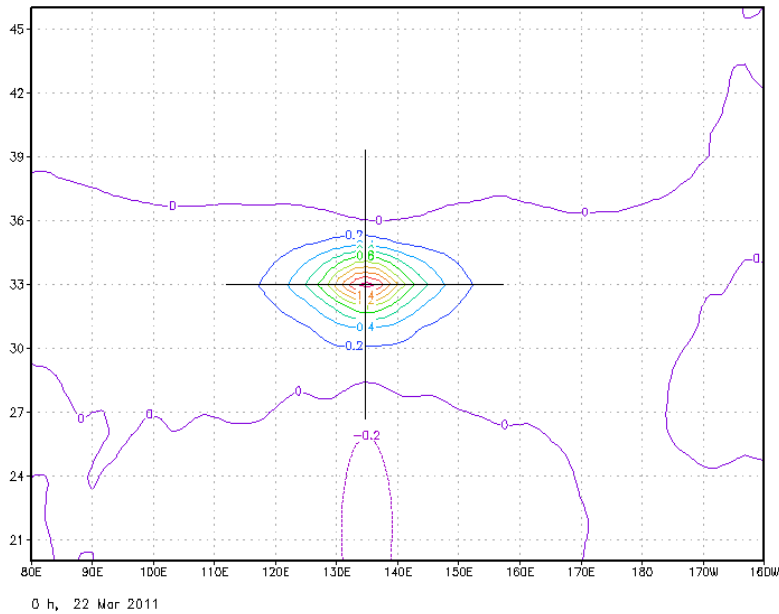
Single Obs 4DVAR: T inc XY (anal=0 h ; obs=+3 h)



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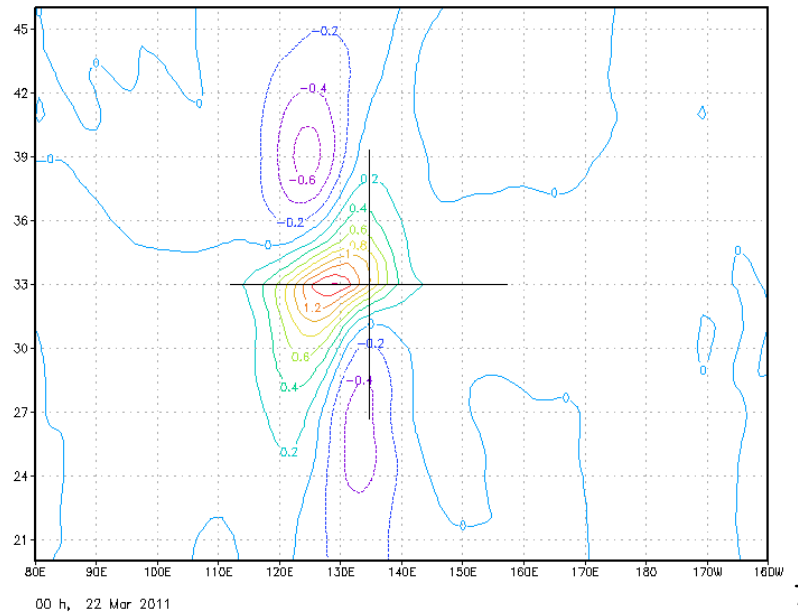
Single Obs 3DVAR: T inc XZ (anal=0 h ; obs=+3 h)



GRADS: COLA/IGES

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Single Obs 4DVAR: T inc XZ (anal=0 h ; obs=+3 h)



GRADS: COLA/IGES

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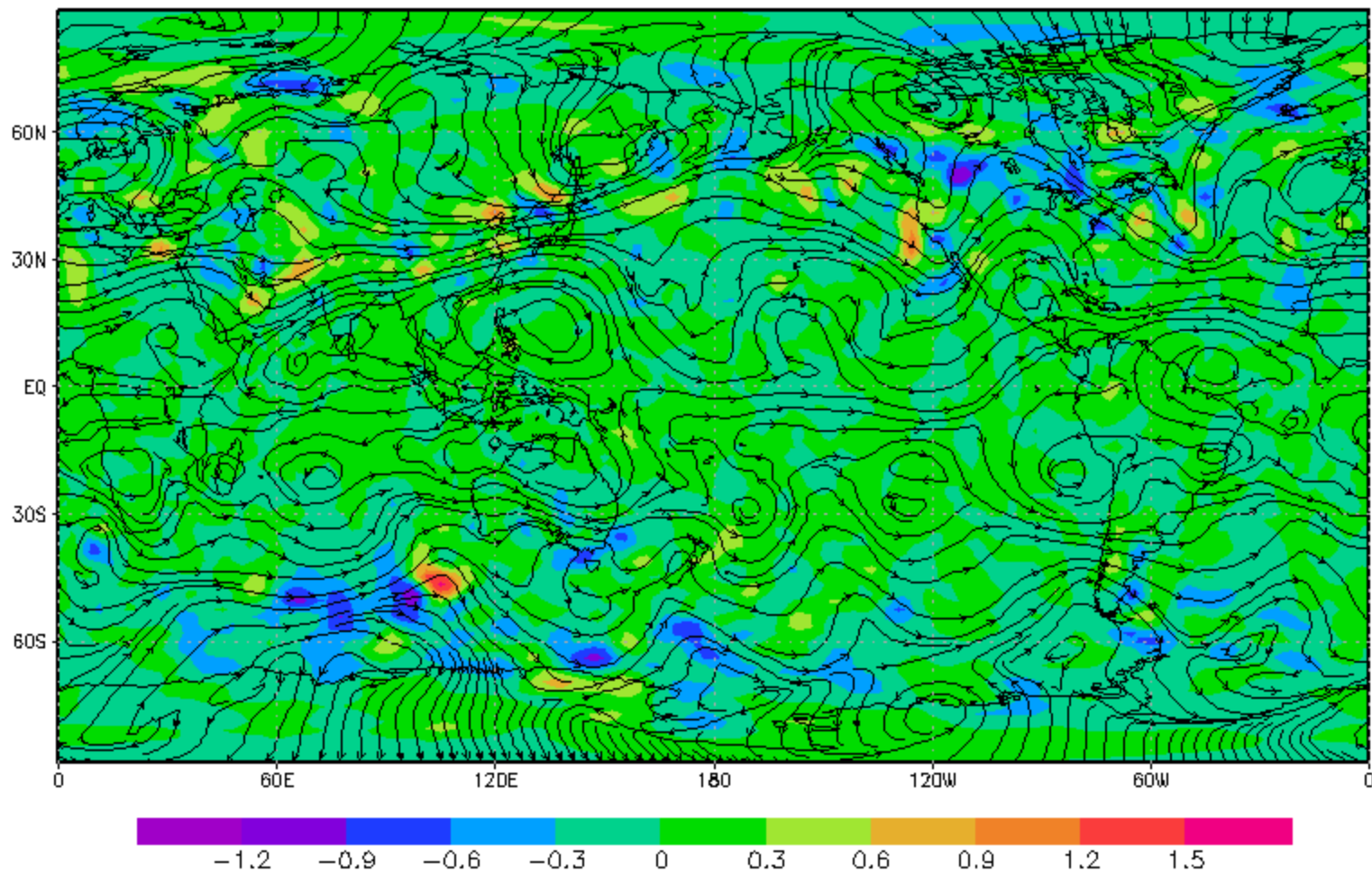


### 3. Example of a single analysis

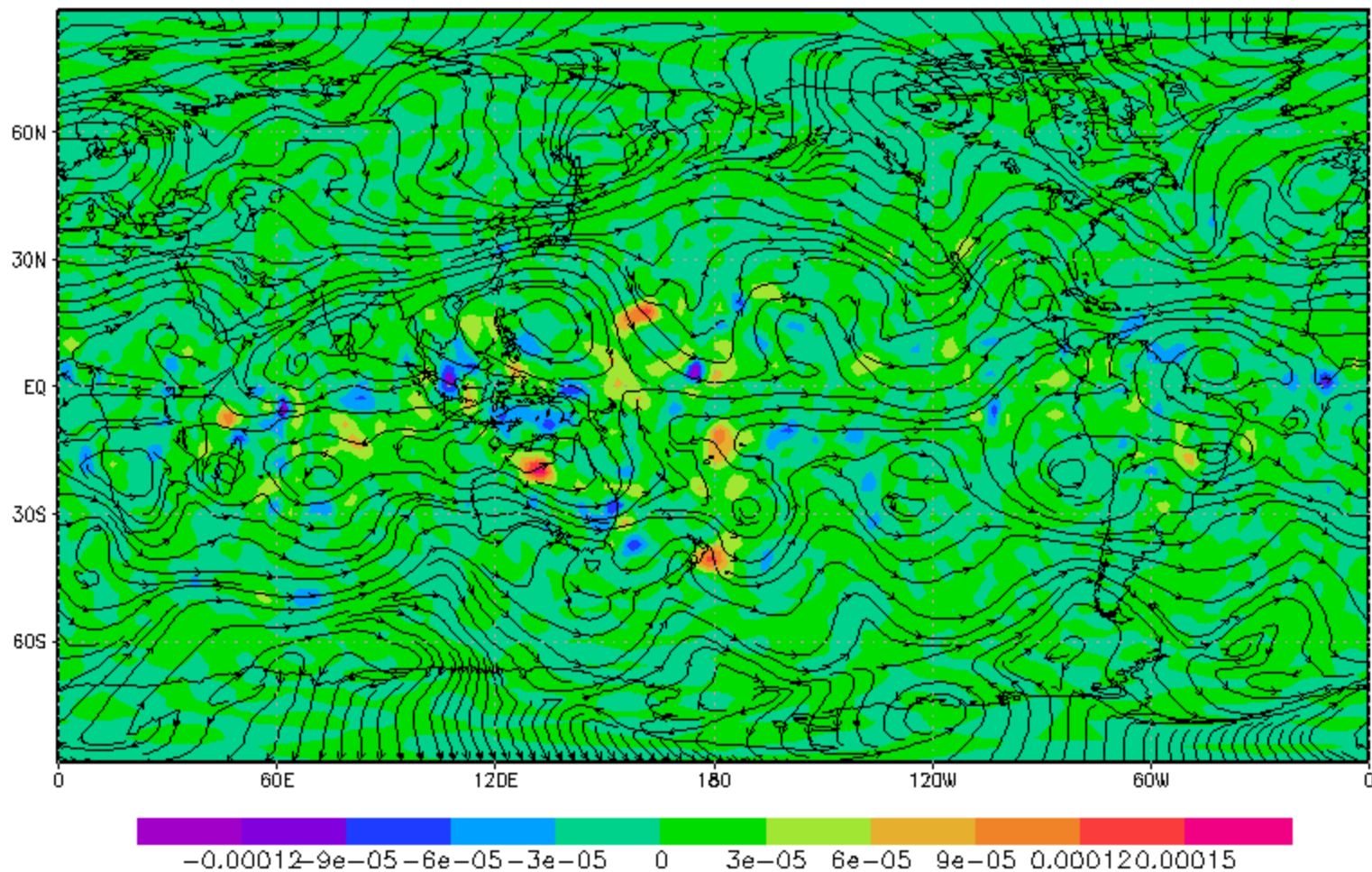
- ▶ T62 Gaussian grid
- ▶ Nonlinear fields are read in **1 hour intervals**
- ▶ **Analysis window is 6 hours** long, with the analysis time in the middle
- ▶ Analysis for March 22, 2011 at 0 h
- ▶ Code is organized in such a way that we run separately the '**observer**' and the **minimization**



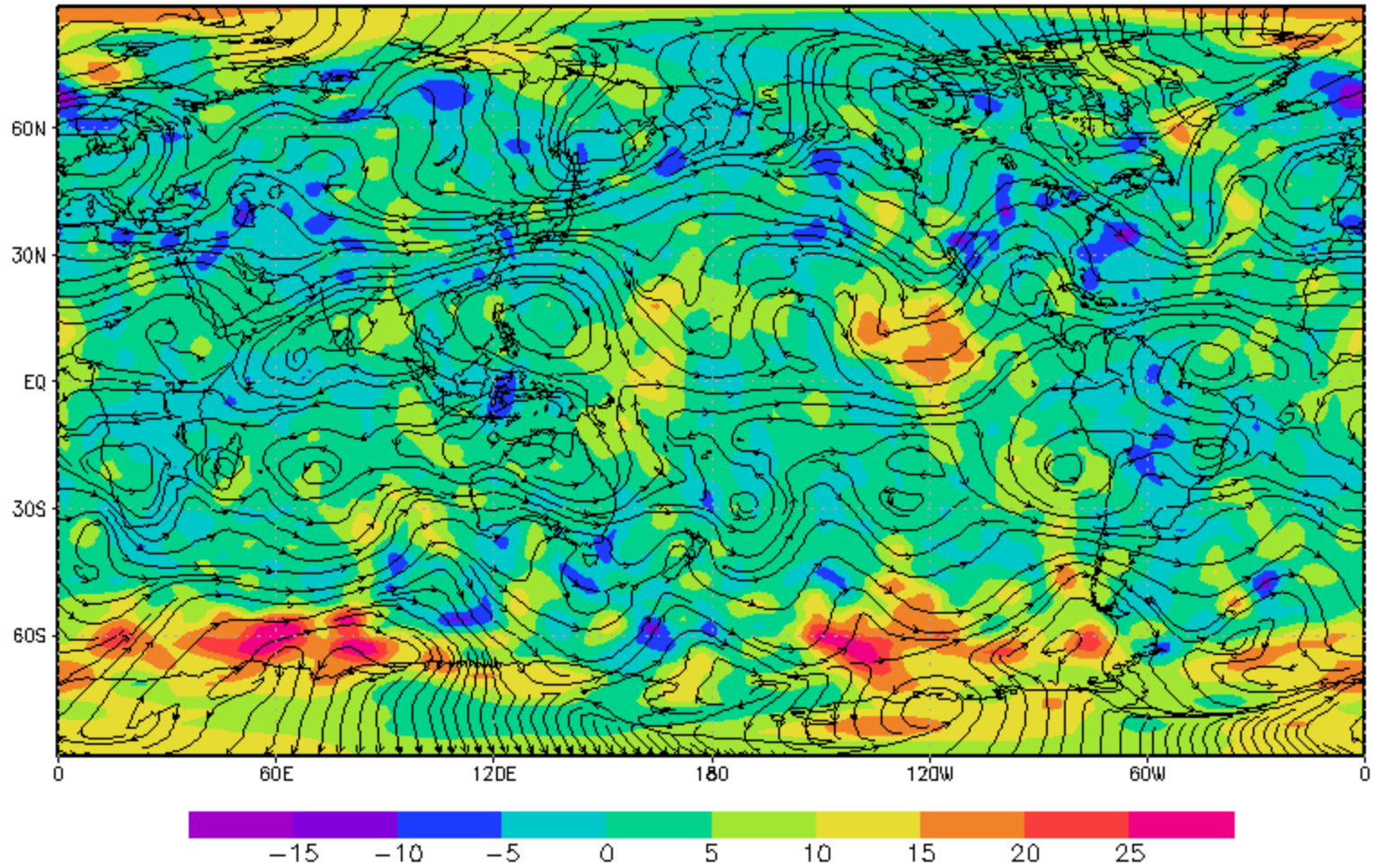
t\_4dvar-t\_3dvar at lev 32



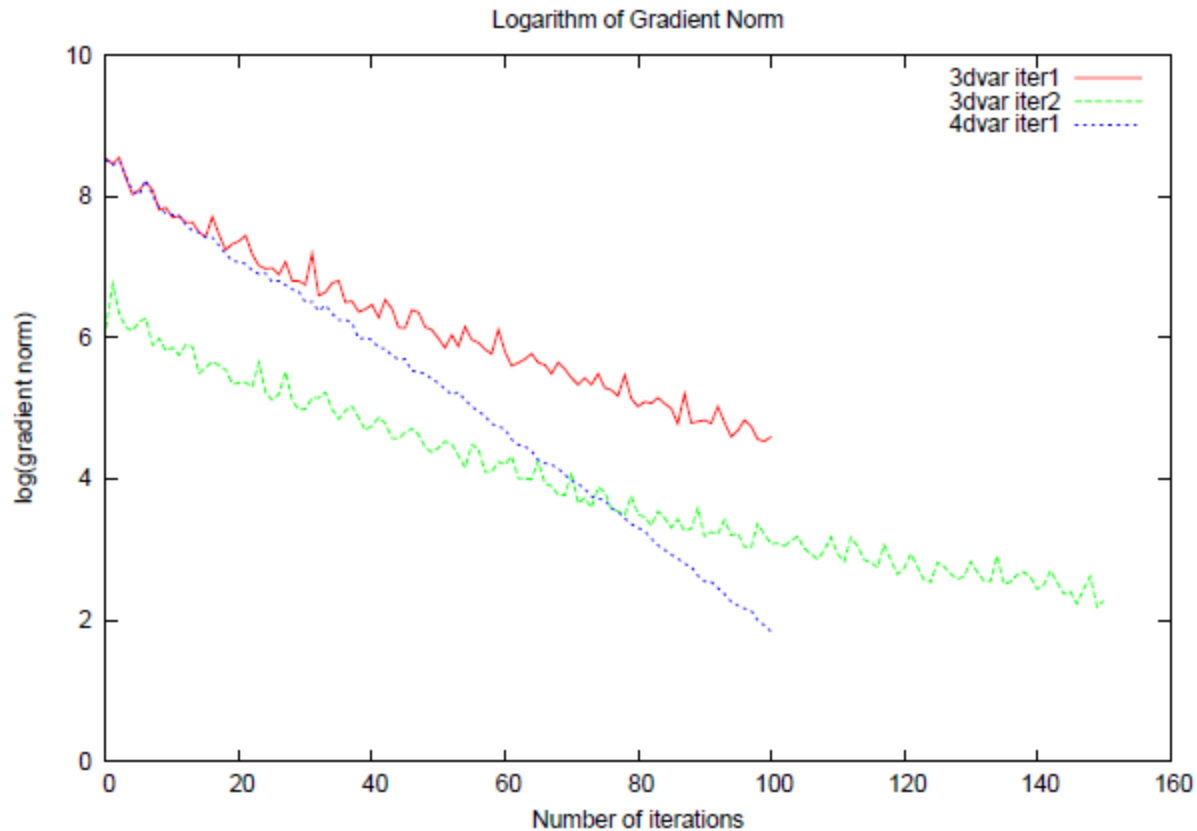
q\_4dvar-q\_3dvar at lev 32



$p_{4dvar} - p_{3dvar}$  at lev 32



# Logarithm of the Gradient Norm

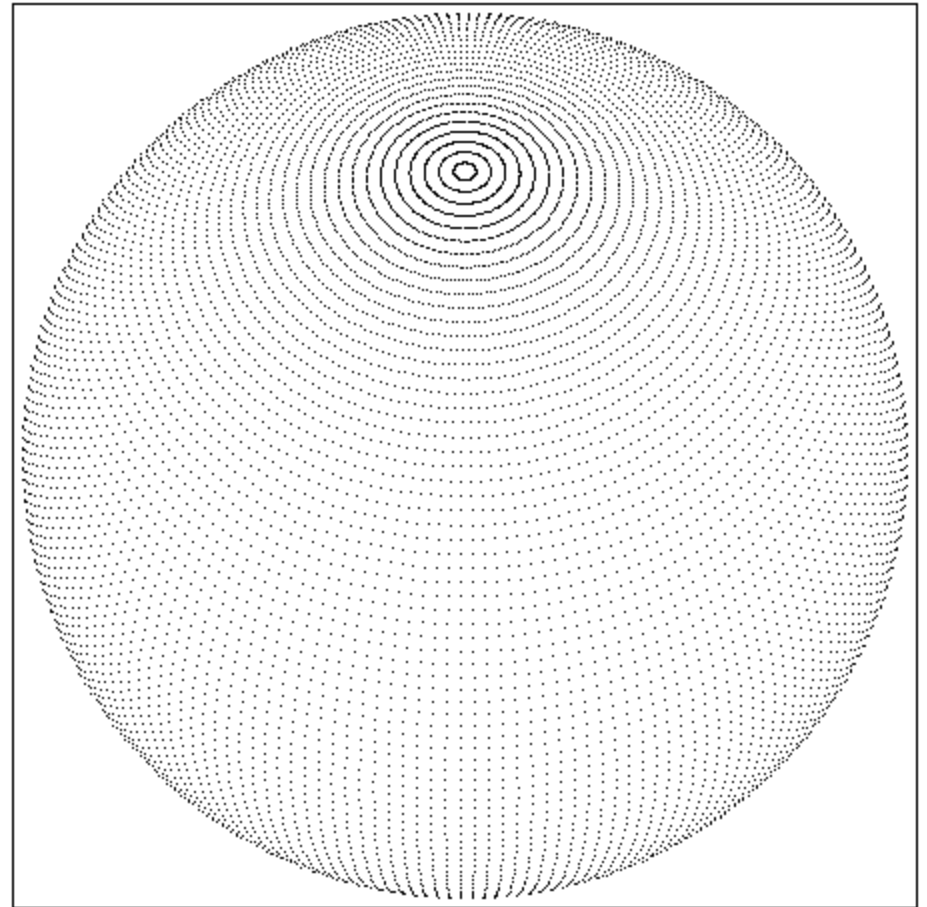


# Computational Efficiency

- ▶ 3DVAR spends 654.966 s, using preconditioned conjugate gradient for minimization, using 32 PE of NCEP's IBM supercomputer
- ▶ 4DVAR spends 238.940 s for observer, and 4769.815 s for minimization, using Lanczos algorithm for minimization with 100 inner iterations (~7.6 times more)
- ▶ With typical 2 outer loops, first with 100, followed by another with 150 inner iterations, **4DVAR is at this stage about ~16-20 time more expensive than 3DVAR**

## 4. Improving efficiency of the perturbation model

- ▶ The major consumer of computational time is **perturbation model**, primarily due to a very small time step on the Gaussian grid (**3 min on T62 resolution!!**)



# Several strategies for improving efficiency are investigated

- ▶ Further **simplifications** of the model
- ▶ Application of a **cylindrical** longitude-latitude grid
- ▶ Applying a new concept of polar filtering through **zonal averaging** of tendencies
- ▶ Running model on a **reduced grid**
- ▶ Reformulating model using a **quasi-uniform grid**



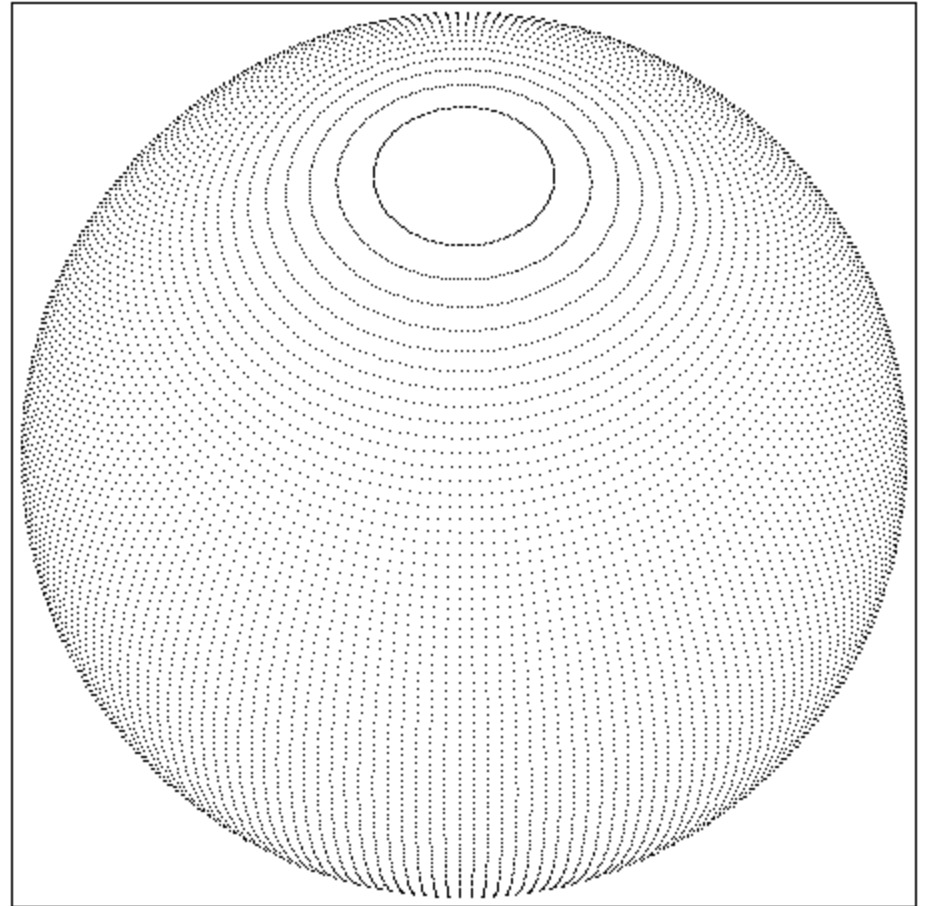
# Cylindrical grid (Sadourny 1975)

- ▶ Cylindrical grid is defined by assuming spherical coordinates as

$$x = \lambda$$

$$y = \sin \varphi$$

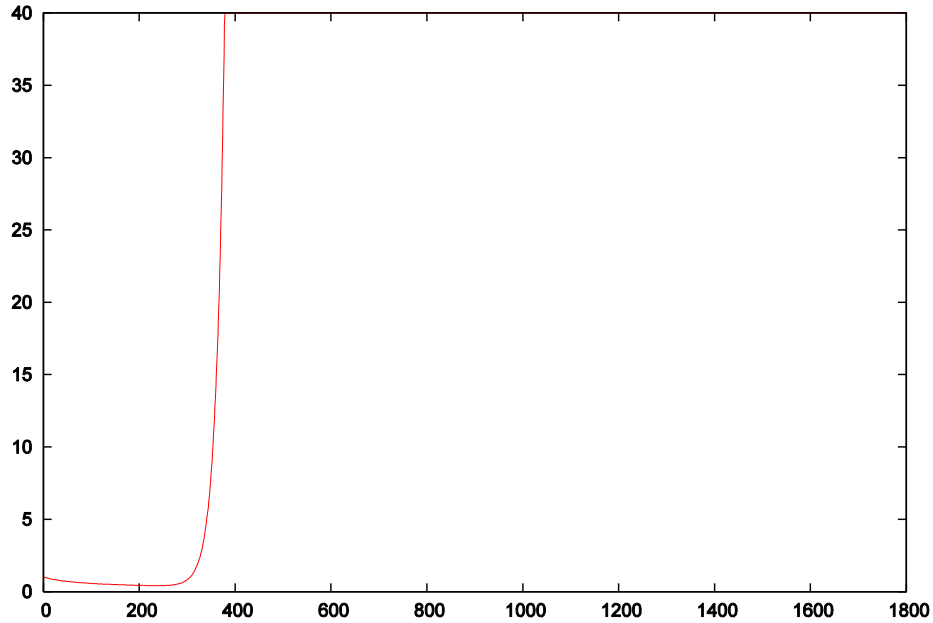
- ▶ **Equal grid boxes** and a larger time-step
- ▶ **No meridional structure** close to the poles



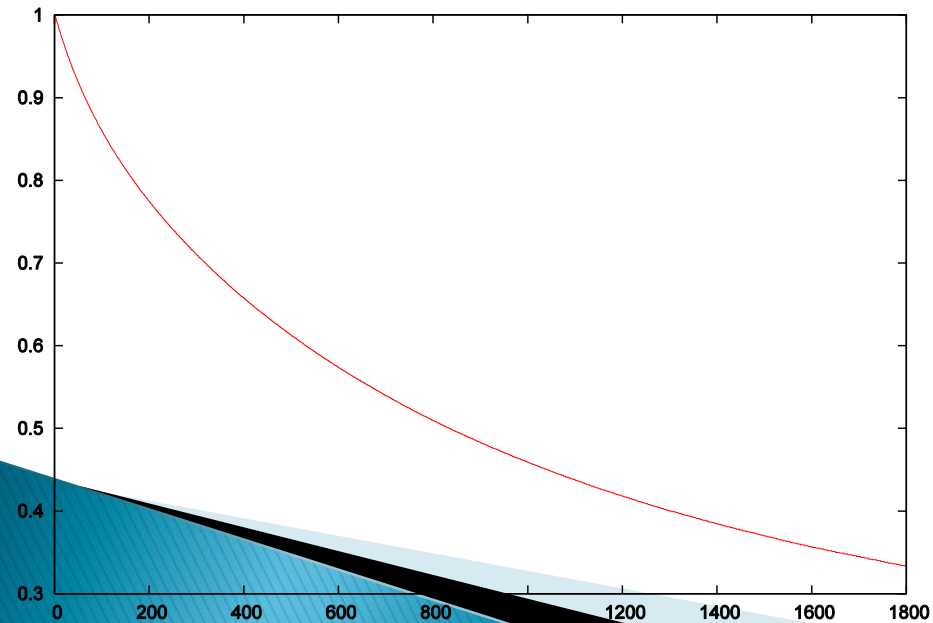
# Polar averaging

- ▶ Polar filtering through **zonal averaging** is an innovative and presumably a more efficient alternative to standard Fourier polar filtering
- ▶ The averaging as the method to increase time-step of a numerical scheme was originally suggested by Konor and Arakawa (2007)
- ▶ **Averaging coefficients** are derived by requiring that the dispersion relation for the propagation of gravity waves at a high latitude has the same stability properties as at some lower, reference latitude

Evolution of a stability measure without averaging

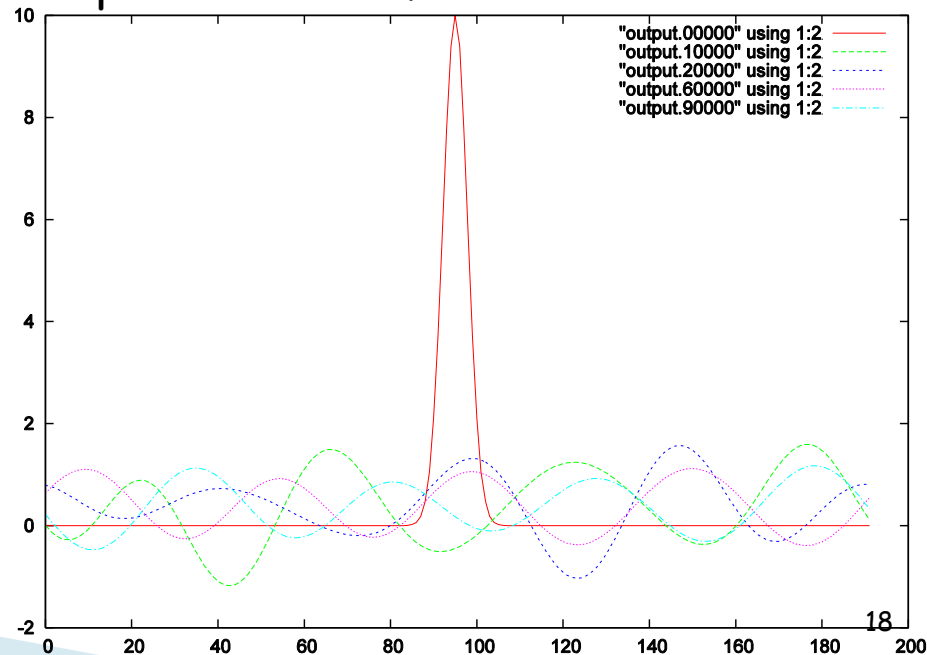


Evolution of a stability measure with averaging



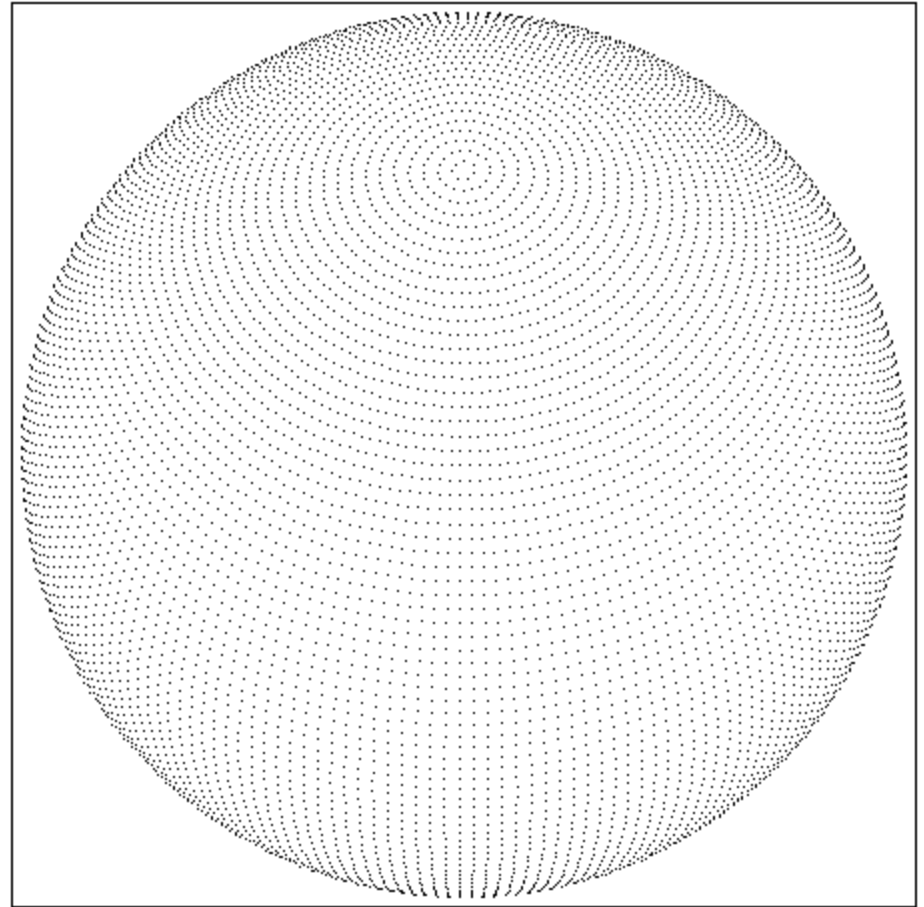
**Left panels** show evolution of a stability measure at a latitude 84.76 deg at the Gaussian T62 grid without (upper) and with (lower) polar averaging in the test of propagation of 1D gravity wave

Figure in the **right lower corner** shows propagation of the gravity wave from the panel on its left

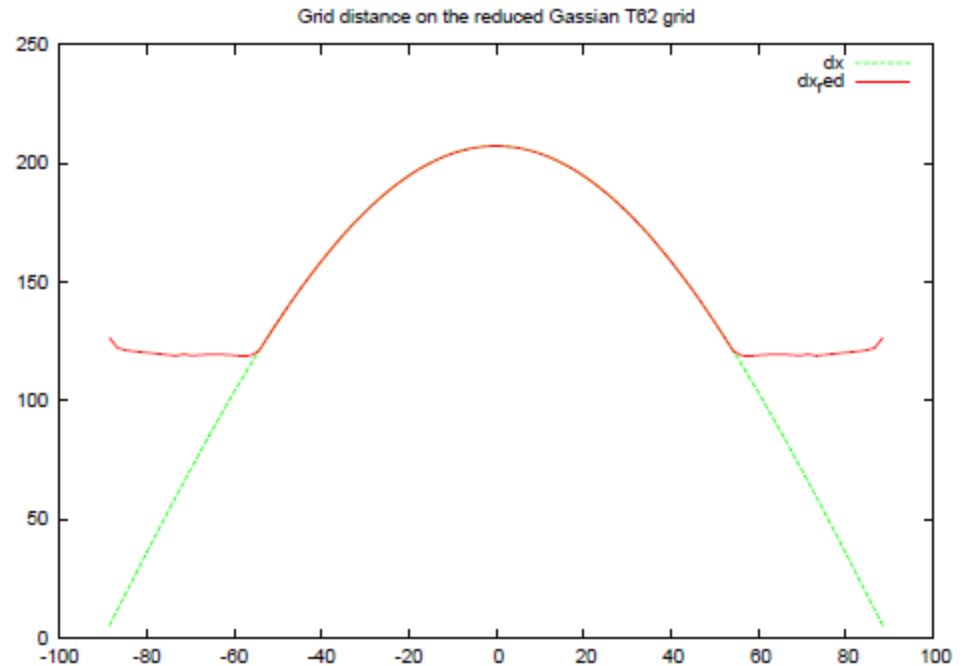


# Reduced Gaussian Grid

- ▶ Reduced grid is not used in weather prediction models because of the problems related to formulation of the **gradients in the meridional direction**
- ▶ In the short integrations of TLM and ADM **in data assimilation** we are not too concerned with the lack of formal conservation, and the reduced grid **is an acceptable and a promising choice**

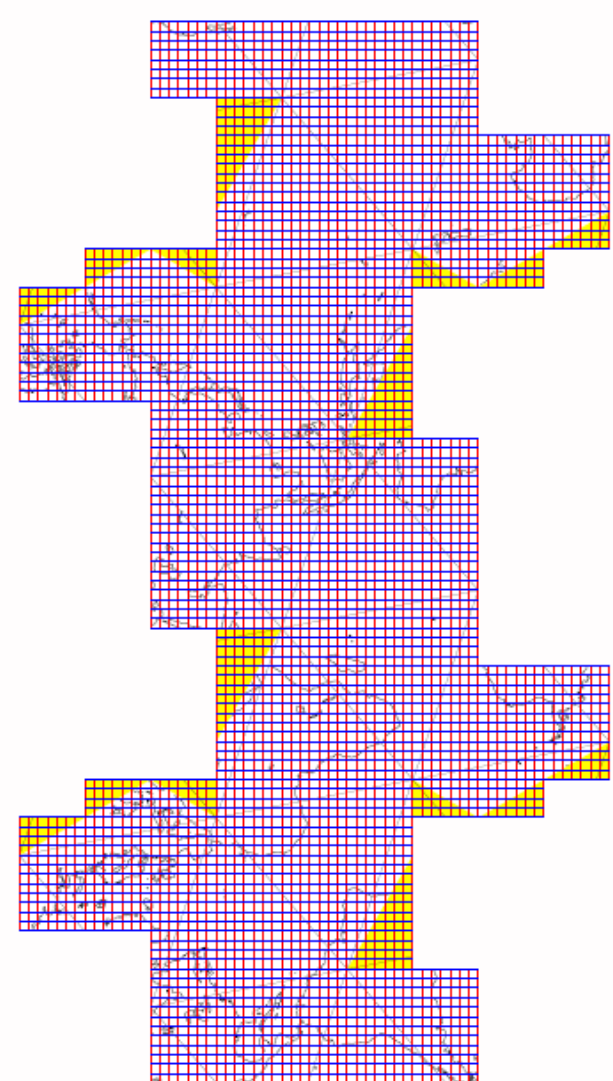


- ▶ The reduced grid has about **20% less grid points** than a full Gaussian grid
- ▶ **Aspect ratio** of the smallest to the largest time step is **0.630** on the particular grid shown on the previous slide



# Application of a quasi-uniform grid

- ▶ The idea is to cover surface of the earth **with a series of orthogonal rectangular grids** with a similar resolution, allowing a small overlapping at the edges
- ▶ This is achieved by a **modification of the mappings** between various **regular polyhedra and the sphere**
- ▶ Figure shows as an example **a regular icosahedron mapped** to the surface of the Earth using the new method



# Possible advantages of the quasi-uniform grid approach



- ▶ **Smaller number number of used grid points** than on the reduced grid
- ▶ **Larger time step**, that is, aspect ratio between the smallest and the largest time step is closer to 1
- ▶ An original **conformal mapping** (very soon)
- ▶ **More extra work !!!**





## 5. Other developments ...

- ▶ **GMAO** is using the same 4DVAR algorithm as NCEP but with a perturbation model derived by the linearization of their own atmospheric model
  - At this stage, the efficiency of GMAO's TLM and ADM of dry core appears to need further optimization
    - 7500 s for 100 iterations in the inner loop at 24 PEs
    - TLM runs about 2 times longer than NLM and ADM even 4 times on 24 PEs
- ▶ A **4-dimensional ensemble-variational method** is less affected with the efficiency problem - it is just twice as expensive as the 3D Hybrid EnKF

## ... and future work

- ▶ **Improve efficiency** and start testing 4DVAR in the cycling experiments
- ▶ **Extend physics** of the perturbation model (moist physics, more comprehensive PBL and surface exchange)
- ▶ Include capability to use **arbitrary nonlinear model** (GFS, a global NMMB - Nonhydrostatic Multiscale Model on B-grid)
- ▶ Develop a parameterized **model error** targeting a **weak 4DVAR**
- ▶ Investigate how a more realistic treatment of time dimension affects overall **performance of GSI**
- ▶ Include 4DVAR in **the regional analysis**

# Acknowledgements

- ▶ 4DVAR development at NCEP has been done through collaboration with **GMAO/NASA**, with a significant participation of **Yannick Trémolet** on the leave from **ECMWF**
- ▶ A 4-dimensional ensemble-variational method is being developed through collaboration with **Xuguang Wang** from **The University of Oklahoma**
- ▶ Overlapping quasi-uniform grids are investigated jointly with **Jim Purser** (NCEP Office Note 467 at <http://www.emc.ncep.noaa.gov/officenotes/FullTOC.html>)