



# Evolution of Finite Vorticity Strips Using a Barotropic, Non-Divergent, Pseudo-Spectral Model

M. T. Vaughan, and T. A. Guinn (Research Advisor)

Embry-Riddle Aeronautical University  
 Daytona Beach, FL

## The Model

Model based on the following momentum and mass-continuity equations in Cartesian coordinates:

$$\frac{\partial \zeta}{\partial t} + \frac{\partial(\psi, \zeta)}{\partial(x, y)} = \nu \nabla^2 \zeta - \beta \frac{\partial \psi}{\partial y} \quad (1)$$

$$\zeta = \nabla^2 \psi \quad (2)$$

## Solution Technique:

- Equations solved using spectral methods
- Method allows for efficient calculation of the derivatives
- The streamfunction  $\psi$  is used to derive the vorticity equation.

## Model Specifications:

- 6400km x 6400km doubly periodic domain
- 512 x 512 grid points
- Ordinary diffusion with e-folding time of 1 hour for waves with a total wave number of 170

## Objectives:

- Replicate the non-divergent, barotropic, pseudo-spectral model used in Schubert et al. (1999) in a MatLab environment.
- Examine the effects of finite vorticity strip length and width on the evolution of an  $f$ -plane vorticity field.
- Investigate the effects of  $\beta$  forcing on finite vorticity strips

## Cases

Case 1: 1350km x 150km ( $f$ -plane)

Case 2: 2250km x 250km ( $f$ -plane)

Case 3: 3600km x 400km ( $f$ -plane)

Case 4: 2000km x 200km ( $\beta$ -plane)

## References:

- Guinn, T.A., and W.H. Schubert, 1993: Hurricane spiral bands. *J. Atmos. Sci.*, **50**, 3380-3403.
- Schubert, W.H., et al. 1999: Polygonal eyewalls, asymmetric eye contraction, and potential vorticity mixing in hurricanes. *J. Atmos. Sci.*, **56**, 1197-1223.
- Ferreira, Rosana Nieto, Wayne H. Schubert, 1997: Barotropic Aspects of ITCZ Breakdown. *J. Atmos. Sci.*, **54**, 261-285.
- Wang, Chia-Chi, Chia Chou, Wei-Liang Lee, 2010: Breakdown and Reformation of the Intertropical Convergence Zone in a Moist Atmosphere. *J. Atmos. Sci.*, **67**, 1247-1260.
- , and G. Magnusdottir, 2005: ITCZ breakdown in three-dimensional flows. *J. Atmos. Sci.*, **62**, 1497-1512.

## Initial Vorticity Field

$$r = \begin{cases} \sqrt{a^2(|xt| - x1)^2 + (yt)^2} & \text{for } |xt| > x1 \\ |yt| & \text{otherwise,} \end{cases}$$

$$\zeta = \begin{cases} \zeta_0 & \text{if } r \leq r1 \\ \zeta_0 H(r) & \text{if } r2 > r > r1 \\ 0 & \text{if } r \geq r2 \end{cases}$$

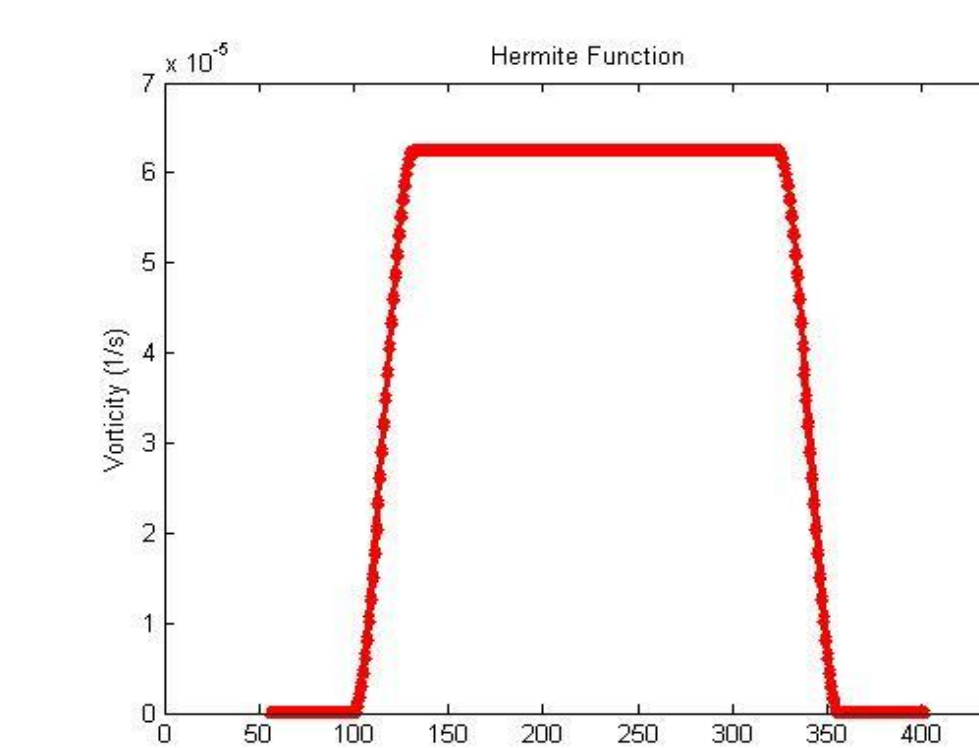
$$\text{where } H(r) = 1 - 3w^2 + 2w^3,$$

$$\text{and } w \equiv \frac{r-r1}{r2-r1}$$

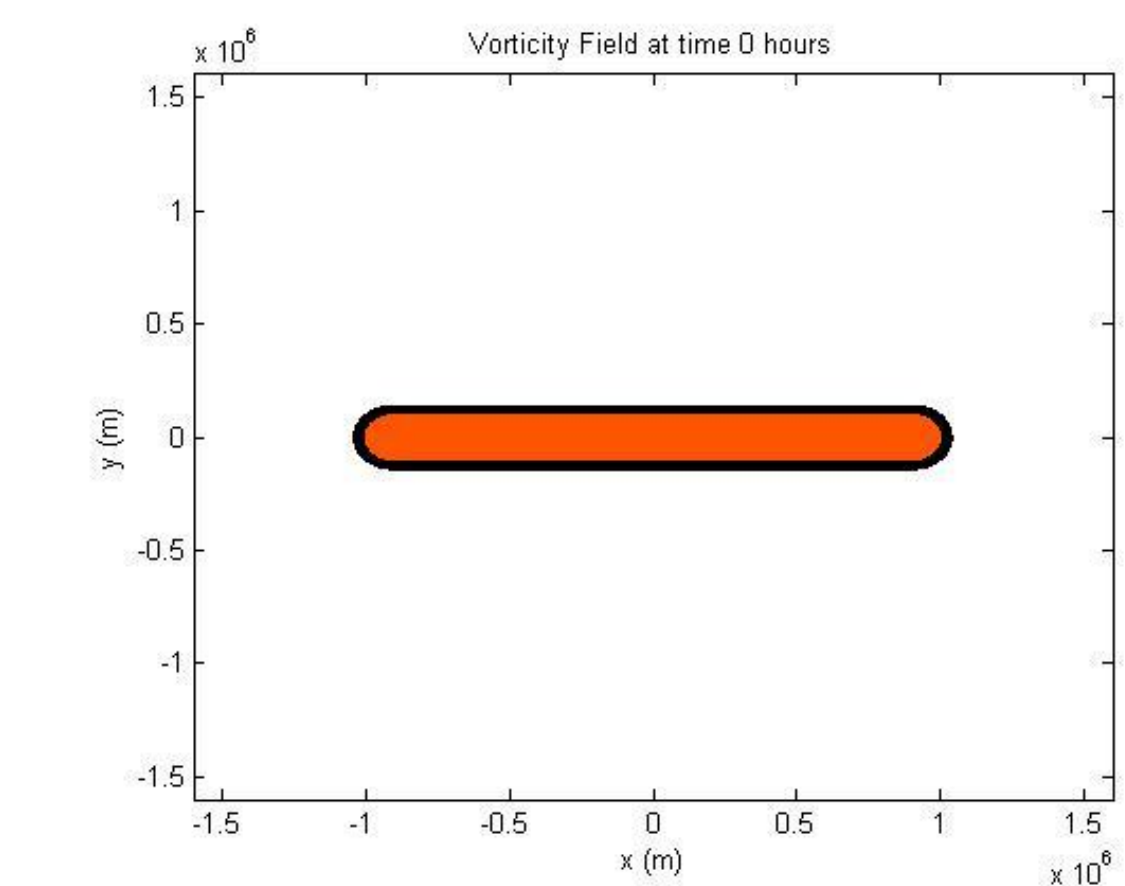
Vorticity Evolution Ratios				
Width (km)	One	Merging	Separate Centers	Independent Vortices
100	1-12	12-14	14-20	20+
150	1-9	9-11	11-14	14+
200	1-8	8-9	9-13	13+
250	1-6	6-7	7-11	11+
300	1-6	6-7	7-10	10+
400	1-6	6-7	7-9	9+

## Model Initialization

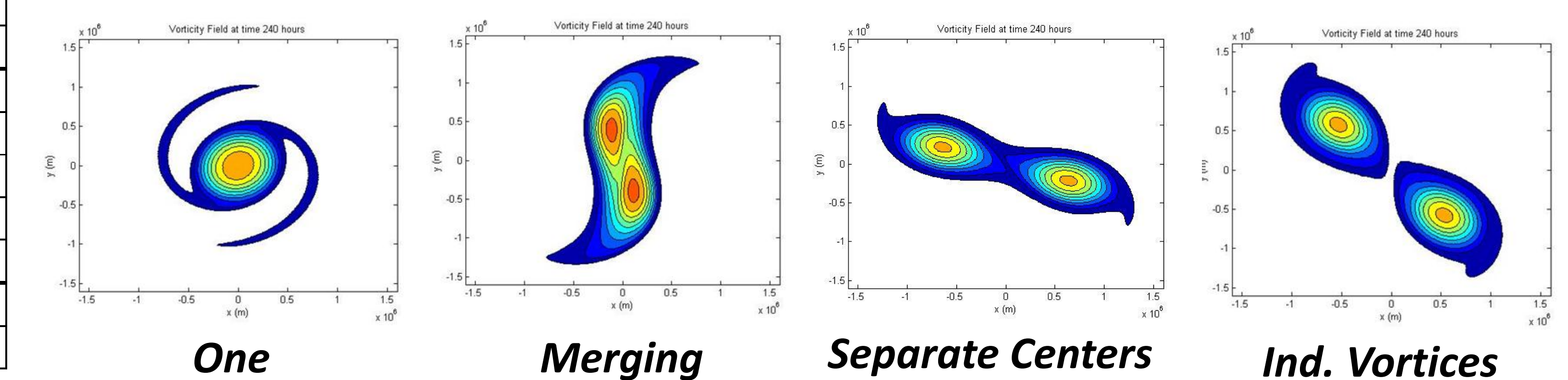
### Vorticity Cross-section



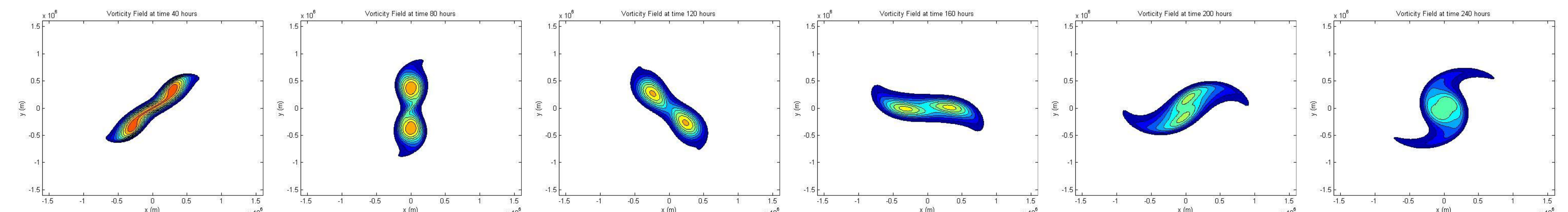
### Vorticity Plan View



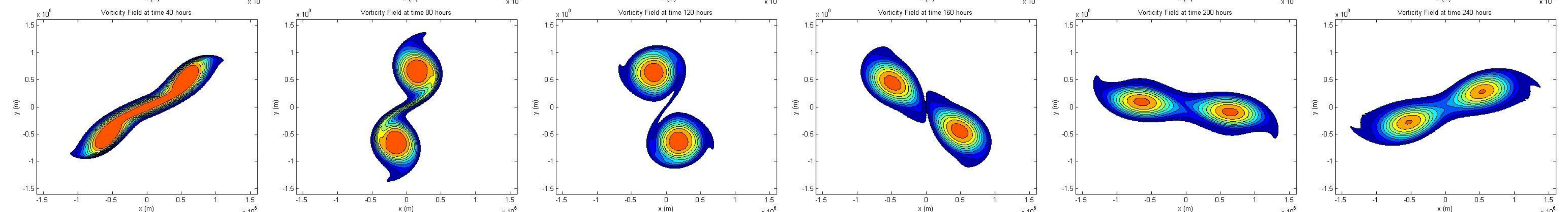
### $f$ -plane



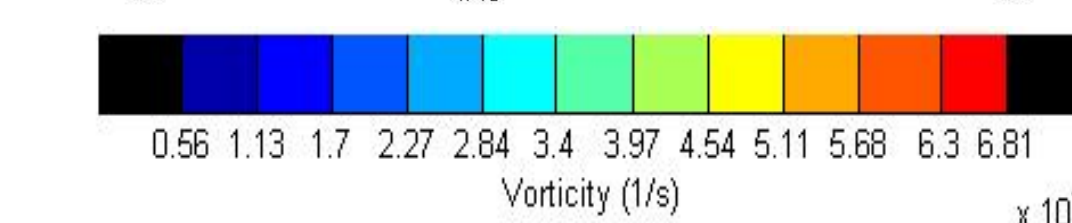
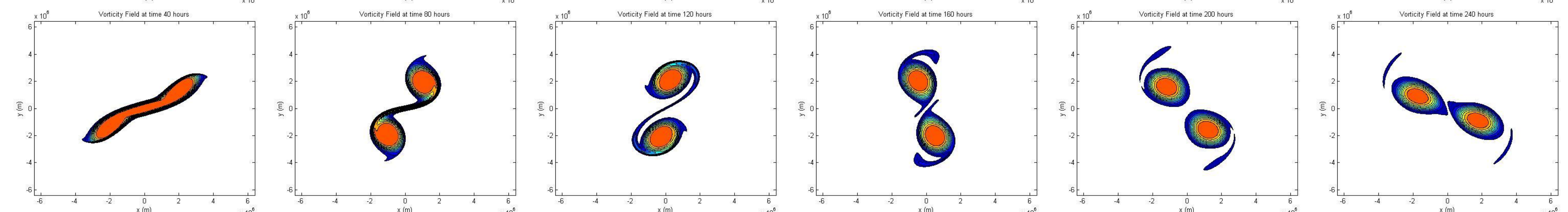
### Case 1



### Case 2



### Case 3



### $\beta$ -plane

### Case 4

