

Dependence of mean radiant temperature  
on 3D radiant flux densities:  
the example of urban quarters  
in a mid-size Central European city  
during summer heat

Helmut Mayer and Hyunjung Lee

Albert-Ludwigs-University of Freiburg, Germany



Chair of Meteorology and Climatology



- main problem for urban planning in Central European cities:  
increasing summer heat due to regional climate change  
→ to develop, apply and validate mitigation methods
- relevance for citizens by methods and results from  
urban human-biometeorology
- thermal stress for citizens  
quantified by thermal indices like PET (not  $T_a$  or UHI!)  
strongest outdoors in summer
- most crucial variable: radiant exchange in terms of  $T_{mrt}$



- numeric simulation by models, e.g.
  - SOLWEIG
  - ENVI-met
  - RayMan
- experiments
  - globe thermometer
  - **six-directional method**  
measuring short- and long wave radiant flux densities
    - from the four horizontal cardinal directions (E, S, W, N)
    - as well as from the upper and the lower hemisphere



$$T_{\text{mrt}} = \left[ \frac{S_{\text{rad}}}{\varepsilon \cdot \sigma} \right]^{0.25} - 273.15$$

$T_{\text{mrt}}$ : mean radiant temperature ( $^{\circ}\text{C}$ )

$S_{\text{rad}}$ : total of all absorbed radiant flux densities ( $\text{W m}^{-2}$ )

$\varepsilon$ : emissivity of the human body (0.97)

$\sigma$ : Stefan-Boltzmann constant ( $5.67 \cdot 10^{-8} \text{ W m}^{-2} \text{ K}^{-4}$ )



$$S_{\text{rad}} = \sum_{i=1}^6 W_i \cdot (\alpha_k \cdot K_i + \alpha_l \cdot L_i)$$

$S_{\text{rad}}$ : total of all absorbed radiant flux densities ( $\text{W m}^{-2}$ )

$K_i$ : short-wave radiant flux densities

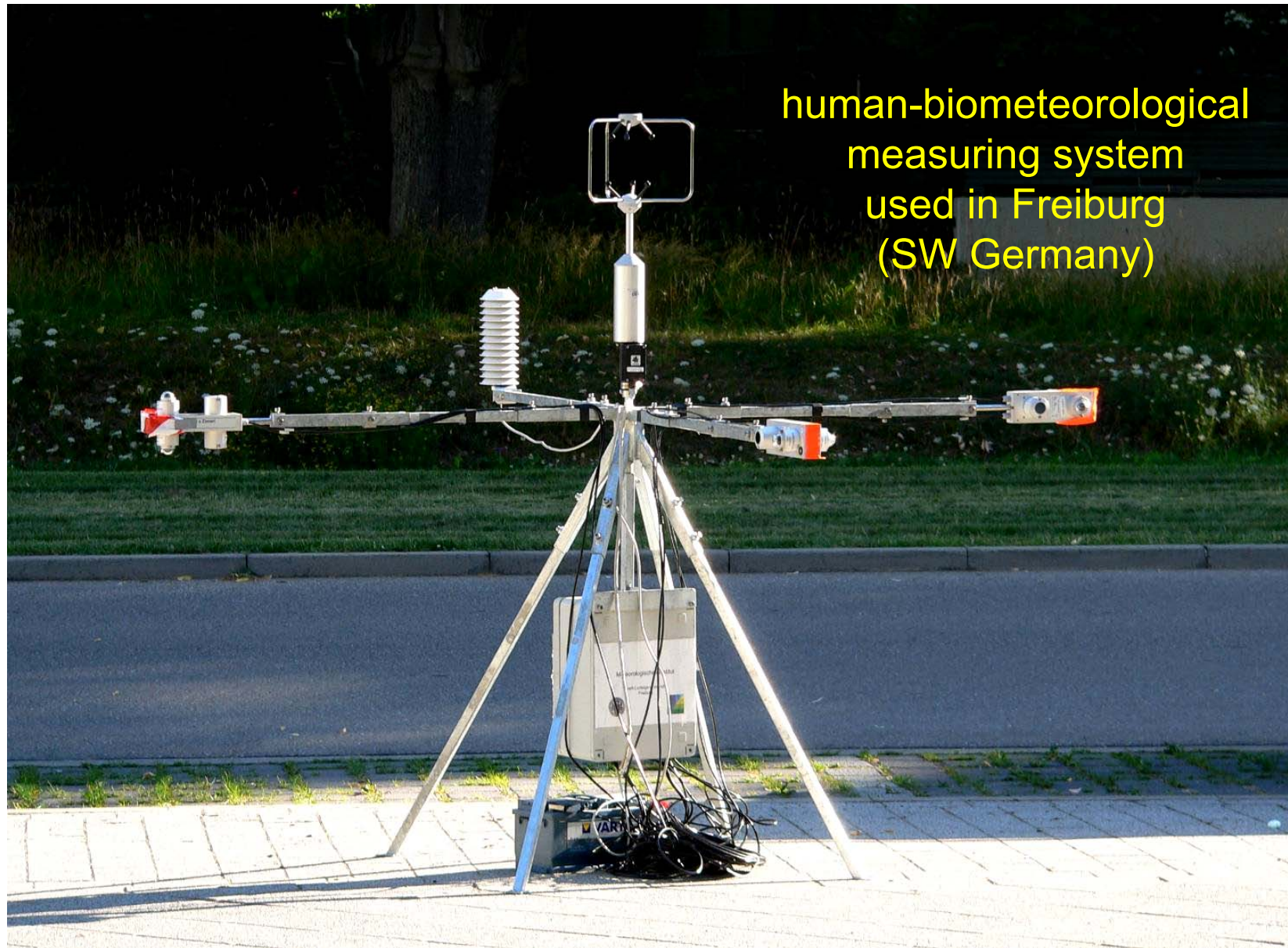
$L_i$ : long-wave radiant flux densities

$\alpha_k$ : short-wave absorption coefficient (0.7)

$\alpha_l$ : long-wave absorption coefficient (0.97)

$W_i$ : angle factors (percentage of  $K_i$  and  $L_i$ ,  
received by the human body in each direction  $i$ )

# six-directional method



human-biometeorological  
measuring system  
used in Freiburg  
(SW Germany)



- 1-d experiments (7 a.m. - 9 p.m.)
  - by use of specific human-biometeorological measuring systems
  - at 90 different sites in Freiburg (mid-size city in SW Germany) mostly street canyons of various designs
  - during typical Central European summer weather
  - from 2007-2010
- results are aggregated to mean values over 10-16 CET typical timescale for daytime heat in Central European cities

# results (I)



- linear regressions:  $y = a \cdot x + b$   
x: sky view factor for the  
southern part of the upper half space ( $SVF_{90-270}$ )

<b>y</b>	<b>x</b>	<b>R<sup>2</sup></b>
$T_a$ (°C)	$SVF_{90-270}$ (%)	0.002
$T_{mrt}$ (°C)	$SVF_{90-270}$ (%)	<b>0.774</b>
PET (°C)	$SVF_{90-270}$ (%)	0.332



## results (II)



- linear regressions:  $y = a \cdot x + b$   
x: short-wave radiant flux densities  
absorbed by the human-biometeorological reference person

<b>y</b>	<b>x</b>	<b>R<sup>2</sup></b>
$T_{\text{mrt}}$ (°C)	$K_{\downarrow, \text{abs}}$ (W/m <sup>2</sup> )	0.898
$T_{\text{mrt}}$ (°C)	$K_{\text{hor,abs}}$ (W/m <sup>2</sup> )	0.900
$T_{\text{mrt}}$ (°C)	$K_{\text{vert,abs}}$ (W/m <sup>2</sup> )	0.902
$T_{\text{mrt}}$ (°C)	$K^*_{\text{abs}}$ (W/m <sup>2</sup> )	<b>0.910</b>

## results (III)



- linear regressions:  $y = a \cdot x + b$

x: long-wave radiant flux densities

absorbed by the human-biometeorological reference person

<b>y</b>	<b>x</b>	<b>R<sup>2</sup></b>
$T_{\text{mrt}} \text{ (}^\circ\text{C)}$	$L_{\downarrow\text{abs}} \text{ (W/m}^2\text{)}$	0.021
$T_{\text{mrt}} \text{ (}^\circ\text{C)}$	$L_{\uparrow\text{abs}} \text{ (W/m}^2\text{)}$	<b>0.755</b>
$T_{\text{mrt}} \text{ (}^\circ\text{C)}$	$L_{\text{hor,abs}} \text{ (W/m}^2\text{)}$	0.400
$T_{\text{mrt}} \text{ (}^\circ\text{C)}$	$L_{\text{vert,abs}} \text{ (W/m}^2\text{)}$	0.391
$T_{\text{mrt}} \text{ (}^\circ\text{C)}$	$L^*_{\text{abs}} \text{ (W/m}^2\text{)}$	0.402



- linear regressions:  $y = a \cdot x + b$ 
  - $y: T_a, T_{\text{mrt}}, \text{PET}$  (averaged over 10-16 CET)  
 $x = \text{SVF}_{90-270}$   
→ highest  $R^2$  (0.774) for  $y = T_{\text{mrt}}$
  - $y = T_{\text{mrt}}$  (10-16 CET)  
 $x: \text{absorbed short-wave radiant flux densities}$  (10-16 CET)  
→ highest  $R^2$  (0.910) for  $x = K_{\text{abs}}^*$
  - $y = T_{\text{mrt}}$  (10-16 CET)  
 $x: \text{absorbed long-wave radiant flux densities}$  (10-16 CET)  
→ highest  $R^2$  (0.755) for  $x = L_{\text{abs}}^{\uparrow}$



- linear regressions:  $T_{\text{mrt}} = a \cdot x + b$ 
  - higher  $R^2$  values for different  $K_{\text{abs}}$  flux densities (x)  
in contrast to different  $L_{\text{abs}}$  flux densities (x)

- multiple regression:

$$T_{\text{mrt}} = 0.113 \cdot K_{\text{abs}}^* + 1.535 \cdot L_{\text{abs}} - 12.6$$

$$\rightarrow R^2 = 0.977$$



- linear regressions:  $T_{\text{mrt}} = a \cdot x + b$ 
  - higher  $R^2$  values for different  $K_{\text{abs}}$  flux densities (x)  
in contrast to different  $L_{\text{abs}}$  flux densities (x)

- multiple regression:

$$T_{\text{mrt}} = 0.113 \cdot K_{\text{abs}}^* + 1.535 \cdot L_{\text{abs}}^{\uparrow} - 12.6$$

$$\rightarrow R^2 = 0.977$$

$$T_{\text{mrt}} = 0.661 \cdot K_{\text{abs}}^{\downarrow} + 1.359 \cdot L_{\text{abs}}^{\uparrow} - 6.7$$

$$\rightarrow R^2 = 0.941$$

$T_{\text{mrt}}$  (°C);  $K_{\text{abs}}^{\downarrow}$ ,  $K_{\text{abs}}^*$ ,  $L_{\text{abs}}^{\uparrow}$  (W/m<sup>2</sup>): mean values over 10-16 CET



Thank you for  
your attention

