



A cross-spectral approach to assessing the performance of hydrological models: observed v modelled daily discharge of the River Thames, UK

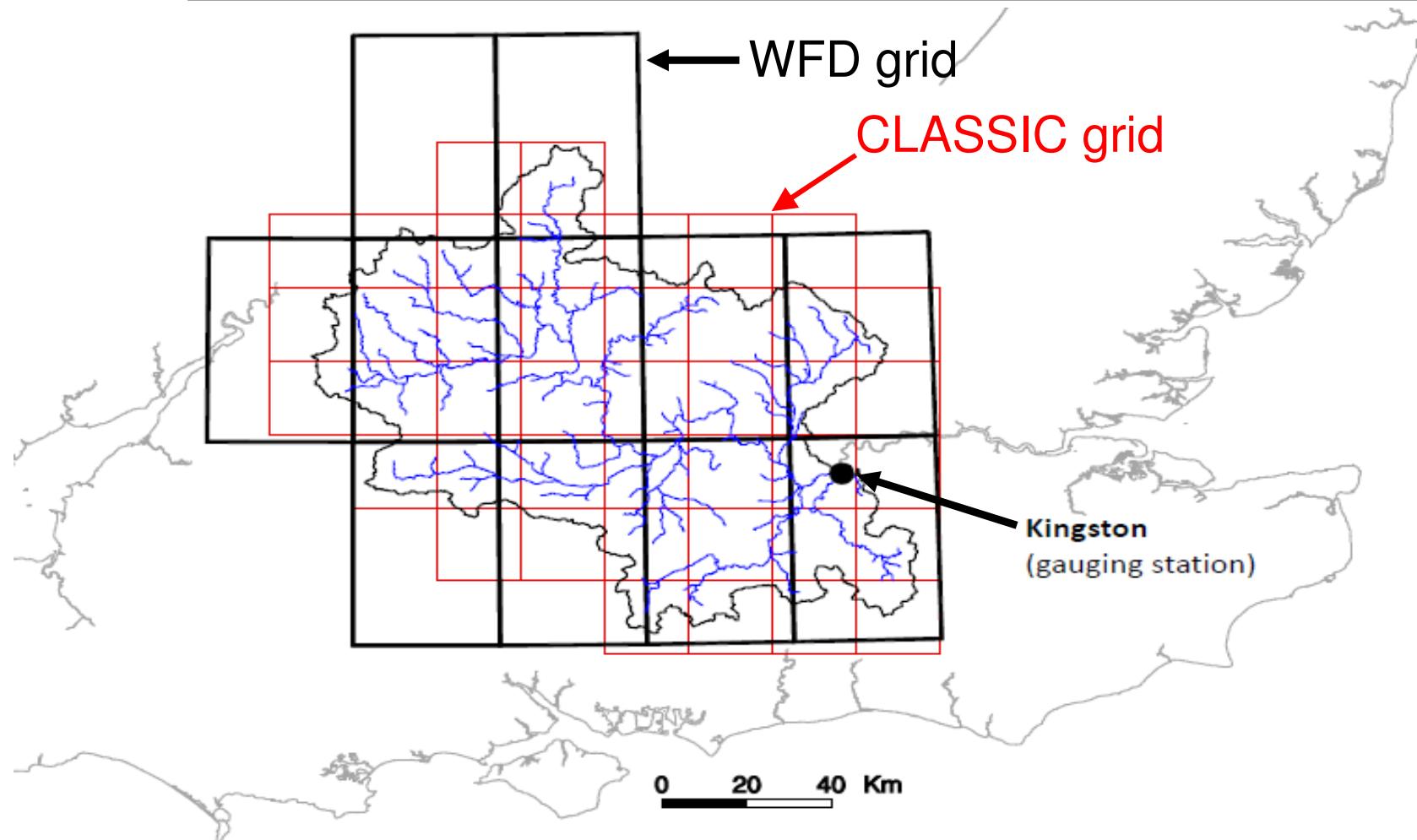
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AMS annual meeting, Atlanta. February 2014

¹Met Office, ²Centre for Ecology and Hydrology

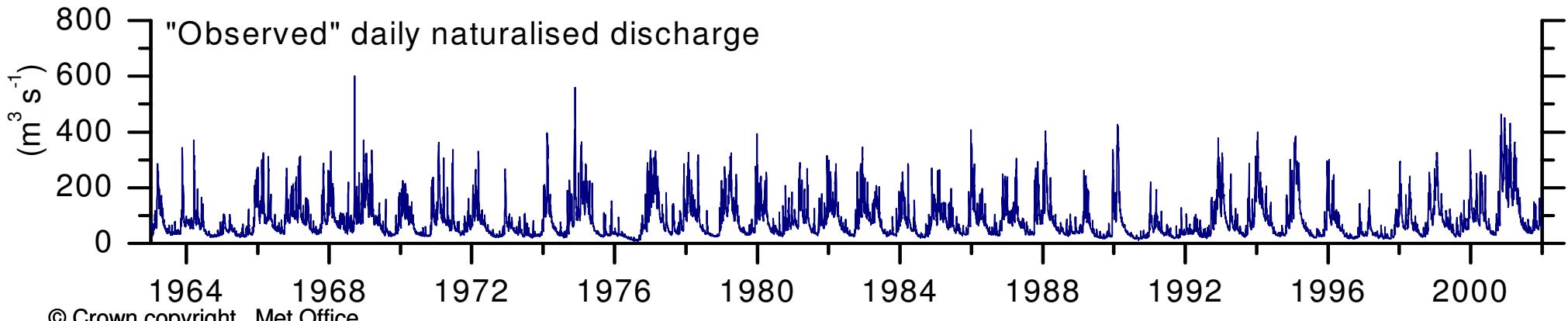
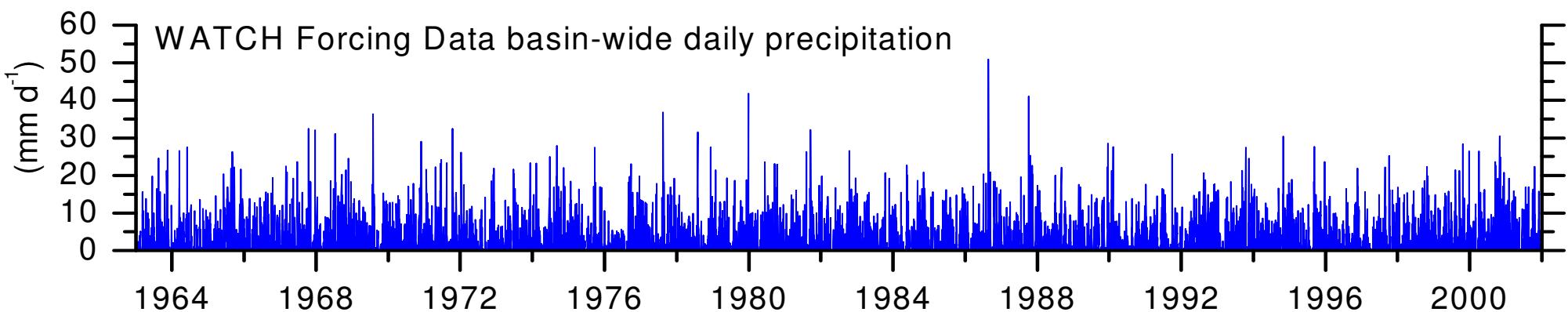
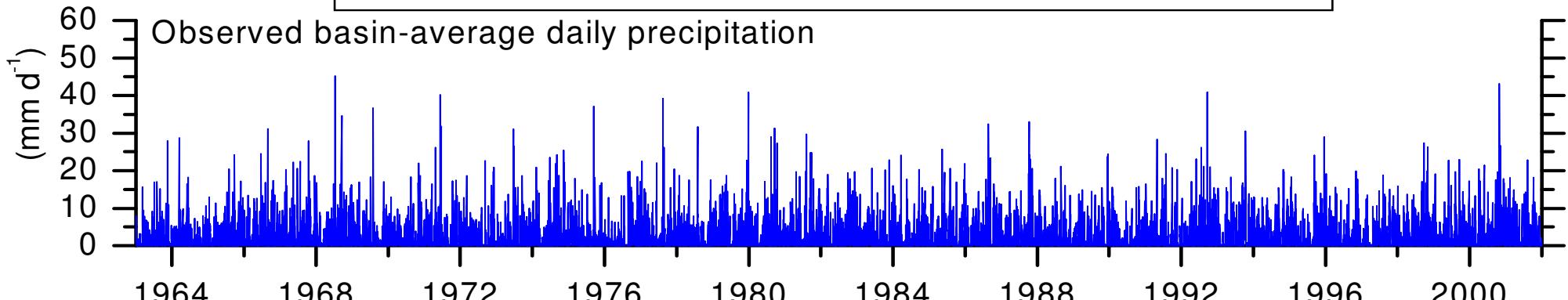
Modelling the Thames Basin

Model type	Models	(* = Calibrated)
RBM =	CLASSIC*	
GHM =	WaterGAP*, MPI-HM, LPJml, GWAVA	
LSM =	MATSIRO, JULES, H08, Orchidee	

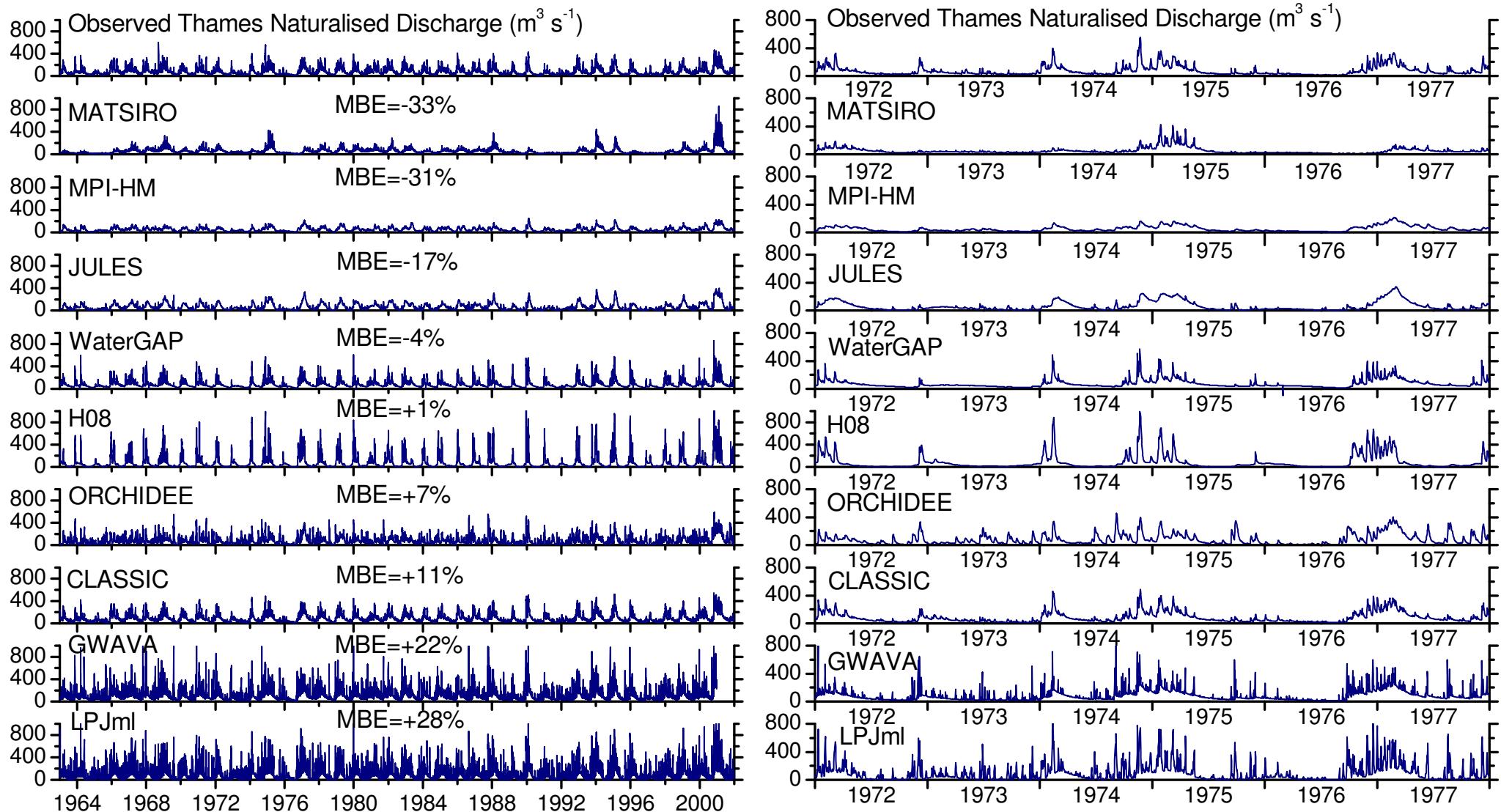




Precip. Observed Mean = 1.97 +/-0.06mm STDev = 3.68mm
Precip. WFD Mean = 1.99 +/-0.06mm STDev = 3.79mm
Correlation (Pearson's r) = 0.635 (P<0.001) MAE = 1.57mm



Observed and modelled time series of daily discharge





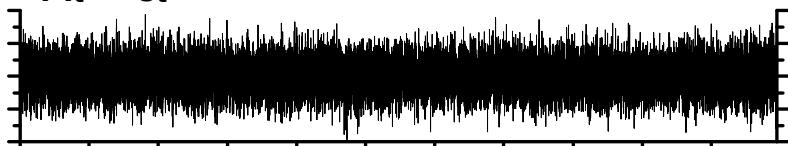
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Standard Noise Models

Time series

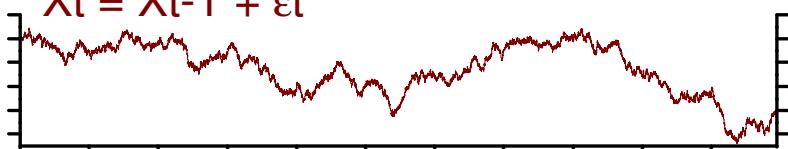
Random numbers or **White Noise**

$$X_t = \varepsilon_t$$



Random walk or **Brown Noise**

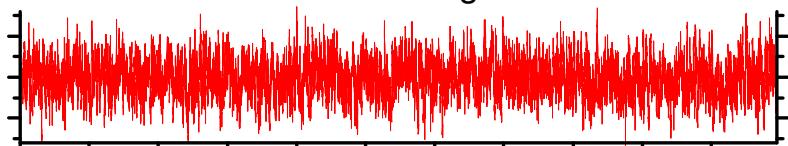
$$X_t = X_{t-1} + \varepsilon_t$$



Autoregression, AR1 Noise or **Red Noise**

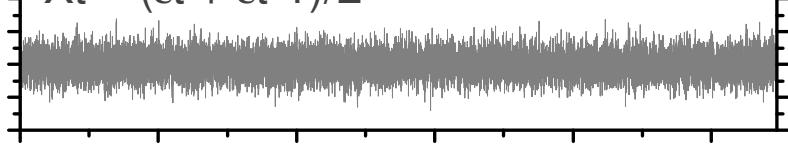
$$X_t = \rho_1 X_{t-1} + \varepsilon_t \quad (0.0 \geq \rho_1 \geq 1.0)$$

Lag-1 auto-correlation

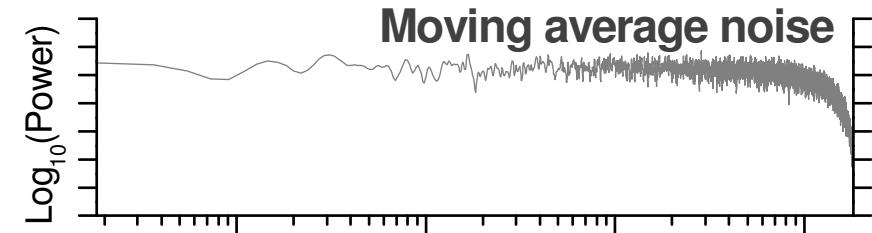
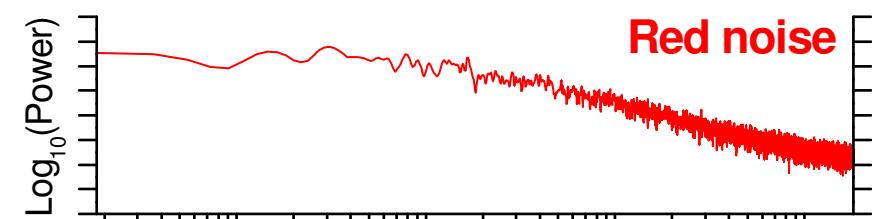
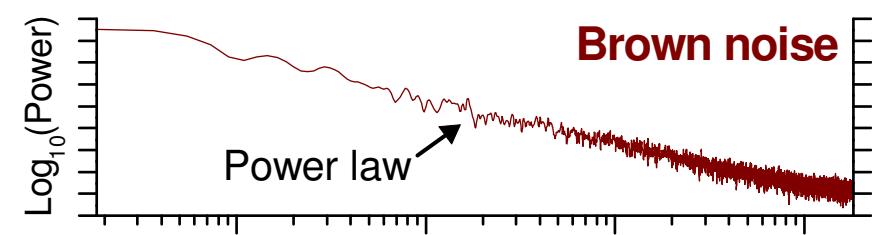
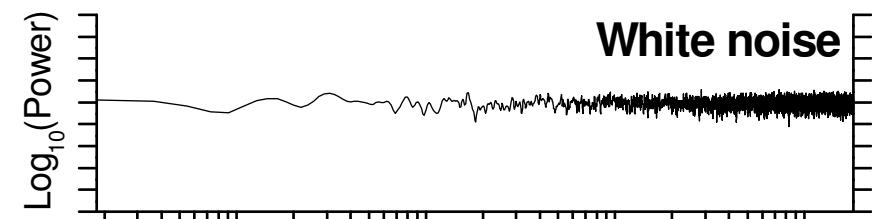


Moving average Noise

$$X_t = (\varepsilon_t + \varepsilon_{t-1})/2$$



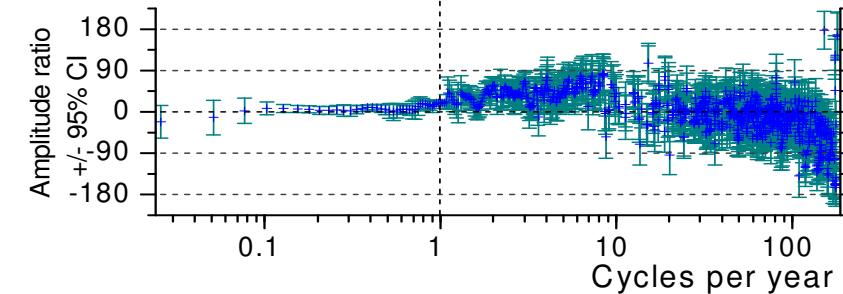
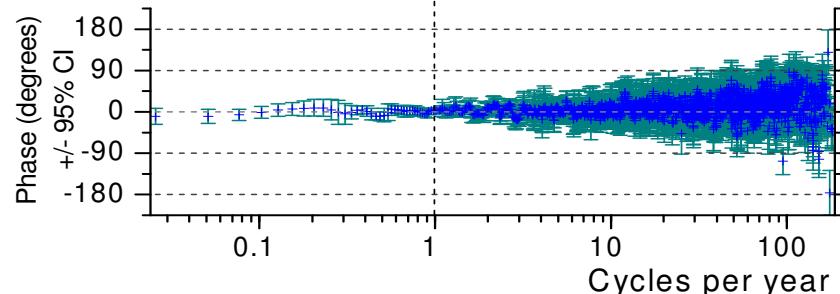
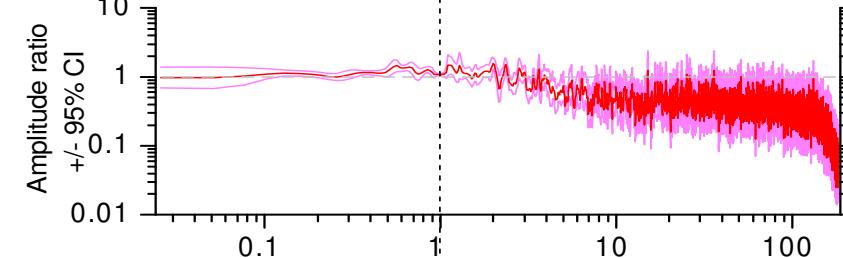
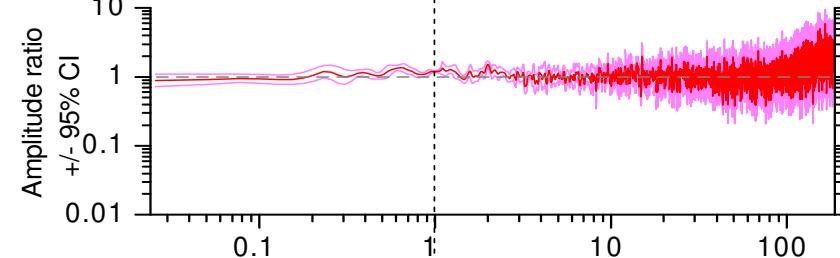
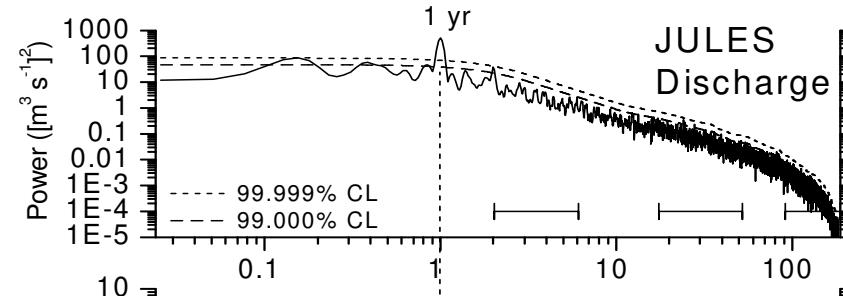
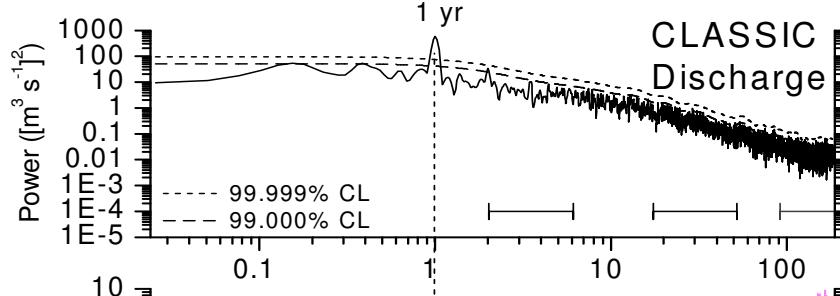
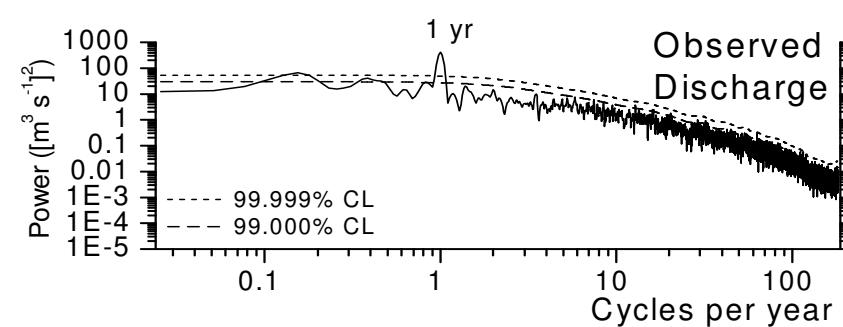
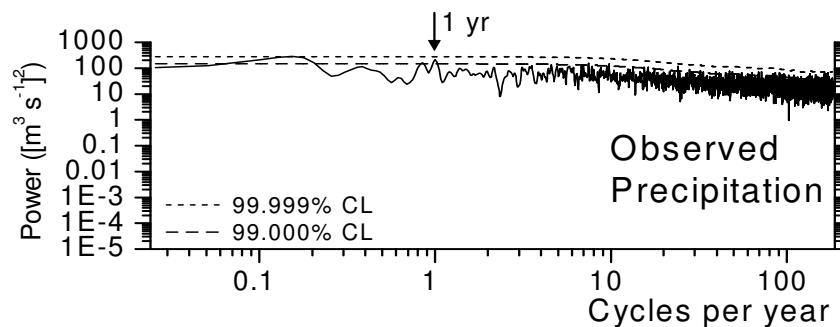
Power spectra





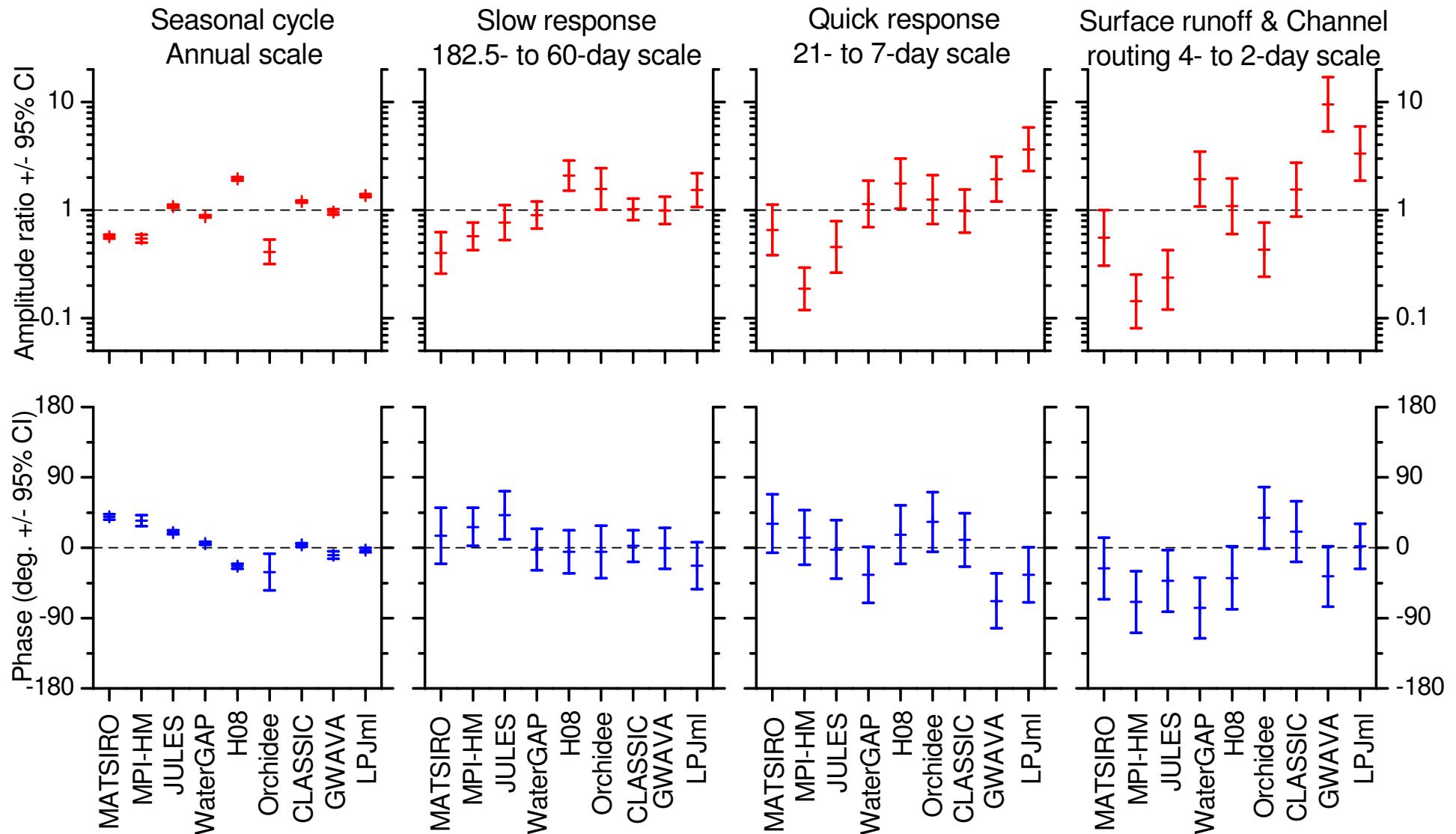
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Thames Basin Discharge Spectra

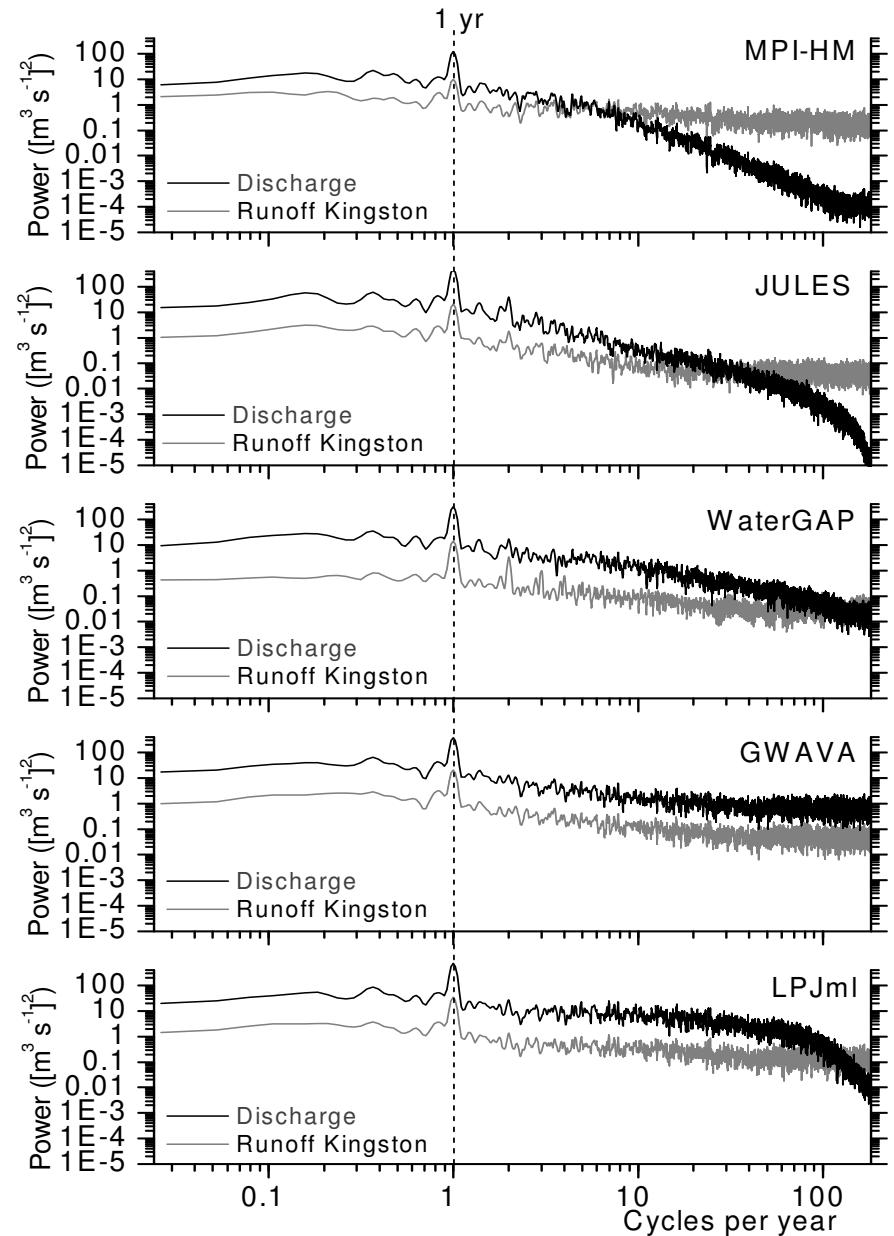
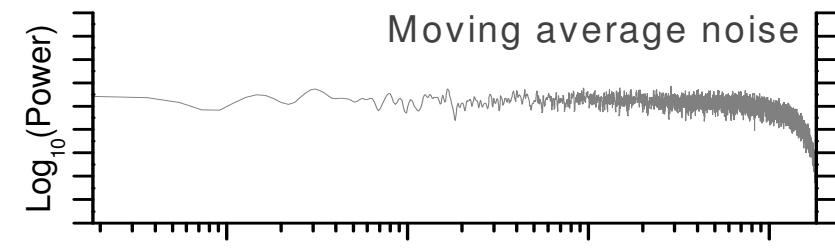
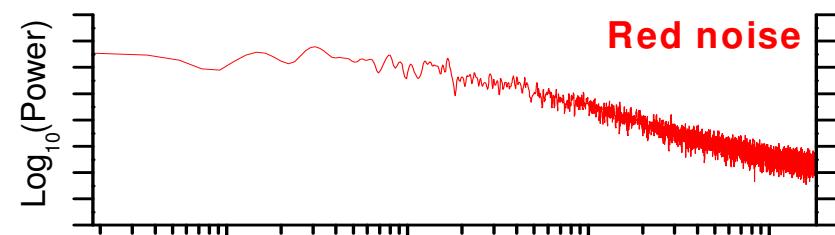
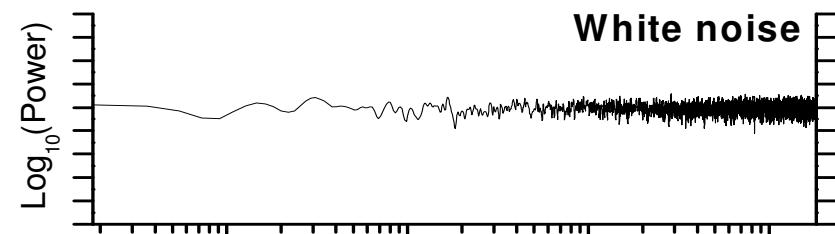
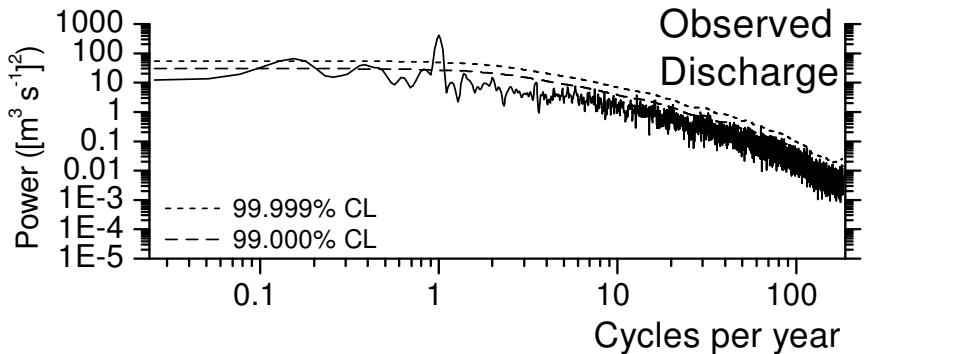




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Power Spectra of Modelled Runoff & Discharge





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Conclusions

- Cross-spectral analysis is a valuable technique to help understand model performance
- Can study model's response at different ranges of frequencies related to physical processes
- Observations indicate that the physical processes in the Thames Basin convert rainfall variability to river discharge variability by adding “short term” memory
- Within distributed hydrological models this memory is introduced at the river routing stage rather than during runoff generation
- Some routing schemes introduce smoothing at high frequencies due to a moving average
- Numerical coupling within models can lead to un-physical responses – e.g. short term output variations leading inputs
- Weedon et al., submitted to *J. Hydrometeorol.*