

14.5 How Should a Numerical Weather Prediction (NWP) Model Forecast be made: Full Field or Anomaly?

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Basic idea

- Any variable can be decomposed into a long-term average (“climate”) and a departure (“anomaly”)
- Climate (known) can be pre-calculated using historical data such as reanalysis and doesn’t need to be predicted, only anomalies need to be predicted
- Therefore, if a model only predicts anomalies but not climate part, total forecast error might be dramatically reduced given erroneous “model climate”

Variables decomposition (Qian, Du and Ai, 2021, *BAMS*)

“anomaly = total field – climate”

$$u'(\lambda, \varphi, z, t) = u(\lambda, \varphi, z, t) - \tilde{u}(\lambda, \varphi, z, t)$$

$$v'(\lambda, \varphi, z, t) = v(\lambda, \varphi, z, t) - \tilde{v}(\lambda, \varphi, z, t)$$

$$w'(\lambda, \varphi, z, t) = w(\lambda, \varphi, z, t) - \tilde{w}(\lambda, \varphi, z, t)$$

$$\pi'(\lambda, \varphi, z, t) = \pi(\lambda, \varphi, z, t) - \tilde{\pi}(\lambda, \varphi, z, t)$$

$$\theta'(\lambda, \varphi, z, t) = \theta(\lambda, \varphi, z, t) - \tilde{\theta}(\lambda, \varphi, z, t)$$

$$T'(\lambda, \varphi, z, t) = T(\lambda, \varphi, z, t) - \tilde{T}(\lambda, \varphi, z, t)$$

$$q'(\lambda, \varphi, z, t) = q(\lambda, \varphi, z, t) - \tilde{q}(\lambda, \varphi, z, t)$$

Anomaly form of atmospheric governing equations (Qian and Du 2022, *Meteor.*)

$$\begin{aligned}\frac{du'}{dt} &= \frac{\partial u'}{\partial t} + \frac{u}{a \cos \varphi} \frac{\partial u'}{\partial \lambda} + \frac{v}{a} \frac{\partial u'}{\partial \varphi} + w \frac{\partial u'}{\partial z} = \frac{\partial u'}{\partial t} + \frac{\tilde{u} + u'}{a \cos \varphi} \frac{\partial u'}{\partial \lambda} + \frac{\tilde{v} + v'}{a} \frac{\partial u'}{\partial \varphi} + (\tilde{w} + w') \frac{\partial u'}{\partial z} \\ &= -\frac{C_p \theta'}{a \cos \varphi} \frac{\partial \pi'}{\partial \lambda} - \frac{C_p \tilde{\theta}}{a \cos \varphi} \frac{\partial \pi'}{\partial \lambda} - \frac{C_p \theta'}{a \cos \varphi} \frac{\partial \tilde{\pi}}{\partial \lambda} - \frac{u'}{a \cos \varphi} \frac{\partial \tilde{u}}{\partial \lambda} - v' \frac{\partial \tilde{u}}{a \partial \varphi} - w' \frac{\partial \tilde{u}}{\partial z} + f v' + F_u\end{aligned}$$

$$\begin{aligned}\frac{dv'}{dt} &= \frac{\partial v'}{\partial t} + \frac{u}{a \cos \varphi} \frac{\partial v'}{\partial \lambda} + \frac{v}{a} \frac{\partial v'}{\partial \varphi} + w \frac{\partial v'}{\partial z} = \frac{\partial v'}{\partial t} + \frac{\tilde{u} + u'}{a \cos \varphi} \frac{\partial v'}{\partial \lambda} + \frac{\tilde{v} + v'}{a} \frac{\partial v'}{\partial \varphi} + (\tilde{w} + w') \frac{\partial v'}{\partial z} \\ &= -\frac{C_p \theta'}{a} \frac{\partial \pi'}{\partial \varphi} - \frac{C_p \tilde{\theta}}{a} \frac{\partial \pi'}{\partial \varphi} - \frac{C_p \theta'}{a} \frac{\partial \tilde{\pi}}{\partial \varphi} - \frac{u'}{a \cos \varphi} \frac{\partial \tilde{v}}{\partial \lambda} - v' \frac{\partial \tilde{v}}{a \partial \varphi} - w' \frac{\partial \tilde{v}}{\partial z} - f u' + F_v\end{aligned}$$

$$\begin{aligned}\frac{dw'}{dt} &= \frac{\partial w'}{\partial t} + \frac{u}{a \cos \varphi} \frac{\partial w'}{\partial \lambda} + \frac{v}{a} \frac{\partial w'}{\partial \varphi} + w \frac{\partial w'}{\partial z} = \frac{\partial w'}{\partial t} + \frac{\tilde{u} + u'}{a \cos \varphi} \frac{\partial w'}{\partial \lambda} + \frac{\tilde{v} + v'}{a} \frac{\partial w'}{\partial \varphi} + (\tilde{w} + w') \frac{\partial w'}{\partial z} \\ &= -C_p \theta' \frac{\partial \pi'}{\partial z} - C_p \tilde{\theta} \frac{\partial \pi'}{\partial z} - C_p \theta' \frac{\partial \tilde{\pi}}{\partial z} - \frac{u'}{a \cos \varphi} \frac{\partial \tilde{w}}{\partial \lambda} - v' \frac{\partial \tilde{w}}{a \partial \varphi} - w' \frac{\partial \tilde{w}}{\partial z} + F_w\end{aligned}$$

$$\begin{aligned}\frac{d\pi'}{dt} &= \frac{\partial \pi'}{\partial t} + \frac{u}{a \cos \varphi} \frac{\partial \pi'}{\partial \lambda} + \frac{v}{a} \frac{\partial \pi'}{\partial \varphi} + w \frac{\partial \pi'}{\partial z} = \frac{\partial \pi'}{\partial t} + \frac{\tilde{u} + u'}{a \cos \varphi} \frac{\partial \pi'}{\partial \lambda} + \frac{\tilde{v} + v'}{a} \frac{\partial \pi'}{\partial \varphi} \\ &= -\frac{1}{(\gamma - 1)} \pi' \cdot D'_3 - \frac{1}{(\gamma - 1)} \tilde{\pi} \cdot D'_3 - \frac{1}{(\gamma - 1)} \pi' \cdot \tilde{D}_3 + \frac{1}{(\gamma - 1)} \frac{F_{\tilde{\theta}}}{\tilde{\theta} + \theta'} - \frac{1}{(\gamma - 1)} \frac{F_{\tilde{\theta}}}{\tilde{\theta}} + \frac{1}{(\gamma - 1)} \frac{F_{\theta'}}{\tilde{\theta} + \theta'} \\ &\quad - \frac{u'}{a \cos \varphi} \frac{\partial \tilde{\pi}}{\partial \lambda} - v' \frac{\partial \tilde{\pi}}{a \partial \varphi} - w' \frac{\partial \tilde{\pi}}{\partial z}\end{aligned}$$

$$\begin{aligned}\frac{d\theta'}{dt} &= \frac{\partial \theta'}{\partial t} + \frac{u}{a \cos \varphi} \frac{\partial \theta'}{\partial \lambda} + \frac{v}{a} \frac{\partial \theta'}{\partial \varphi} + w \frac{\partial \theta'}{\partial z} = \frac{\partial \theta'}{\partial t} + \frac{\tilde{u} + u'}{a \cos \varphi} \frac{\partial \theta'}{\partial \lambda} + \frac{\tilde{v} + v'}{a} \frac{\partial \theta'}{\partial \varphi} + (\tilde{w} + w') \frac{\partial \theta'}{\partial z} \\ &= \frac{F_{\tilde{\theta}}}{\tilde{\pi} + \pi'} - \frac{F_{\tilde{\theta}}}{\tilde{\pi}} + \frac{F_{\theta'}}{\tilde{\pi} + \pi'} - \frac{u'}{a \cos \varphi} \frac{\partial \tilde{\theta}}{\partial \lambda} - v' \frac{\partial \tilde{\theta}}{a \partial \varphi} - w' \frac{\partial \tilde{\theta}}{\partial z}\end{aligned}$$

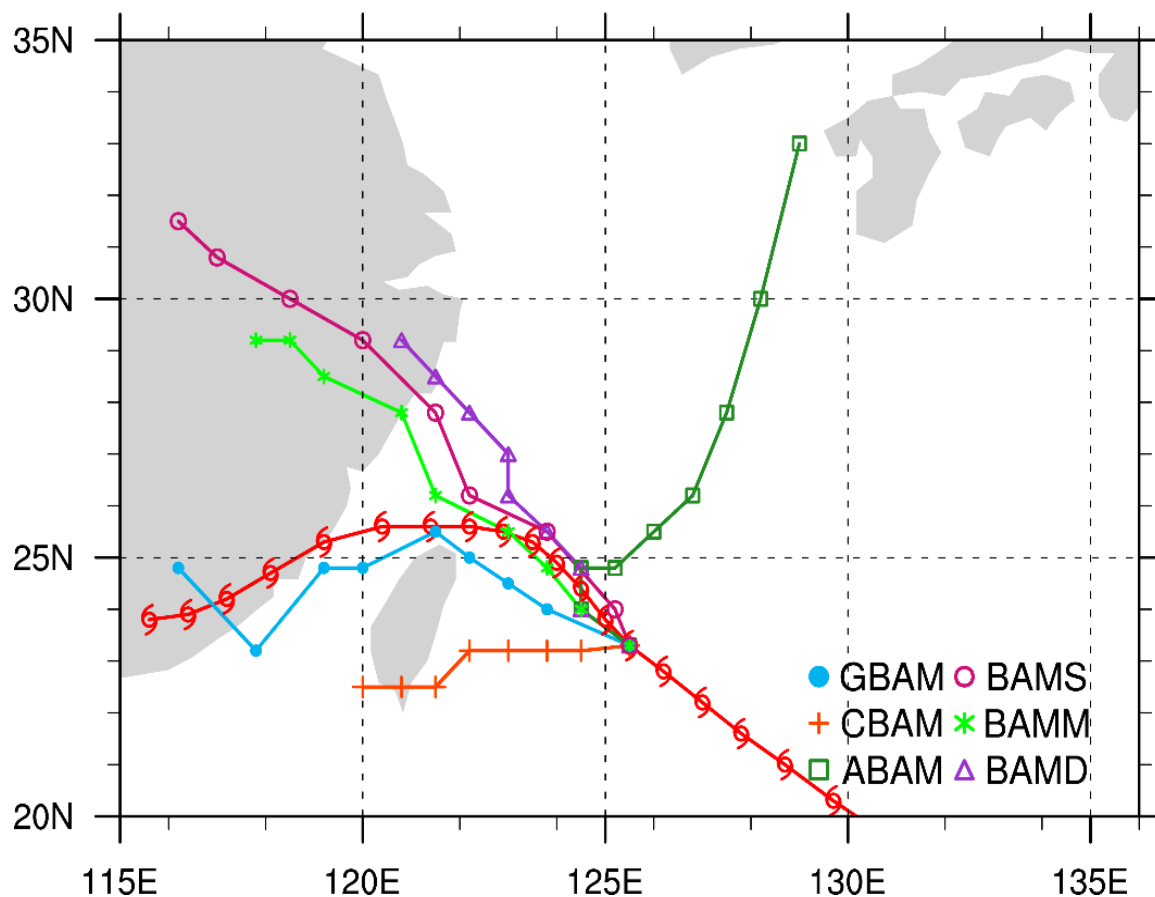
$$T' = \pi' \theta' + \tilde{\pi} \theta' + \pi' \tilde{\theta}$$

$$\frac{\partial q'}{\partial t} = -\left[u' \frac{\partial q'}{\partial x} + v' \frac{\partial q'}{\partial y} + w' \frac{\partial q'}{\partial z}\right] - \left[u' \frac{\partial \tilde{q}}{\partial x} + v' \frac{\partial \tilde{q}}{\partial y} + w' \frac{\partial \tilde{q}}{\partial z}\right] - \left[\tilde{u} \frac{\partial q'}{\partial x} + \tilde{v} \frac{\partial q'}{\partial y} + \tilde{w} \frac{\partial q'}{\partial z}\right] + Q'_{source} - Q'_{sink}$$

The 48h track forecasts of Typhoon Aere, initiated at 0600 UTC 23 August 2004

$$\frac{\partial \zeta}{\partial t} = -u \frac{\partial \zeta}{\partial x} - v \frac{\partial \zeta}{\partial y} - \beta v \quad (\text{full-field BAM}) \quad (1)$$

$$\frac{\partial \zeta'}{\partial t} = -[(\tilde{u} + u') \frac{\partial \zeta'}{\partial x} + (\tilde{v} + v') \frac{\partial \zeta'}{\partial y}] - \beta v' \quad (\text{anomaly GBAM}) \quad (2)$$



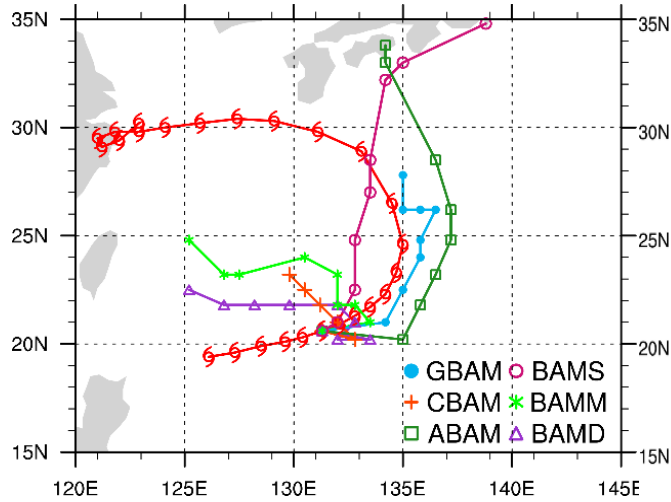
(A total of 133 TCs occurred in the Western Pacific during 1979-2011)

GBAM vs. BAM [three versions: BAMS (shallow 850–700 hPa), BAMB (medium, 850–400 hPa), and BAMD (deep, 850–200hPa)]. GBAM is applied to anomaly Max-Vor/Min-Div level

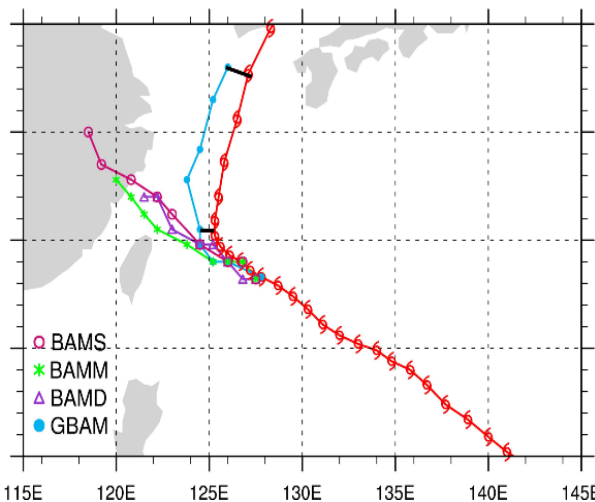
(Huang, Du, and Qian, 2015, WAF)

Turning tracks (48hr forecasts)

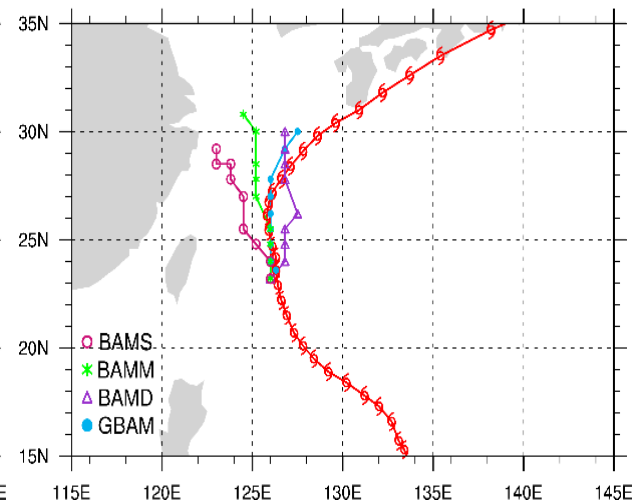
(a) Todd 00Z 16Sep1998



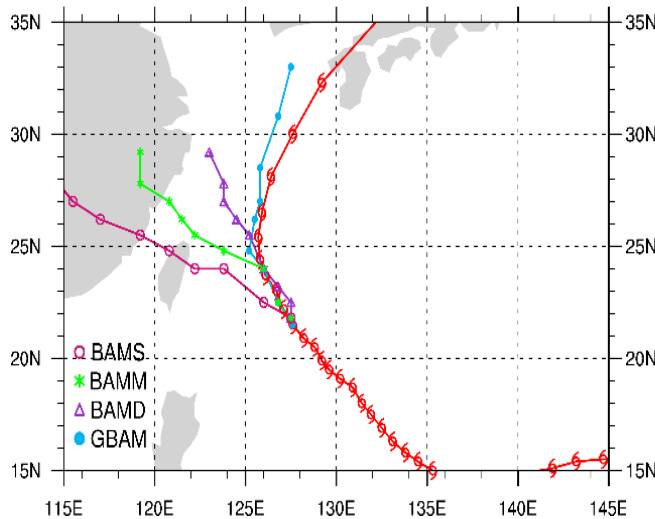
(b) TC (2003#15)



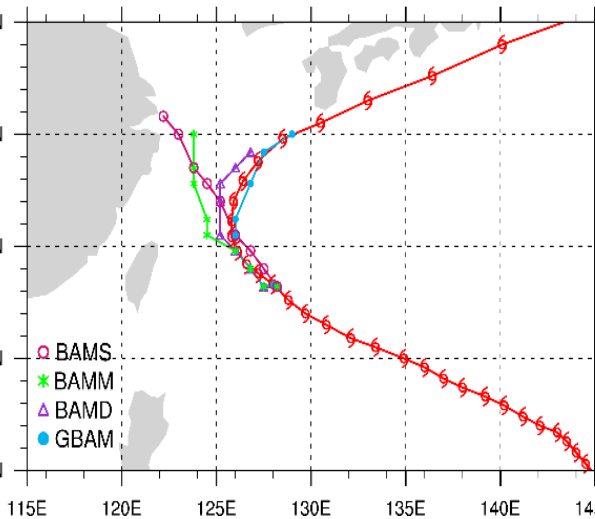
(c) TC (1990#21)



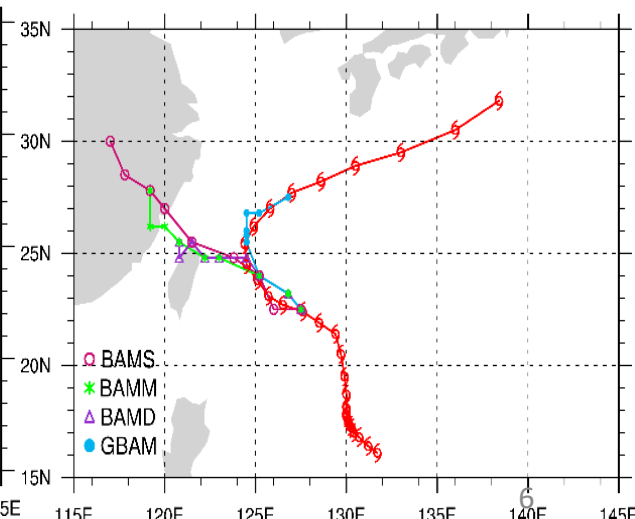
(d) TC (1991#21)



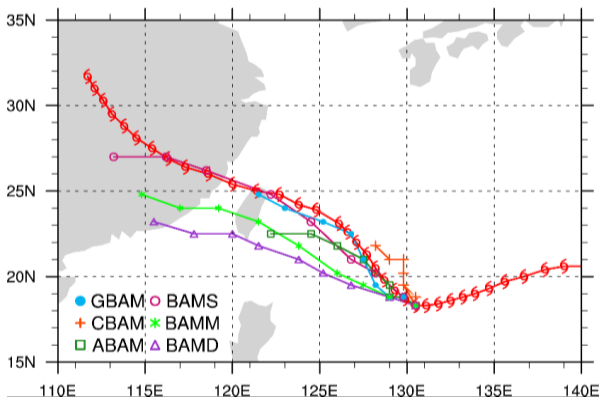
(e) TC (1980#23)



(f) TC (2001#25)

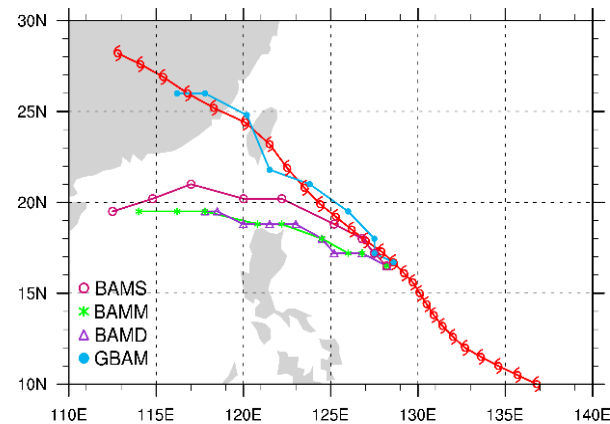


(a) Herb 18Z 28Jul 1996

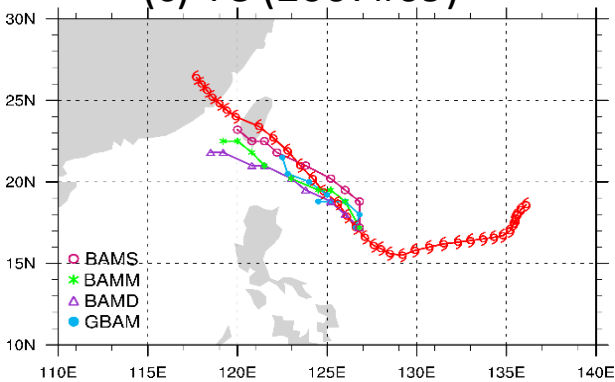


Straight tracks (48hr forecasts)

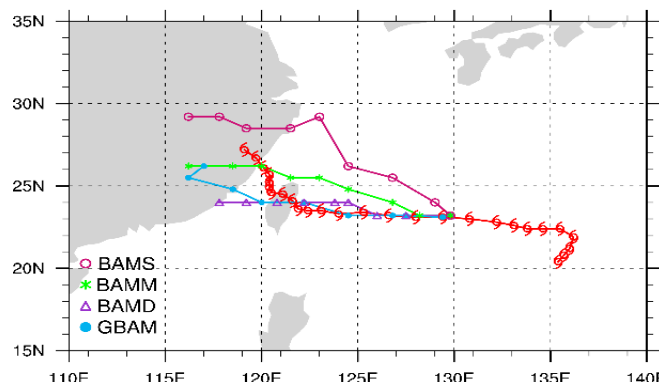
(b) TC (1994#08)



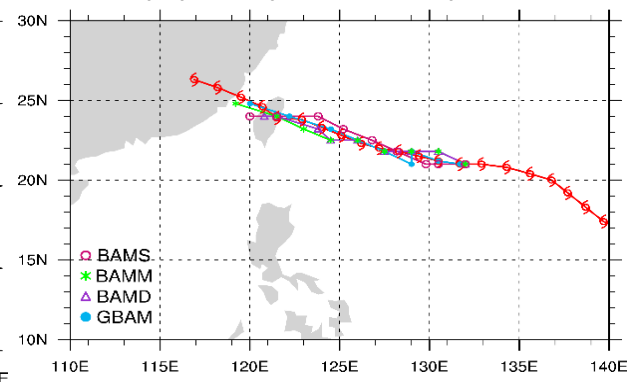
(c) TC (2007#09)



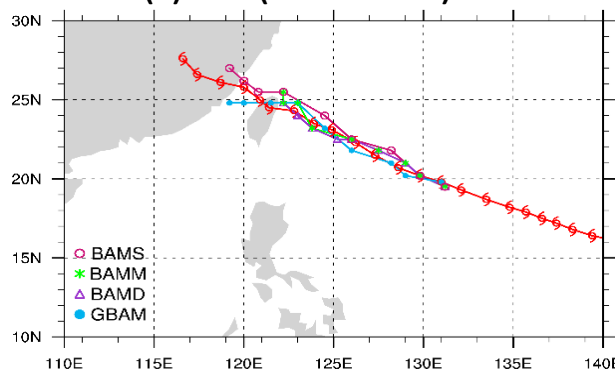
(d) TC (2009#09)



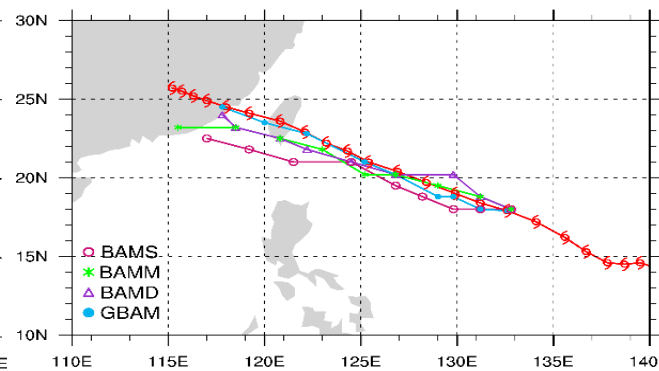
(e) TC (2005#13)



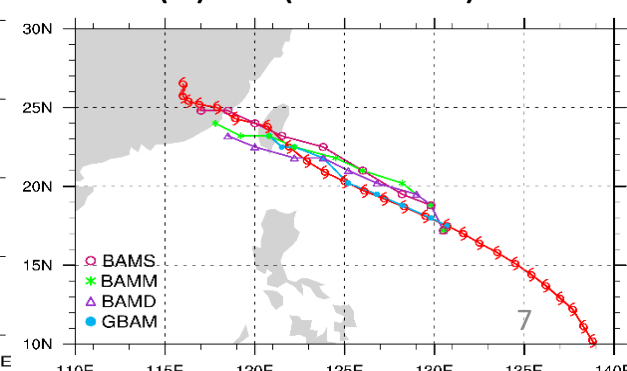
(f) TC (1980#15)



(g) TC (1990#17)



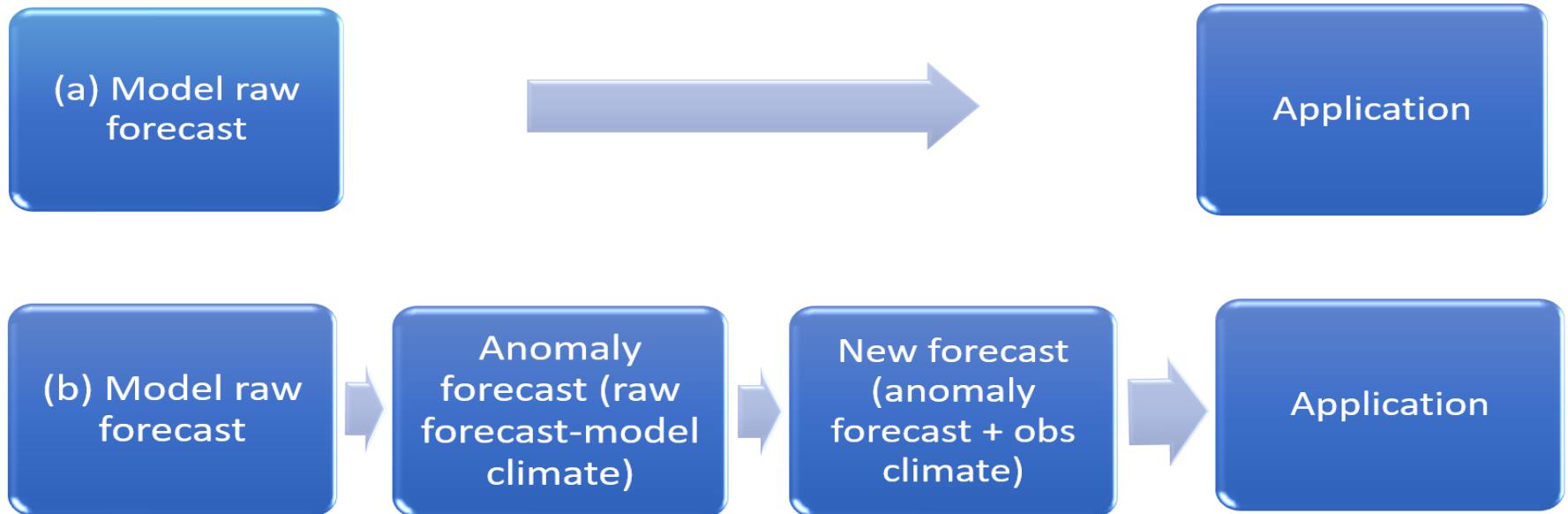
(h) TC (2000#18)



Anomaly-based post-processing (model climate is replaced by observed climate) (Du and Deng 2022, *Atmos.*)

$$fcst_{anomaly} = fcst_{raw} - climate_{model} \quad (1)$$

$$fcst_{new} = (fcst_{raw} - climate_{model}) + climate_{observed} \quad (2)$$



Lorenz model (Lorenz-84)

The 3-variable (X , Y , and Z) nonlinear Lorenz model (Lorenz 1984 and 1990)

$$\frac{dX}{dt} = -Y^2 - Z^2 - aX + aF$$

$$\frac{dY}{dt} = XY - bXZ - Y + G$$

$$\frac{dZ}{dt} = bXY + XZ - Z$$

X represents zonal wind, Y and Z are superposed waves, and t is time. The parameters a , b , F and G can be viewed as model physics, where a and b are drag damping, and F and G are symmetric and asymmetric thermal forcing.

Experiment design

- Perfect model → 30 years for calculating “observed climate”; the 31st year as truth for verification

$$X_0 = [2.0 + 2 \cos(\frac{2\pi \cdot \text{day}}{365})] + \text{RAN}_x(\text{year})$$

$$Y_0 = [1.0 + 2 \cos(\frac{2\pi \cdot \text{day}}{365})] + \text{RAN}_y(\text{year})$$

$$Z_0 = [0.0 + 2 \cos(\frac{2\pi \cdot \text{day}}{365})] + \text{RAN}_z(\text{year})$$

- Imperfect model → 30 years for calculating “model climate”; the 31st year as forecasts for verification

$$X'_0 = [2.0 + 2 \cos(\frac{2\pi \cdot \text{day}}{365}) + \text{RAN}_{-x}(\text{year})] + \text{RAN}_{-x}(\text{day})$$

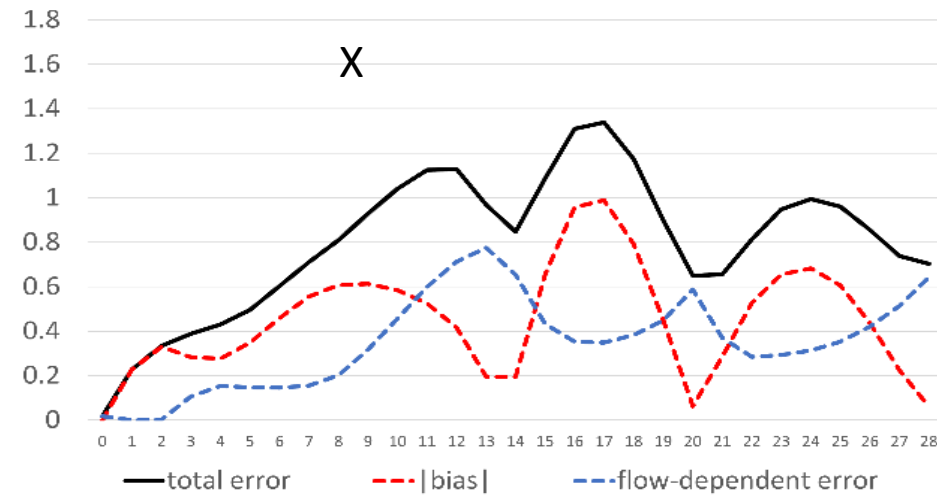
$$Y'_0 = [1.0 + 2 \cos(\frac{2\pi \cdot \text{day}}{365}) + \text{RAN}_{-y}(\text{year})] + \text{RAN}_{-y}(\text{day})$$

$$Z'_0 = [0.0 + 2 \cos(\frac{2\pi \cdot \text{day}}{365}) + \text{RAN}_{-z}(\text{year})] + \text{RAN}_{-z}(\text{day})$$

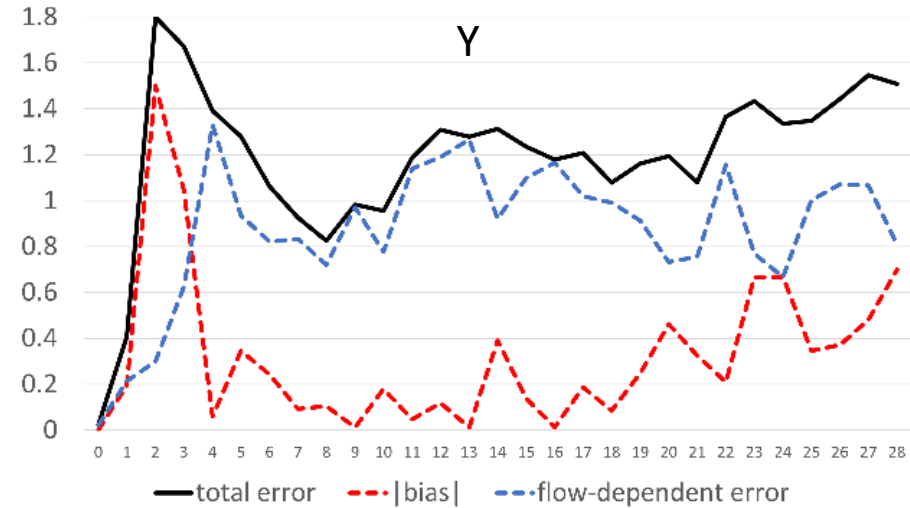
- Forecast once per day with forecast length of 1-28 days (4 weeks trying to include sub-seasonal range)

Total error and its decomposition

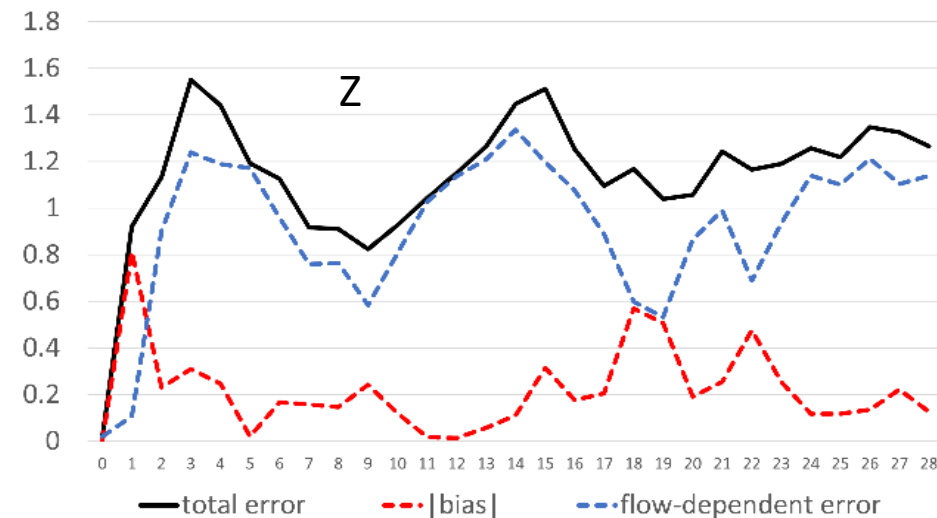
(a) Forecast error and its decomposition of X (average of 365 days in year31)



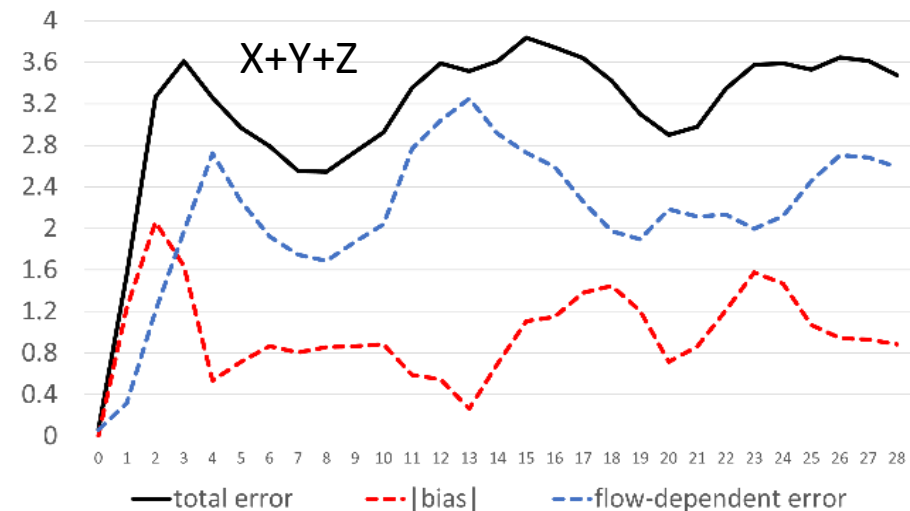
(b) Forecast error and its decomposition of Y (average of 365 days in year31)



(c) Forecast error and its decomposition of Z (average of 365 days in year31)

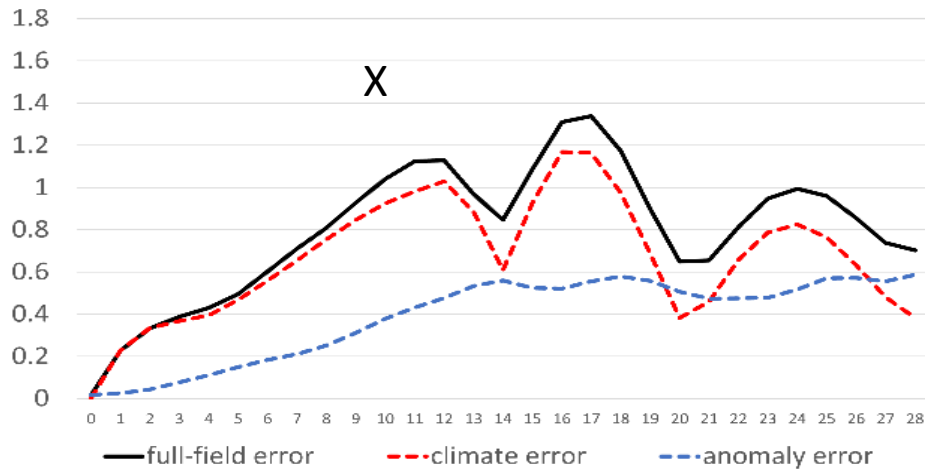


(d) Forecast error (sum) and decomposition of X+Y+Z (average of 365 days in year31)

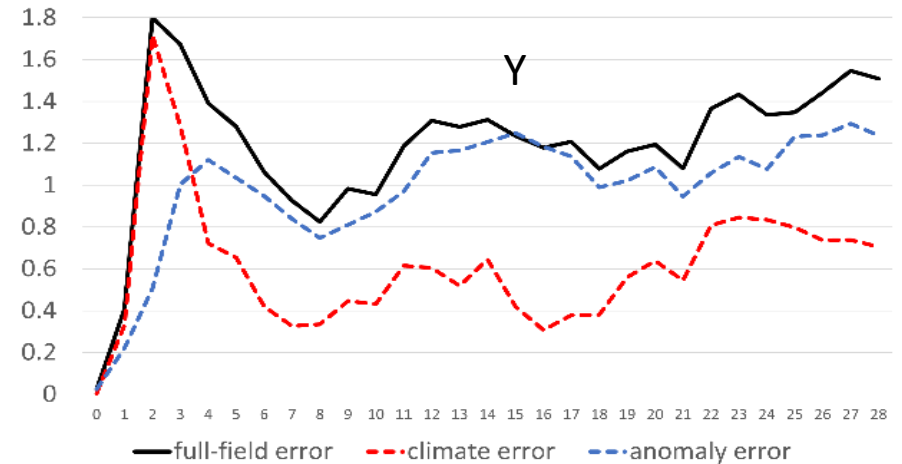


Forecast errors of the full, climate and anomaly fields

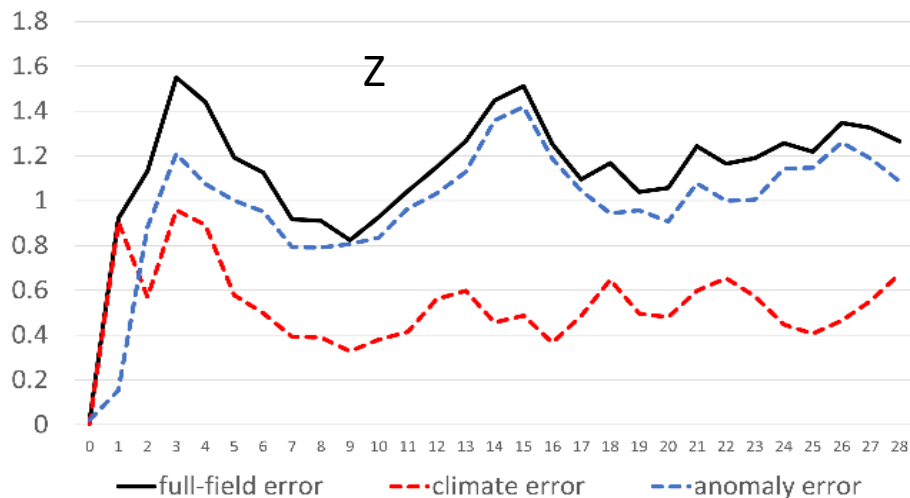
(a) Absolute errors of full field, climate and anomaly forecasts for X (average of 365 days in year31)



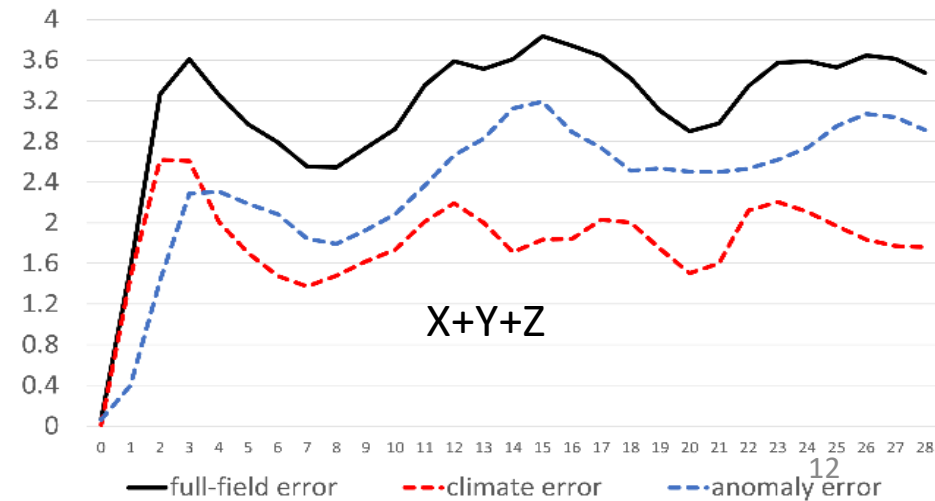
(b) Absolute errors of full field, climate and anomaly forecasts for Y (average of 365 days in year31)



(c) Absolute errors of full field, climate and anomaly forecasts for Z (average of 365 days in year31)



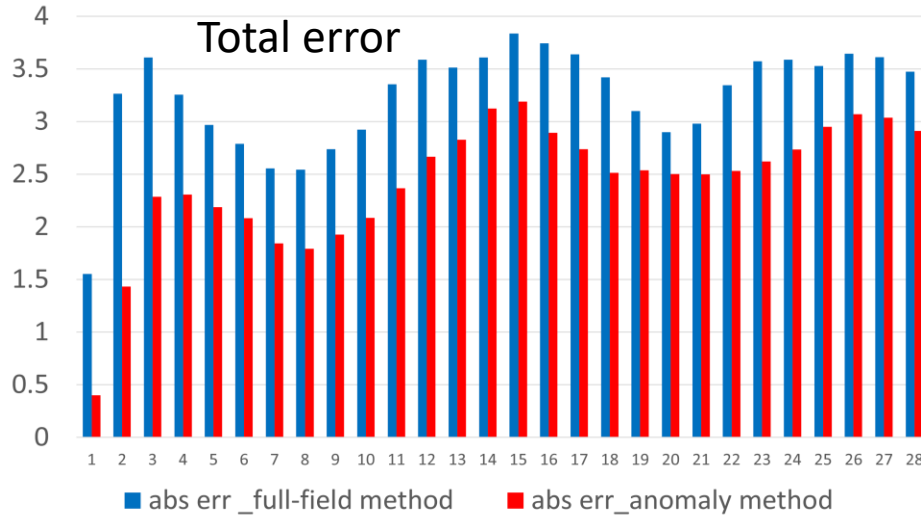
(d) Absolute errors of full field, climate and anomaly forecasts for X+Y+Z (average of 365 days in year31)



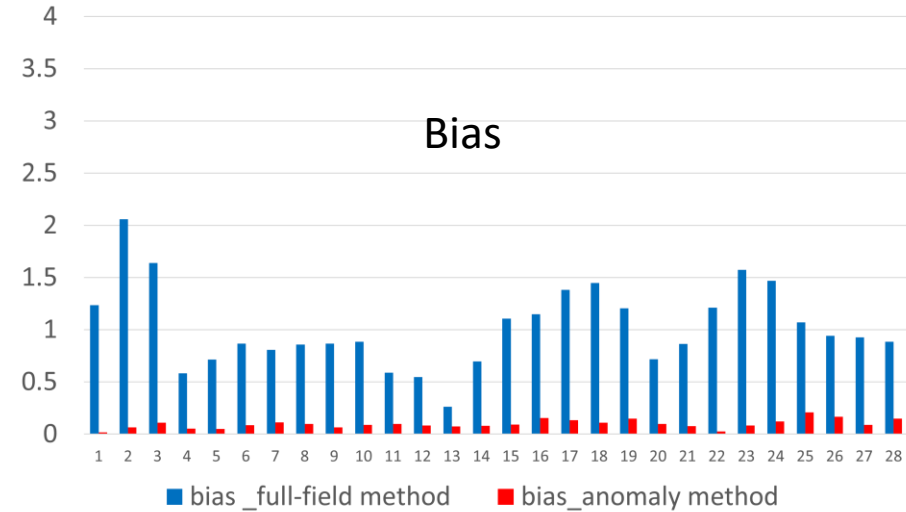
Magnitude improvement: error changes before and after

X+Y+Z average

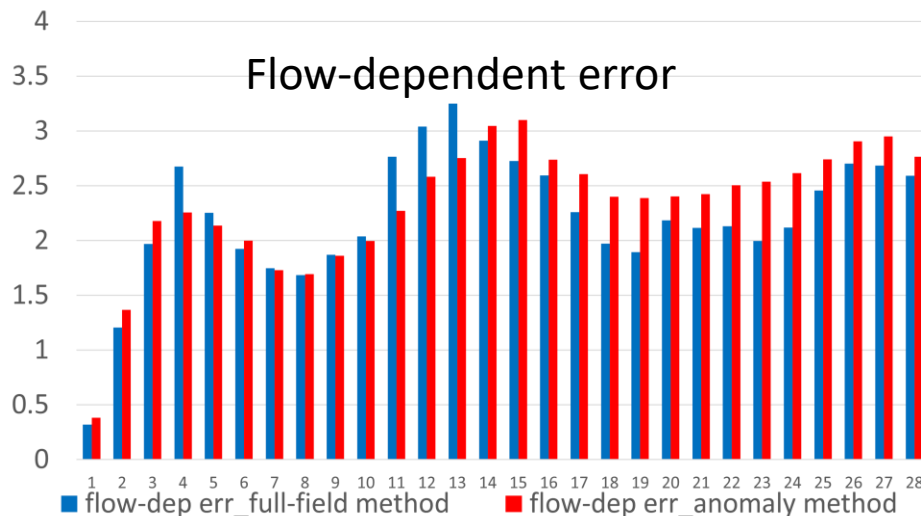
(a) Average change of absolute error for X, Y and Z (average of 365 days in year31)



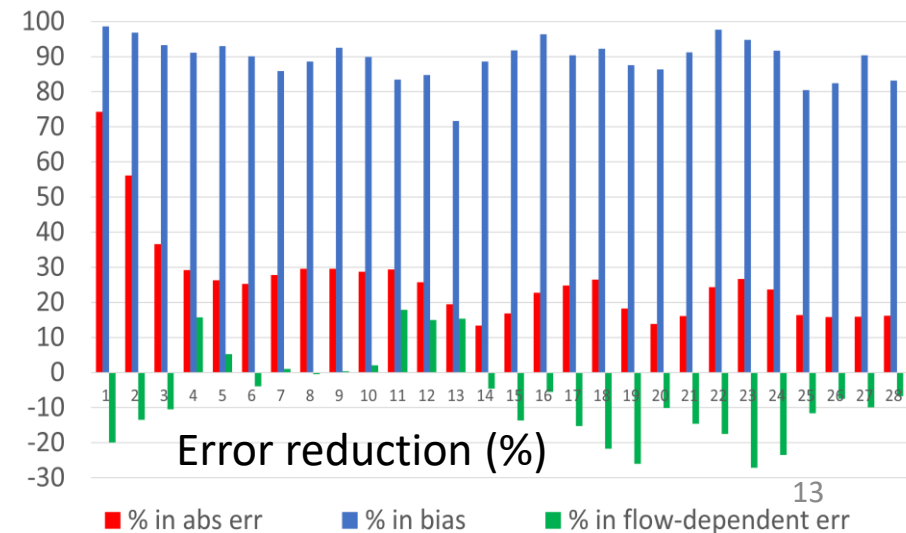
(b) Average change of bias error for X, Y and Z (average of 365 days in year31)



(c) Average change of flow-dependent error for X, Y and Z (average of 356 days in year31)

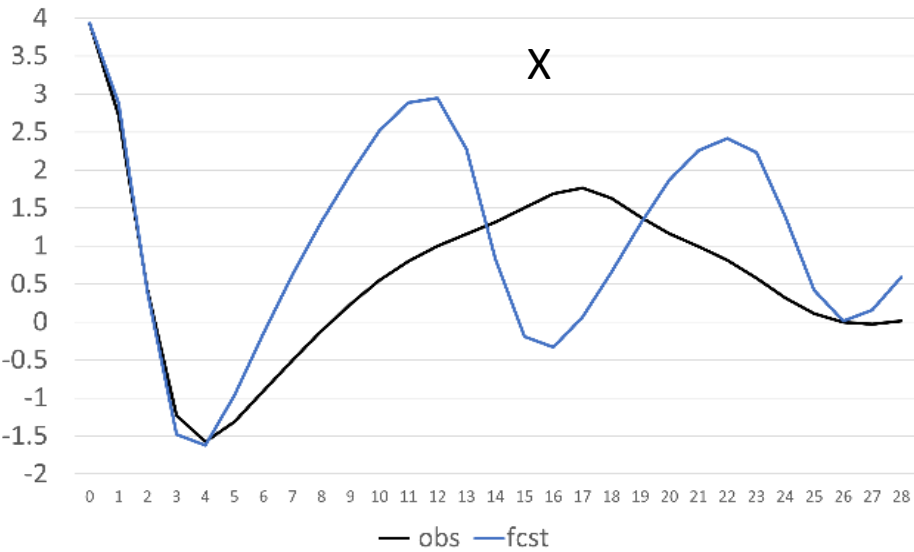


(d) Average percentage of error reduction for X, Y and Z (%) (average of 365 days in year31)

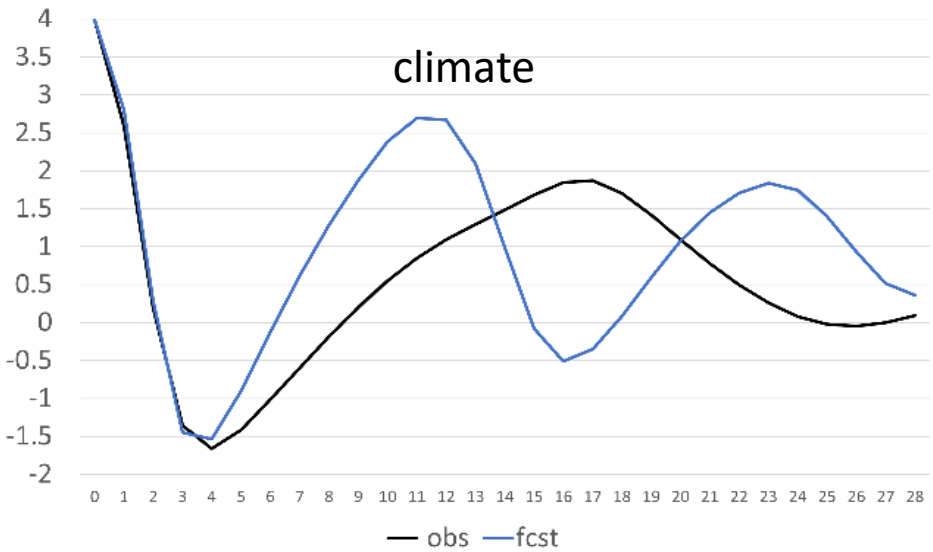


Situation 1: larger bias and smaller flow-dependent errors

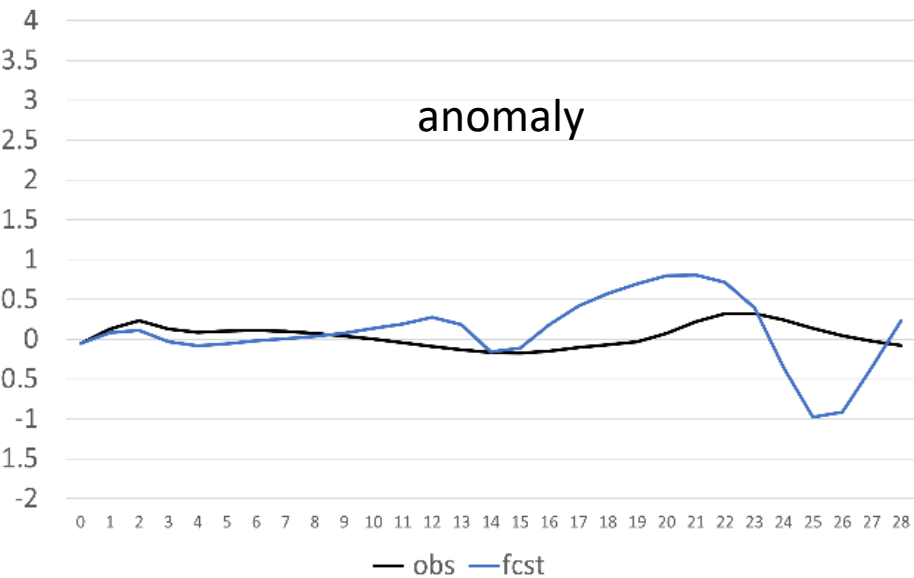
(a) Full field of X (day1 of year31)



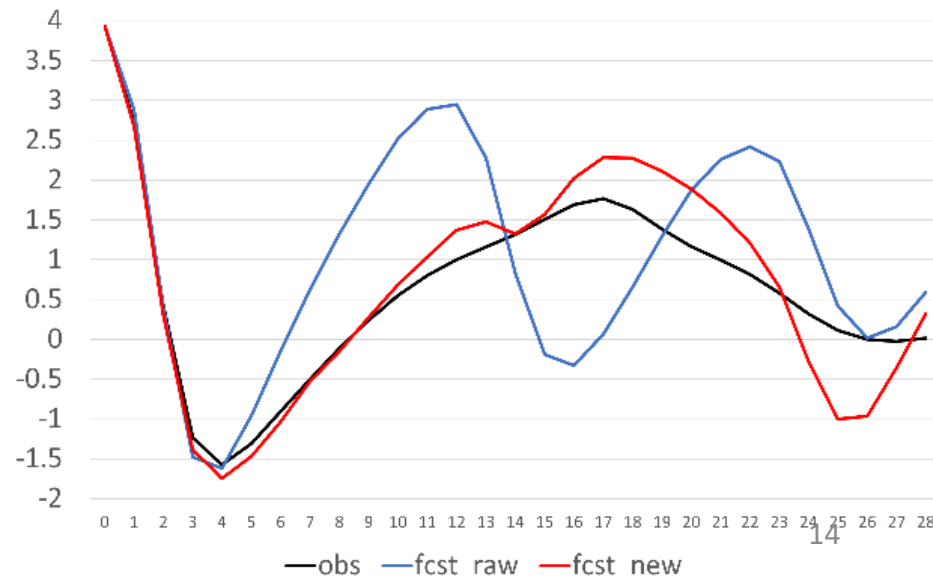
(b) Climate of X (day1)



(c) Anomaly of X (day1 of year31)

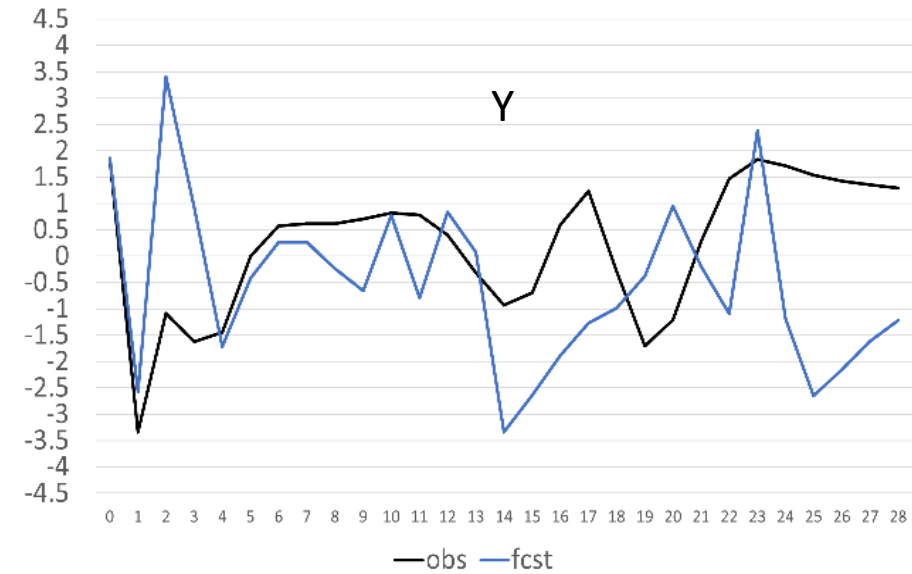


(d) Raw and new forecasts of X (full field, day1 of year31)

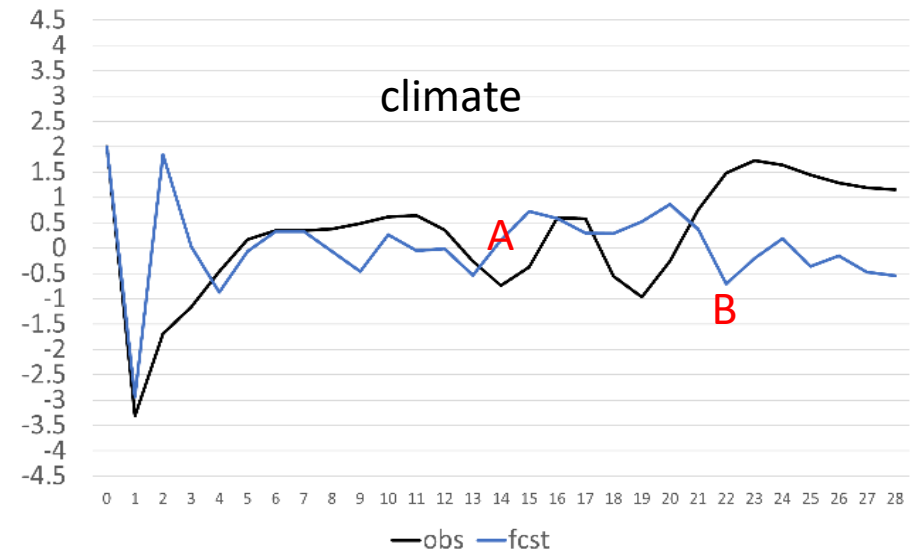


Situation 2: smaller bias error and larger flow-dependent error

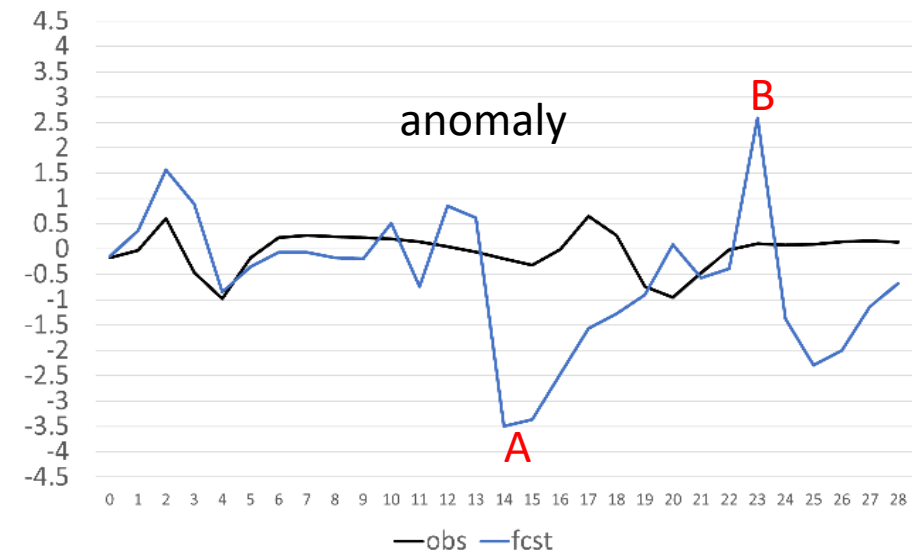
(a) Full field of Y (day1 of year31)



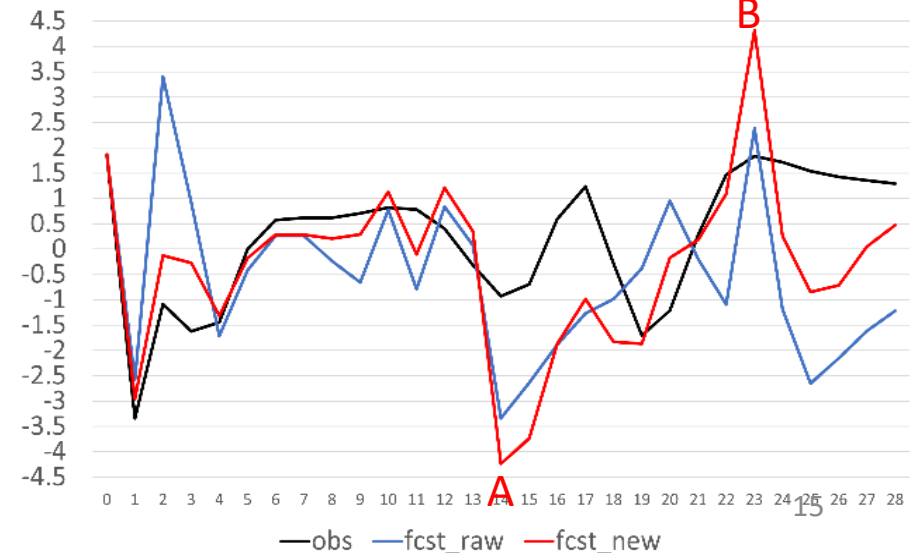
(b) Climate of Y (day1)



(c) Anomaly of Y (day1 of year31)

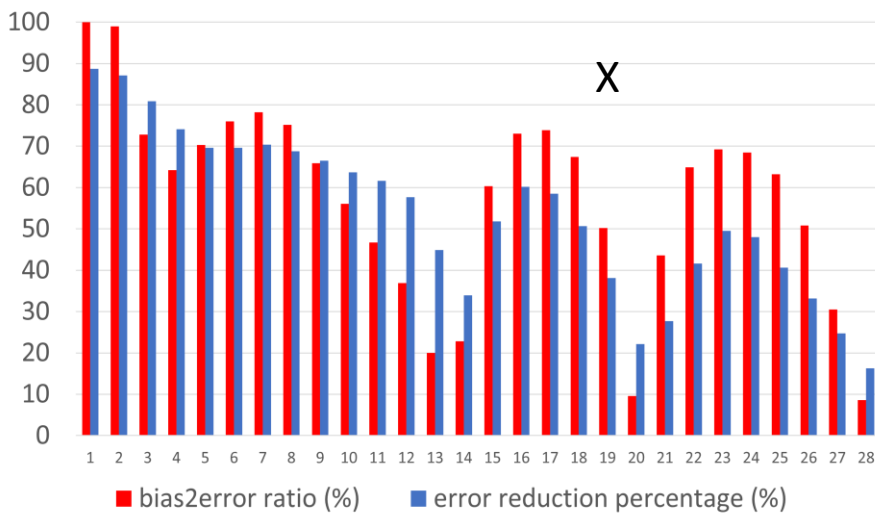


(d) Raw and new forecasts of Y (full field, day1 of year31)

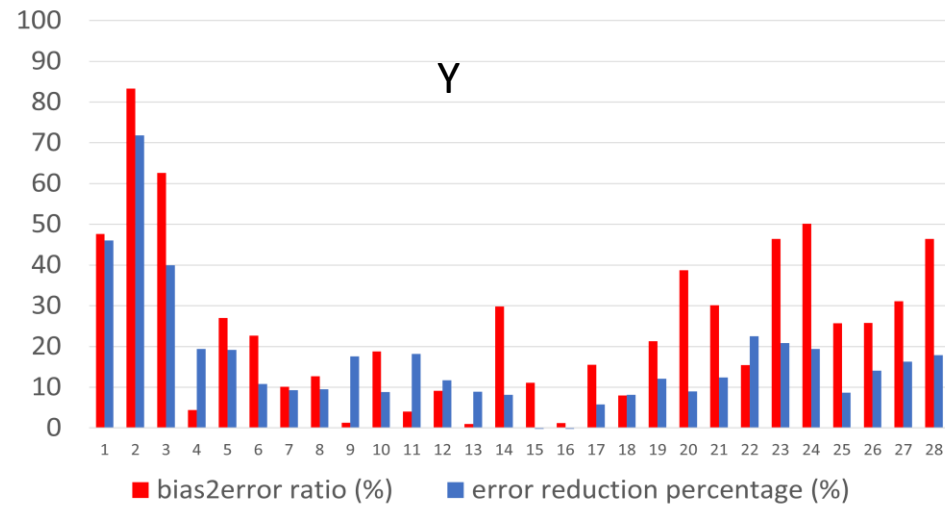


Relationship between Bias error and forecast improvement

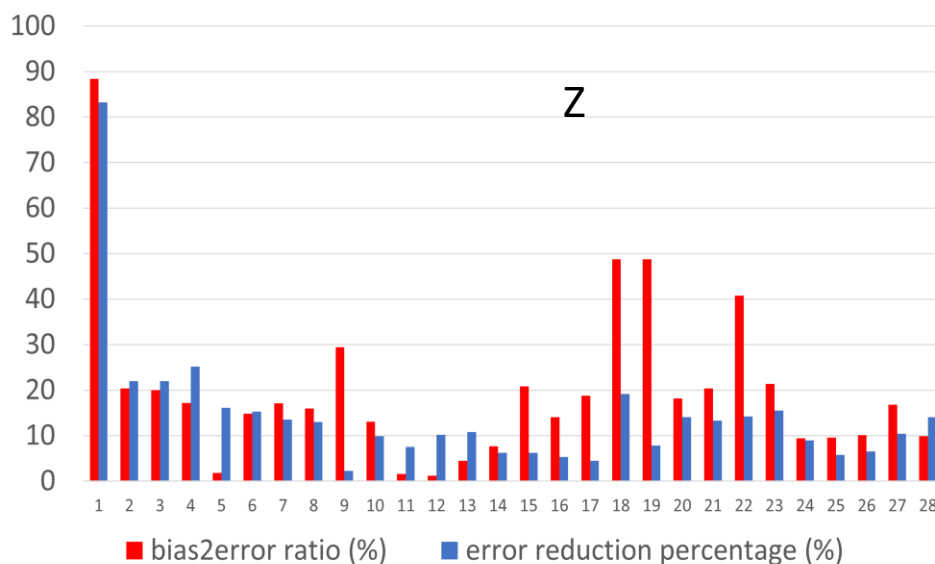
(a) Relation between bias and error reduction for X (average of 365 days in year31)



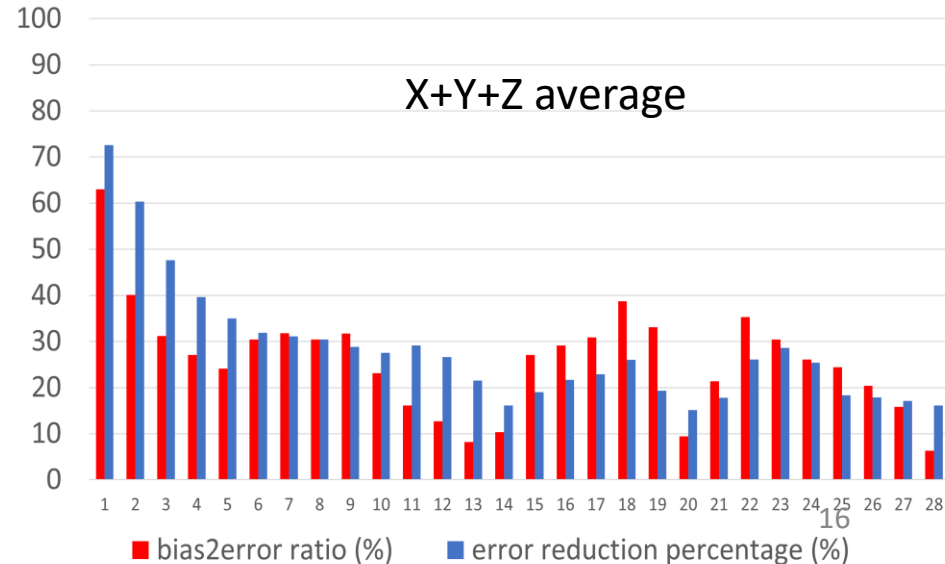
(b) Relation between bias and error reduction for Y (average of 365 days in year31)



(c) Relation between bias and error reduction for Z (average of 365 days in year31)



(d) Relation between bias and error reduction, averaged for X, Y and Z (average of 365 days in year31)



What we learn?

- Bias error mainly stems from climate part and flow-dependent error mainly stems from anomaly part. Therefore, anomaly-based NWP model could be a systematic-error free system
- Could anomaly-based NWP model be a possible direction for the next-generation NWP? If the answer is “yes”, an NWP center needs to invest some resources on developing such a state-of-the-art anomaly-based NWP model
- High-resolution (both spatial and temporal) reanalysis and model’s reforecast datasets are needed