

14.2. Multivariate Data Assimilation of Carbon Cycle Using Local Ensemble Transform Kalman Filter

¹Ji-Sun Kang, ¹Eugenia Kalnay, ²Junjie Liu, ²Inez Fung, and ¹Ning Zeng

¹University of Maryland, College Park, Maryland

²University of California, Berkeley, California

1. Introduction

In order to project a future climate, it is necessary to take into account of the impact of greenhouse gases which are being emitted more and more due to the human activities. This study has focused on CO₂, one of major greenhouse gases. In addition to the anthropogenic emission, it is absorbed or released from the surface (land and ocean), depending on the biogeochemical conditions as well as its interaction and feedback with the climate. Estimating surface CO₂ fluxes is essential to project the global budget of CO₂ because natural variability of surface CO₂ fluxes can answer how much of CO₂ will remain in the atmosphere.

Thus, our purpose in this study is to estimate surface CO₂ fluxes as well as atmospheric CO₂ concentration with an advanced data assimilation technique.

2. SPEEDY-C and VEGAS with SLand

First, we modified SPEEDY model (Molteni, 2003) to simulate atmospheric CO₂ concentration. We added one prognostic variable of atmospheric CO₂ which has only advection and diffusion, in addition to the original prognostic variables of wind (U, V), temperature (T), humidity (q), and surface pressure (Ps). Then, the model reads the forcing of surface CO₂ fluxes and transports it by wind in the atmosphere. The model does not change surface CO₂ fluxes. This model will be referred to as "SPEEDY-C".

For the time-varying fluxes of surface CO₂, we coupled a terrestrial carbon model VEGAS (Zeng, 2005), which is coupled to the physical land surface model SLand (Zeng et al., 2000a), to SPEEDY-C. With this coupled atmosphere-vegetation-soil model, we can calculate the CO₂ fluxes over land with time, but the climatology of the SPEEDY-VEGAS-SLand is significantly different from SPEEDY-C. ¹

3. Three types of data assimilation: LETKF

Using LETKF (Hunt et al., 2007), we have tried three types of data assimilation: One is an **uncoupled (univariate) data assimilation** in which

atmospheric CO₂ concentration and surface CO₂ flux are updated by CO₂ observations and not affected by other atmospheric variables. Another is an **one-way multivariate data assimilation** in which the atmospheric CO₂ concentration and surface CO₂ flux are updated by these two variables as well as the wind fields, while the wind field, in addition to other atmospheric variables such as specific humidity and temperature, is not affected by these two carbon-related variables. The other is a **multivariate data assimilation** so that all the dynamical variables are included in one vector.

Here, the dynamic variables of analysis are (U, V, T, q, Ps, CO₂, CF). We do not have any observation of CO₂ fluxes (CF). Thus, CF can be updated by only background error covariance.

4. Experimental design: OSSEs

4.1. Perfect model simulation

We used the same model, SPEEDY-C, for both of nature and forecast, so model error could be ignored. Furthermore, we included only fossil fuel emission as the carbon fluxes forcing which is constant with time and 6 PgC/yr (Andres et al., 1996). We tested three types of analysis introduced above.

The observations of the atmospheric variables are located at the rawinsonde distribution of which coverage is about 9% in horizontal, while those of atmospheric CO₂ are uniformly distributed at every other grid so that the coverage is about 25%. The observation error for each variable is as follow; 1m/s for U and V, 1K for T, 0.1g/kg for q, 1hPa for Ps, 1ppmv for atmospheric CO₂.

Analysis has been done every 6 hour; we have been used 20 ensemble members, and 8% of multiplicative inflation. All the results are the 2-month analysis. The initial condition of CF are generated by randomly choosing 20 CF from the nature run and adding small random perturbation so it does not use any a priori information at all.

4.2. Imperfect model simulation

SPEEDY-VEGAS-SLand was used for nature run. This model has a climatology rather different than the SPEEDY-C which we use as the forecast model so that we need to consider model error, and only the one-way multivariate data assimilation was

¹ Corresponding author address, 4337 CSS, University of Maryland, College Park, MD 20742. E-mail: jskang@atmos.umd.edu

examined for imperfect model simulation. We have the time-varying CF over land from the coupled model and the monthly prescribed CF over ocean given by Takahashi et al. (2002).

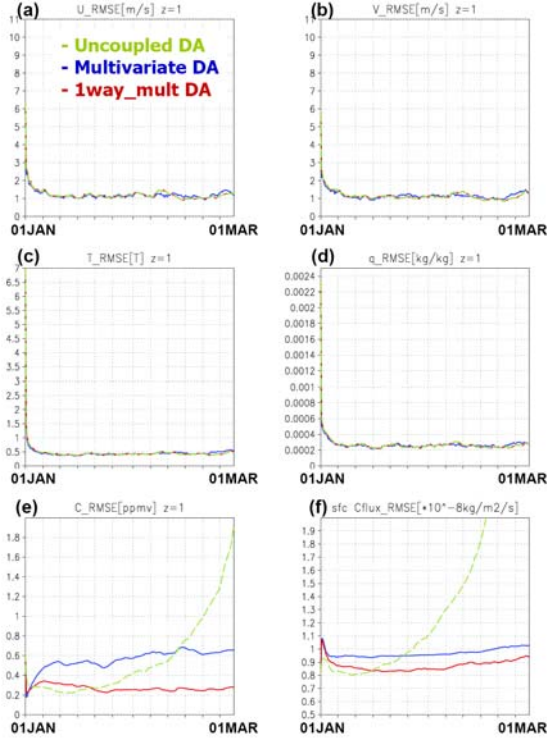


Figure 1. RMS error of analysis from three types of data assimilation: uncoupled(green),multivariate(blue), and one-way multivariate(red) data assimilation for (a) U, (b) V, (c) T, (d) q, (e) atmospheric CO₂ on the lowest layer of model, and (f) surface CO₂ fluxes

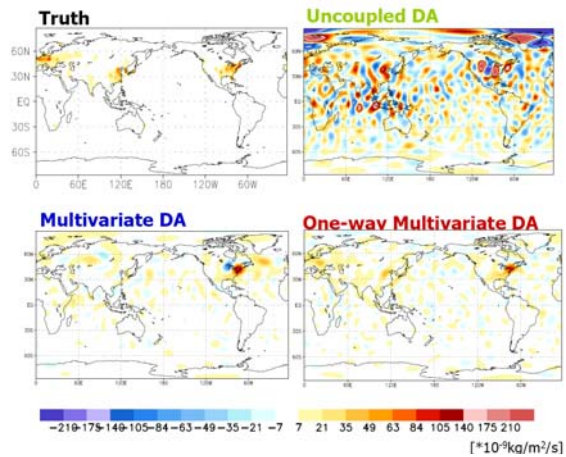


Figure 2. True state of surface CO₂ fluxes after two months of analysis, and the resultant analysis of it from three types of analysis.

10% of multiplicative inflation has been used except for the different inflation experiments (section 6.2). Rest of experimental settings is same as that of perfect model simulation.

5. Perfect model simulation

Both multivariate systems performed well in terms of RMS error (Fig. 1 and 2). The one-way multivariate assimilation resulted in the optimal performance for the CO₂ variables because it minimizes the sampling in the feedback from carbon variables to the atmospheric variables. By contrast, the univariate assimilation of carbon had larger errors and diverged. Using one-way multivariate data assimilation technique, we also tested the experiment which has the observations of CO₂ concentration only in the lowest layer and got the comparably good results (not shown). Moreover, experiment with daily observations of CO₂ still estimated CF reasonably well (not shown).

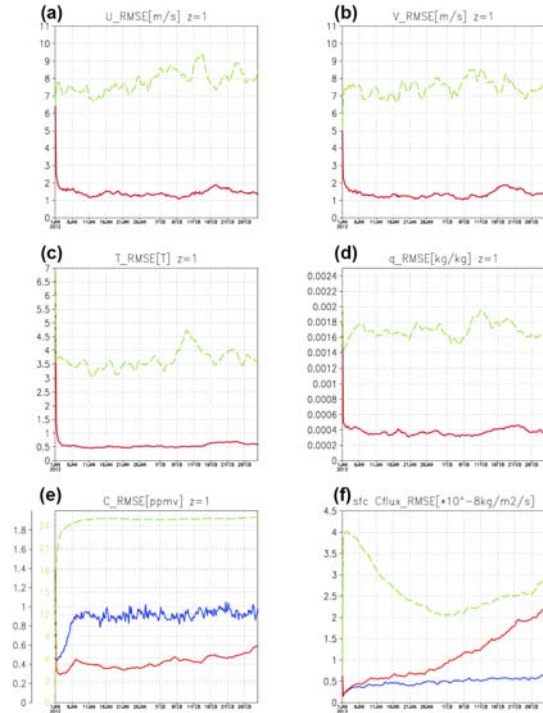


Figure 3. RMS error of analysis from imperfect model simulations: no bias correction (green), bias correction (red), and bias correction + different inflation (blue) for (a) U, (b) V, (c) T, (d) q, (e) atmospheric CO₂ on the lowest layer of model, and (f) surface CO₂ fluxes

6. Imperfect model simulation

Since we confirmed that one-way multivariate data assimilation has optimal performance through the perfect model simulation, we applied only this technique for imperfect model case. From the figure of RMS error (Fig.3: green), we found that the forecast was significantly different from the nature so that the ensemble system does not represent the true state well.

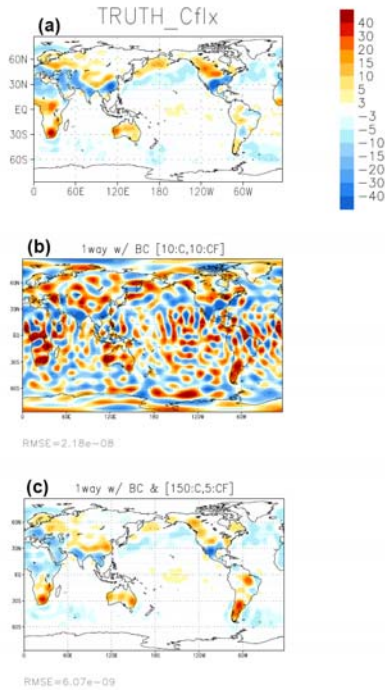


Figure 4. (a) True state of surface CO₂ fluxes after two months of analysis, and the resultant analysis of it from the experiment (b) with bias correction, (c) with bias correction + different inflation factors for CO₂ variables.

6.1. Model bias correction

We tried to estimate and fix the model bias we saw the previous experiment. Similar to Danforth et al. in 2007, we averaged the distance between the nature and the six-hour forecast which started from the true state for two months. Then, we subtracted this estimated model bias from the ensemble forecast before the analysis step.

With this simple method, we could get remarkable improvement in the analysis. Especially for the atmospheric variables and atmospheric CO₂ which have the observations, the current ensemble system worked very well. The analysis of CF, however, got diverged with time (Fig.3: red, Fig. 4(b) and 5(b)).

6.2. Inflation for atmospheric CO₂ and surface CO₂ fluxes

We found that the ensemble spread of CO₂ is not enough to estimate CF well so that we made a test run which has different inflation factor for CO₂ and CF. With large inflation (=1.50) for CO₂ and small inflation (=0.05) for CF, we obtained an excellent performance of CF (Fig.3: blue). Analysis of CO₂ got a little worse, but not bad if we consider 1ppmv of the observation error (Fig. 3, 4, and 5).

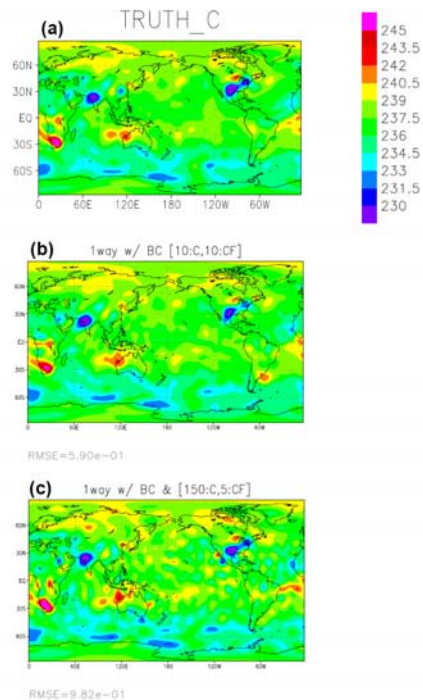


Figure 5. (a) True state of atmospheric CO₂ on the lowest layer after two months of analysis, and the resultant analysis of it from the experiment (b) with bias correction, (c) with bias correction + different inflation factors for CO₂ variables.

7. Summary and discussion

This study is a component of a project for CO₂ data assimilation with LETKF/CAM3.5 system (PIs: Eugenia Kalnay/Inez Fung). The CAM3.5 is very complex and expensive whereas the SPEEDY and the VEGAS are simple but realistic, having only an intermediate complexity. The coupled system of SPEEDY-VEGAS has produced reasonable results and LETKF has been also implemented successfully.

Through the perfect model simulation with three types of data assimilation, we can conclude that the multivariate CO₂ data assimilation experiments were performed for the first time, and the results indicate

that multivariate EnKF assimilation is much more effective in estimating both atmospheric CO₂ and surface CO₂ fluxes, even in the absence of observations or prior estimations of surface fluxes.

Under the imperfect model assumption, we could estimate and remove the model bias and then get encouraging results and further improve the results with different inflation factors for atmospheric CO₂ and surface CO₂ fluxes. In order to find the optimal values for the inflation, we plan to calculate adaptive inflation and observation error (Li, 2008) for atmospheric variables as well as atmospheric CO₂.

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