A COMPARISON OF PRECIPITATION FORECAST SKILL BETWEEN SMALL CONVECTION-ALLOWING AND LARGE CONVECTION-PARAMETERIZING ENSEMBLES

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1. INTRODUCTION

In current global ensemble forecast systems [e.g., the National Centers for Environmental Prediction (NCEP) Global Forecast System (GFS; Toth and Kalnay 1993), Ensemble Prediction System; European Center for Medium-Range Weather Forecasts (ECMWF; Molteni et al. 1996) Ensemble Prediction System], various methods to generate initial condition (IC) perturbations [e.g., Toth and Kalnay 1997; Palmer et al. 1992; Molteni et al. 1996] and model perturbations yield reliable medium-range (2-10 day) forecasts of synoptic-scale parameters like 500-hPa geopotential height and mean-sea-level pressure. For the purpose of medium-range synoptic forecasting, IC errors make much larger relative contributions than model errors after synoptic-scale error growth becomes non-linear (~24 hrs; Gilmour 2001). However, for short-range forecasts of small-scale phenomena like warm-season precipitation, which is the focus of this study, accounting for model error by using different combinations of physical parameterizations [e.g., Houtekamer et al. 1996; Stensrud et al. 2000; Du et al. 2004; Jones et al. 2007] and numerical models [e.g., Wandishin et al. 2001; Du et al. 2004; Eckel and Mass 2005] becomes very important in generating sufficient model dispersion. Unfortunately, even in these ensembles that include IC, model formulation, and physics perturbations, short-range forecasts for sensible weather phenomenon like convective precipitation remain underdispersive (Eckel and Mass 2005). Several factors are probably contributing to this lack of spread including coarsely resolved and temporally interpolated lateral boundary conditions (LBCs; Nutter et al. 2003), inappropriate IC perturbation strategies for short-ranges (Eckel and Mass 2005), and inability to capture small-scale variability because of insufficient resolution (Eckel and Mass 2005).

Because of computational limitations, regional scale short-range ensemble forecast (SREF) systems like those run at NCEP (Du et al. 2004), the University of Washington (UW; Eckel and Mass 2005), and Stony Brook University (SBU; Jones et al. 2007) have been forced to use relatively coarse grid-spacing (32-45 km for NCEP’s SREF system, 12-km within a 32-km outer nest in UW’s system, and 12-km for SBU’s system) and, thus, must use cumulus parameterization (CP). In ensemble systems, using different CPs is an effective way to generate spread in rainfall forecasts (e.g., Jankov et al. 2005), but using CPs introduces systematic errors in rainfall forecasts (e.g., Davis et al. 2003; Liu et al. 2006; Clark et al. 2007), and models using CPs cannot resolve fine scale features in rainfall systems. Because of these limitations, significant improvements in rainfall forecasts may be realized by running an ensemble using explicit representation of convection (i.e., no CP).

Ongoing experiments that began in 2003 supporting the BAMEX project (Bow echo and MCV Experiment, Davis et al. 2004) using various 4-km grid-spacing configurations of the Weather Research and Forecasting (WRF; Skamarock et al. 2005) model to aid convective forecasting have been rather successful (see Kain et al. 2008 for a thorough review). For example, simulations using convection-allowing resolution (CAR, hereafter) have been found to more accurately depict the diurnal precipitation cycle (Clark et al. 2007; Weisman et al. 2008), as well as MCS frequency and convective system mode (Done et al. 2004; Weisman et al. 2008) relative to simulations using parameterized-convection resolution (PCR, hereafter). Although increasing to CAR may not necessarily increase forecast skill for deterministic forecasts as measured by traditional “grid-based” metrics [e.g., Equitable Threat Score (Schaefer 1990) and bias] because of small displacement errors in small scale features leading to large errors (Baldwin et al. 2001; Davis et al. 2006a), it is possible that significant improvements in probabilistic precipitation forecasts may be obtained from an ensemble using CAR because of superior spatial/temporal representation of statistical properties of convective precipitation in the CAR members (e.g., Fritsch and Carbone 2004; Kong et al. 2006 and 2007). Also, because error growth occurs more rapidly at smaller scales, ensembles using CAR may have a better representation of forecast uncertainty. However, because of current computational limitations it is difficult to create a CAR ensemble in real-time with a domain size and number of members comparable to ensembles that are currently being used operationally. Although, given the potential advantages of CAR, an ensemble composed of a relatively small number of CAR members could potentially outperform an ensemble composed of a large number of PCR members, in which case there will be incentive for future operational ensemble systems to reduce numbers of members in order to increase to CAR.

Given these computational considerations, this study aims to compare warm-season precipitation
forecast skill between a small (5-member), CAR ensemble using 4-km grid-spacing (ENS4) and a relatively large (15-member), PCR ensemble using 20-km grid-spacing (ENS20), each covering a similar domain over the central United States (Fig. 1). Because these ensembles have different numbers of members, special care is taken to properly compare probabilistic skill metrics. Although ENS4 has fewer members than ENS20, the computational expense should not be considered equal. In fact, because of the time-step reduction and 3-D increase in number of grid-points, a reduction in grid-spacing from 20 to 4-km increases computational expense by a factor of ~125. Thus, because ENS4 has ½ the members as ENS20, it is still about 42 times more computationally expensive than ENS20 (125*½=42), and to conduct the comparison between ensembles with equal computational expense would require ENS20 to have 125*5=625 members. So, the purpose of this study is not to compare ensembles with similar computational expense, but to determine if at some point when computational capabilities allow, it would be advantageous to reduce ensemble size in order to use CAR.

2. ENSEMBLE DESCRIPTIONS AND CASES EXAMINED

The ENS4 ensemble was obtained from a real-time ensemble forecasting experiment conducted as part of the NOAA Hazardous Weather Testbed (HWT) Spring Experiment (Kain et al. 2008) during April-June 2007 (Xue et al. 2007; Kong et al. 2007). A 4-km grid-spacing CAR WRF-ARW (Version 2.2.0) model ensemble was run by the Center for Analysis and Prediction of Storms (CAPS) of the University of Oklahoma, which was composed of 10 members initialized daily at 2100 UTC and integrated 33 hours over an approximately 3000 x 2500 km domain covering much of the central United States (Fig. 1). Four of the members used both perturbed ICs and mixed physical parameterizations (mixed-physics), while six members, including the control member, used only mixed-physics so that effects of changing model physics could be isolated. In this study, only the four members with both mixed-physics and perturbed ICs plus the control member - a five member ensemble (ENS4 ensemble) - are used because the ensemble using mixed-physics alone ignores initial condition uncertainty, an important source of forecast uncertainty. For the control member, the 2100 UTC analyses from NCEP’s operational North American Mesoscale (NAM; Janjic 2003) model (at 12-km grid-spacing) are used for ICs and the 1800 UTC NAM 12-km forecasts are used for LBCs. For the initial perturbed members, perturbations extracted from the 2100 UTC NCEP SREF WRF-ARW and WRF-NMM members are added to the 2100 UTC NAM analyses, and the corresponding SREF forecasts are used for LBCs (3-hr updates). Xue et al. (2007) and Kong et al. (2007) have more details on the configurations.

The ENS20 ensemble was generated at Iowa State University and is also composed of WRF-ARW (Version 2.2.0) members with perturbed ICs/LBCs and mixed-physics. Different sets of ICs for each ENS20 member are obtained directly from NCEP SREF members (listed in Table 2), rather than adding perturbations to the 2100 UTC NAM analyses, and, similar to ENS4, SREF forecasts are used for LBCs. ENS4 and ENS20 specifications are listed in Tables 1 and 2, respectively. Forecasts were examined for 23 cases during April-June 2007 (Figure 2). These cases were chosen based on the availability of the ENS4 real-time forecasts and represent a variety of convective precipitation events [e.g., isolated convection (4/19), heavy rainfall associated with a cut-off lower-lows (4/22 – 4/25), and many nocturnal MCSs (late May/early June)].

3. DATA AND METHODOLOGY

Forecasts of 1-3- and 6-hrly accumulated rainfall are examined. The Stage IV (Baldwin and Mitchell 1997) rainfall estimates are used to verify rainfall forecasts. Both Stage IV rainfall estimates and ENS4 rainfall data are remapped to a 20-km grid covering the central US (Fig. 1), which is just a sub-domain of the ENS20 members. Probabilistic and deterministic forecasts derived from each ensemble were verified. Deterministic forecasts were obtained using the probability matching technique (Ebert 2001), which is applied by assuming that the best spatial representation of rainfall is given by

Table 1 ENS4 ensemble member specifications. NAMa and NAMf indicate NAM forecasts and analyses, respectively; em_pert and nmm_pert are perturbations from different SREF members; and em_n1, em_p1, nmm_n1, and nmm_p1 are different SREF members that are used for LBCs. The remaining table elements are described in the text.

<table>
<thead>
<tr>
<th>Ensemble Member</th>
<th>ICs</th>
<th>LBCs</th>
<th>Microphysics Scheme</th>
<th>Surface Layer Scheme</th>
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Table 2 ENS20 ensemble member specifications. The ICs/LBCs table elements represent various SREF members. The * and + symbols denote the combination of 5 and 10 ensemble members, respectively, with the best statistical consistency.

<table>
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<tr>
<th>Ensemble Member</th>
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the ensemble mean and that the best frequency distribution of rainfall amounts is given by the ensemble member quantitative precipitation forecasts (QPFs). The ensemble mean obtained from the probability matching procedure (PM hereafter) can help correct for large biases in areal rainfall coverage and underestimation of rainfall amounts that are typically associated with using a standard ensemble mean, and results in a precipitation field with a much more realistic distribution.

Forecast probabilities (FPs hereafter) for precipitation were obtained by finding the location of the verification threshold within the distribution of ensemble member forecasts. The reader is referred to Hamill and Colucci (1997 and 1998) for a thorough description of the application of this technique for assigning FPs.

To verify deterministic forecasts, equitable threat score (ETS; Schaefer 1990) is used. Average ETSs were calculated by summing contingency table elements from all cases for each forecast hour and rainfall threshold, and computing the scores from the summed elements. This aggregate method gives greater weight to widespread precipitation events than if the ETS for each case was simply averaged.

To verify probabilistic forecasts, the area under the relative operating characteristic curve (ROC score; Mason 1982) is used, which is closely related to the economic value of a forecast system (e.g., Mylne 1999; Richardson 2000, 2001). The ROC score is computed from members of a contingency table for probabilistic forecasts. To construct the ROC curve, the probability of detection (POD) is plotted against the probability of false detection (POFD) for a set of specified ranges of FPs. The area under this curve is computed using the trapezoidal method (Wandishin et al. 2001). Because the method used to compute FPs in this study allows for continuous (rather than discrete) values of FPs between 0 and 100%, the same set of FP ranges that make up the points on the ROC curve can be used to verify both ensembles, and problems associated with comparing ROC scores between ensembles of different sizes are avoided.

The resampling methodology described in Hamill (1999) was used to determine whether differences in ETS and ROC score were statistically significant.
from CAR and PCR simulations (e.g., Liu et al. 2006; Clark et al. 2007; Weisman et al. 2008) supports this idea. An ensemble of CAR members with a better depiction of the propagating rainfall axis over the central US than a PCR ensemble should have a considerable advantage because individual CAR members will be more likely to fall within the range of likely solutions if they have an accurate "model climatology", whereas many of the PCR solutions may be very unlikely to verify because of consistent biases in timing and location for propagating rainfall systems.

To examine whether differences in the diurnal cycle representation exist for the ensemble members in this study, 1-hr diurnally averaged Hovmöller diagrams for all ensemble member forecasts and Stage IV observations are constructed. The Hovmöller diagram for Stage IV observations (Fig. 3c) shows that coherent propagating rainfall axes exist even for the relatively small number of cases examined. A primary axis of observed rainfall begins around 2200 UTC (forecast hour 1) at about 102˚W and ends around 1500 UTC (forecast hour 18) at about 94˚W longitude, while a weaker secondary rainfall axis begins a few hours before model initialization (perhaps 1900 UTC) at 98˚W and ends around 0900 UTC (forecast hour 12) at about 90˚W longitude. Note that both axes begin to repeat during the second diurnal cycle within the forecast period.

The Hovmöller diagrams for the five members of ENS4 (not shown) all reveal coherent propagating rainfall axes resembling both the primary and secondary axes from Stage IV observations. The ENS4 ensemble mean (computed using PM; Fig. 3a) also exhibits the propagating axes showing that the averaging process retains the propagating signal and may actually improve its representation relative to individual members. This improvement is suggested by the spatial correlation coefficients computed in Hovmöller space (Fig. 3e), which are higher for the ENS4 ensemble mean than all of its members during forecast hours 4 – 18, and all but one of its members during forecast hours 19 – 33.

Generally, Hovmöller diagrams and spatial correlation coefficients show that ENS4 has a better diurnal cycle depiction and representation of propagating rainfall axes than ENS20, especially during forecast hours 19 – 33. The larger differences during this later forecast period appear to result from the ENS20 members simulating the rainfall maximum that occurs during the second simulated diurnal cycle too early and too intensely, which is reflected in the ENS20 ensemble mean Hovmöller diagram and diurnally averaged time series of domain averaged rain volume for ENS4 and ENS20 members (Fig. 3d). These results imply that ENS4 has an inherent advantage over ENS20. The following sections will use various standard verification metrics to determine whether this advantage is enough to compensate for the smaller ensemble size of ENS4 relative to ENS20.

4. Comparison of ensemble ETSs

4.1 Analysis of diurnally-averaged Hovmöller diagrams

Warm season precipitation in the central United States tends to form at similar times of day and propagate over similar longitudes so that when diurnally averaged time-longitude (Hovmöller) diagrams of precipitation are constructed, coherent and propagating rainfall axes are observed (Carbone et al. 2002). These coherent axes, which are often composed of long-lived convective "episodes", suggest that an intrinsic predictability is associated with propagating rainfall systems over the central United States, so that predictability limits that have been suggested by past theoretical studies (e.g., Smagorinsky 1969, Lorenz 1969) may be longer than previously thought. However, partly because of shortcomings associated with CPs (e.g., Molinari and Dudek 1992; Kain and Fritsch 1998; Davis et al. 2003; Bukovsky et al. 2006), it is believed that numerical models will not be able to take advantage of this inherent predictability until CAR is utilized. Evidence from some preliminary studies comparing data

<table>
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<td>29 30</td>
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Figure 1 Domains for a) SREF ensemble members, b) ENS4 and ENS20 ensemble members, and c) the analyses conducted in this study.

Figure 2 Light pink highlighted dates indicate when SSEF ensemble runs were conducted and dark red highlighted dates indicate which of these cases were used in this study.

(a=0.05; resampling repeated 1000 times). For ETS comparisons, the biases from both ensembles were adjusted to the average bias between them which minimized the adjustments made to precipitation forecasts to account for bias. Because ROC score is insensitive to bias (e.g., Harvey et al. 1992; Mason and Graham 2002), no adjustments were made to forecasts prior to its computation.

4. RESULTS
The skill of deterministic forecasts derived using PM from each ensemble is compared by constructing time series of ETSs for 1-, 3-, and 6-h intervals at the 0.10-, 0.25-, and 0.50-inch rainfall thresholds (Fig. 4). For the ENS20 ensemble, in addition to computations using all 15 members, the ETSs computed using the ensemble mean from the 5 and 10 members with the best statistical consistency, as described by Eckel and Mass (2005) for a finite ensemble, are also examined [these members are noted in Table 2 and referred to as ENS20(5m) and ENS20(10m), hereafter]. Thus, comparisons between ensembles with the same number of members can be made, and impacts of the additional members to ENS20 can be examined. The range of ensemble member ETSs for ENS4 and ENS20 are also shown in Figure 4.

Generally, both ENS4 and ENS20 tend to have maxima in ETS between forecast hours 9 and 15 when both models have had sufficient time to "spin-up" (e.g., Skamarock 2004) and synoptic-scale error growth should still be relatively small. In addition, these forecast hours correspond to the times at which the propagating rainfall axis in the Midwest is at its maximum amplitude, suggesting some enhanced predictability associated with long-lived MCSs, which occur most frequently at times corresponding to these forecast hours (e.g., Maddox et al. 1983).

ENS20(5m) appeared to generally have lower ETSs than ENS20, while ENS20(10m) generally had very similar ETSs to ENS20, indicating that most of the skill realized from increasing ensemble size was obtained with an increase from 5 to 10 members, while very little skill was obtained with the increase from 10 to 15 members. Similar behavior illustrating a "point of diminishing returns" has been observed in previous studies (e.g., Du et al. 1997; Ebert 2001), and it is likely that additional model diversity (e.g., addition of members with a different dynamic core) would result in a larger increase in skill as demonstrated by the NCEP SREF system (Du et al. 2006). In addition, note that ensemble mean ETSs from both ensembles are greater than the highest corresponding ensemble member ETSs illustrating that the ensemble mean forecasts do represent an improvement relative to ensemble member forecasts, which is expected behavior in an ensemble.

After about forecast hour 9, at virtually all forecast lead times, accumulation intervals, and rainfall thresholds examined, ENS4 has higher ETSs than ENS20, with differences that are statistically significant occurring for 1-hrly accumulation intervals at all rainfall thresholds examined, and for 3- and 6-hrly accumulation intervals at the 0.50-inch rainfall threshold. The statistically significant differences generally occur between forecast hours 12 and 21, corresponding to the
times near and just after a maxima in ETS. Furthermore, between forecast hours 9 and 12 at the 0.25- and 0.50-inch rainfall thresholds for 1- and 3-hrly accumulation intervals are examined, which implies that timing errors may explain much of the differences, because timing errors decrease as longer accumulation intervals are examined (e.g., Wandishin et al. 2001). The implied influence of timing errors is also supported by the Hovmöller diagrams of diurnally averaged rainfall from each ensemble (Figs. 3a and b), and the diurnally averaged time series of domain average rainfall for all ensemble members (Fig. 4d), which were discussed in the previous section.

Further analysis (not shown; see Clark et al. 2009) of individual cases suggests that the ability of the CAR members in ENS4 to properly simulate propagating MCSs explains the statistically significant differences in ETS between ENS4 and ENS20 observed in Fig. 4.

4.3 Comparison of ROC scores
The skill of probabilistic forecasts derived from each ensemble is compared by constructing time series of ROC scores for 1-, 3-, and 6-h intervals at the 0.10-, 0.50-, and 1.00-inch rainfall thresholds (Fig. 5). Similar to ETS, ROC scores for the 5 and 10 members of the ENS20 ensemble with the best statistical consistency are also plotted. Because statistically significant differences between ENS4 and ENS20 ROC scores were confined to higher precipitation thresholds than in the ETS analysis, higher thresholds than those shown for ETS are shown for ROC scores in Figure 5. In general, maxima in ROC scores from both ensembles are observed at forecast hours 9-15. However, the amplitude of ROC score oscillations is much larger, especially in ENS4, as the rainfall threshold examined increases. The timing of this ROC score maximum likely is again due to enhanced predictability because of high relative frequency of MCSs at these times. There also appears to be a secondary maximum in ENS4 ROC scores at the 0.50- and 1.00-in rainfall thresholds for all accumulation intervals examined around forecast hour 27 (Figs. 5d-i). This secondary maximum also appears in the ENS20 ROC scores, but only at 6-hrly accumulation intervals (Figs. 5f and i). The timing of the secondary ROC score maximum corresponds to the secondary propagating rainfall axis noted in the Hovmöller diagram of observed precipitation during forecast hours 24-33 (Fig. 3c). Thus, it is also possible that ROC scores are enhanced around forecast hour 27 because of a tendency for propagating MCSs to occur during this time.

Similar to trends seen with ETS, ENS20(5m) generally has lower ROC scores than ENS20, while ENS20(10m) ROC scores are very similar to ENS20. Thus, most of the increase in ROC score realized from increasing ensemble size is obtained with an increase from 5 to 10 members, with the increase from 10 to 15 members having little impact.

At the 0.10-in rainfall threshold, at most forecast lead times, ENS20 has similar or slightly higher ROC
scores than ENS4. However, the differences are statistically significant only before forecast hour 9, at 1- and 3-hrly accumulation intervals, and at forecast hours 20 and 21 at 1-hrly accumulation intervals (Figs. 5a-b). Note that before forecast hour 9, model ‘spin-up’ processes are still ongoing and ENS4 takes longer than ENS20 to generate areas of rainfall because grid-column saturation must occur before rainfall is generated in ENS4 members, while grid-column saturation is not required in ENS20 members because a CP is used. At 0.50- and 1.00-in rainfall thresholds for 1-hrly accumulation intervals, ENS4 ROC scores are higher than ENS20, with differences statistically significant at many forecast lead times (Figs 5d and g). For 3-hrly accumulation intervals, ENS4 ROC scores are higher than ENS20 ROC scores, with differences statistically significant occurring only at the 1.00-in rainfall threshold (Figs. 5e and h), while for 6-hrly accumulation intervals, there are no statistically significant differences (Figs. 5f and i).

In general, statistically significant differences occurred around forecast hours 9-15 and 24-30, corresponding to the times at which maxima in ROC scores were observed. Also, similar to ETS, there was a trend for the differences between ENS4 and ENS20 to decrease with increasing accumulation intervals, implying the decreasing influence of timing errors with increasing accumulations intervals.

### 4.4 Ensemble spread and statistical consistency

#### 4.4.1 Rank histograms

Rank histograms are a useful tool to assess ensemble spread (Hamill 2001), and are constructed by repeatedly tallying the rank of the rainfall observation relative to forecast values from an ensemble sorted from highest to lowest. A reliable ensemble will generally have a flat rank histogram, while too little (much) spread is indicated by a u-shaped (n-shaped) rank histogram (Hamill 2001). Furthermore, the skewness of a rank histogram indicates bias, with right-skewness (left-skewness) indicating a tendency for members to over-predict (under-predict) the variable being examined.

For an ensemble composed of n members, precipitation observations can fall within one of any n+1 bins. The bars that compose a rank histogram represent the fraction of observations that fall within each of these bins. Thus, the ENS4 rank histograms are composed of 6 bars while those of ENS20 are composed of 16 bars. The different numbers of rank histogram bars makes it difficult to compare rank histograms from each ensemble. For example, it is obvious that the right-skewness of rank histograms from both ENS4 (gray shaded bars in Fig. 6a) and ENS20 (Fig. 6b) indicates a tendency for members to over-predict precipitation, but it is not clear which rank histogram indicates the greater tendency for over-prediction. To allow for a more convenient comparison, the 16 bins composing the ENS20 rank histogram are regrouped into 6 bins which each contain an equal portion of the original 16 bins (Fig. 6a). Care should be taken when interpreting the regrouped rank histograms. For example, the outer bins in the regrouped ENS20 rank histogram cannot be interpreted as the fraction of observations that fall completely outside the range of all ensemble members, as they are in ENS4, because they contain fractions from 3 of the original 16 bins. Rather, the regrouped rank histograms should be viewed as the rank histogram that would result from ENS20 if it was composed of 5 members, assuming these 5 members had about the same reliability and bias as the 15 member ENS20.

At all forecast lead times, the right-skewness of rank histograms from both ensembles indicates a tendency for members to over-predict precipitation (Figs. 6a, b). The right-skewness appears to be the most pronounced at forecast hours 21 and 27, which agrees with the time series of observed and forecast domain averaged rainfall (Fig. 3d) also showing the most pronounced over-prediction during these times. A comparison between the ENS4 and ENS20 (regrouped) rank histograms (Fig. 6a) reveals that ENS20 members more severely over-predict precipitation than the ENS4 members. Both ensembles have a slight u-shape indicating a lack of spread (i.e., under-prediction of forecast uncertainty), but the right-skewness of each ensemble’s rank histograms makes it difficult to...
diagnose which ensemble suffers most severely from this lack of spread. Thus, a procedure is devised to remove the bias from the members of the ensembles. The biases are removed using the PM method applied to each ensemble member forecast, so that forecast precipitation amounts are reassigned using the corresponding distribution of observed precipitation amounts. Thus, the modified forecast precipitation fields have the same pattern and location as the original forecasts, but forecast rainfall amounts are adjusted so their distribution exactly matches that of the observed precipitation. After the modification is applied, a computation of bias at all precipitation thresholds yields a value of 1. An example of a precipitation forecast before and after this procedure is applied is displayed in Figure 7.

Figure 6c reveals that ENS4* and ENS20* have a very similar representation of forecast uncertainty, with both ensembles exhibiting a slight lack of spread, especially up to forecast hour 21. However, there appears to be a trend for ENS4* rank histograms to become flatter with increasing forecast lead time, while those of ENS20* become slightly more u-shaped. By forecast hours 27 and 33 it is clear that ENS4* has a better representation of forecast uncertainty than ENS20*, as indicated by ENS4*'s flatter rank histogram than ENS20*.

### 4.4.2 Statistical Consistency Analysis

Ensembles correctly forecasting uncertainty are considered statistically consistent, and the mean-square-error (mse) of the ensemble mean will match the ensemble variance when averaged over many cases (Talagrand et al. 1999; Eckel and Mass 2005). In this study, mse and variance are computed according to Eqs. B6 and B7, respectively, in Eckel and Mass (2005), which account for an ensemble with a finite number of members. An analysis of statistical consistency compliments that from rank histograms because forecast accuracy (i.e. mse of ensemble mean) and error growth rates (i.e. ensemble variance) between ensembles can be compared, attributes that cannot be inferred from rank histograms. However, note that rank histograms provide information on ensemble bias, while an analysis of statistical consistency does not. The importance of recognizing bias when interpreting statistical consistency is illustrated in this section.

The trends in the mse of the ensemble mean and ensemble variance of both ensembles follow the diurnal precipitation cycle (Fig. 8). It appears that ENS20 under-predicts forecast uncertainty at most forecast lead times, except around forecast hours 21-24, corresponding to the minimum in the diurnal precipitation cycle. However, the ENS4 ensemble variance increases at a much faster rate than that in ENS20, and the ENS4 mse of the ensemble mean becomes similar to its ensemble variance around forecast hours 9, 12, and 15 for 1-, 3-, and 6-hrly accumulation intervals, respectively (Figs. 8a, c, and e). After about forecast hour 21, the ENS4 mse of the ensemble mean becomes smaller than the ensemble variance for all accumulation intervals, implying over-prediction of forecast uncertainty, contradicting rank histogram results.

The discrepancy between rank histogram and statistical consistency results (Figs. 8a, c, and e)
highlights the importance of recognizing the effects of bias when interpreting statistical consistency analyses. When bias is removed using the adjustment process described in the previous section, and mse of the ensemble mean and ensemble variance are recomputed (Figs. 8b, d, and f), the results are consistent with those obtained from rank histogram analyses (i.e., increasing statistical consistency with increasing forecast lead time in ENS4*, with little change in ENS20* statistical consistency as lead time increases).

Error growth rates (i.e., rate of increase in spread) can be directly analyzed using ensemble variance from ENS4* and ENS20* (Figs. 8b, d, and f). First, note that the faster error growth inferred from ensemble variance in ENS4 relative to ENS20 up to forecast hour 9 (at 1- and 3-hrly accumulation intervals), and after forecast hour 21 (all accumulation intervals; Figs. 8a, c, and e), is largely an artifact of bias. After the biases are removed, it becomes clear that the error growth rates of ENS4* and ENS20* are much more similar than what was implied by ensemble variance from ENS4 and ENS20. However, there are still noticeable differences. An approximation of average error growth rates computed by fitting a least-squares line to the ensemble variance (displayed in Figs. 8b, d, and f) for ENS4* (ENS20*) yields a slope of 0.016 (0.010), 0.255 (0.145), and 0.959 (0.527), for 1-, 3-, and 6-hrly accumulation intervals, respectively. So, although ENS20* ensemble variance begins higher than ENS4*, faster error growth likely resulting from resolving smaller scales in ENS4* than in ENS20*, leads to higher ensemble variance in ENS4* after forecast hour 21. Because ENS20* has one more set of varied physics parameterizations (namely, the CP) than ENS4*, it is likely that the larger ensemble variance in ENS20* during the first part of the forecast period results from larger model uncertainty in ENS4*, which is supported by time series of average ensemble variance from ENS4* and ENS20* run with only mixed-physics for a set of 20 cases (Fig. 12).

5. Conclusions

Generally, the results from this work are very encouraging for CAR, and the improvements realized from utilizing a CAR ensemble should provide incentive for operational SREF systems to refine their ensemble resolution to explicitly resolve convection, even if the number of members must be reduced due to computational limitations. However, because of the limited time period examined (Apr-Jun) and relatively small sample of cases, it is not clear whether these results are representative of other periods with different flow regimes. For example, the mid-summer months (i.e., July-August) characterized by a dominant upper-level ridge over the central US and “weakly-forced” convective events, may be even more advantageous to CAR ensembles relative to PCR ensembles because of a stronger diurnal signal during mid-Summer relative to Spring.

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