

1. Introduction

Rotunno and Emanuel (1987; hereafter RE) constructed an axisymmetric model of tropical cyclone (TC). Non-hydrostatic and with cloud physics, this model resolves cloud-scale convection. This model was used to study tropical cyclogenesis (hereafter abbreviated as cyclogenesis) using special initial conditions. The initial conditions used by RE consist of background vertical temperature and humidity profiles which are neutral to convection and a vortex of solid rotation in the inner most radius, surrounded by a Rankine vortex, which is tapered off to zero at large distance. The initial sea-level pressure and temperature perturbations are in gradient wind and thermal wind balance with the initial tangential winds. Similar type of initial vortex is used in most axisymmetric tropical cyclone models (e.g., Ooyama 1969). RE found that, with the initial condition parameter V_m (maximum surface tangential wind, defined in Eq. 37 of RE; it determines the strength of the initial vortex.) =12 m/s, cyclogenesis occurs within 2 to 3 days but with $V_m = 2$ m/s cyclogenesis fails to occur within 8 days. RE did not show the results after 8 days. Based on these results RE concluded that an initial vortex of sufficient amplitude is important to cyclogenesis. RE mentioned that the experiment with $V_m = 2$ m/s could lead to cyclogenesis if the integration period was extended, but for practical purposes (presumably they meant that what happened after 8 days should not be meaningful.) cyclogenesis did not occur.

The desire to understand the above results, which RE called the finite-amplitude nature of cyclogenesis, motivated the present study (see also Emanuel 1989). We are particularly interested in whether the RE model has two separate and unconnected quasi-equilibrium states: one corresponds to the tropical cyclone and the other to an undeveloped disturbance and whether the evolution leading to the two states depends on the initial condition. Our experiments and results are described in the next section and some discussions on the results are provided in the last section.

2. Experiments

Emanuel kindly provided the RE model. We used it to repeat and extend the RE experiments. The version of the model we used has both horizontal and vertical grid sizes reduced by a factor of 4 (they are 3.75 km and .3125 km respectively.) The time step has been reduced from 20 s to 10 s. Also it includes dissipative heat, which is responsible for more than 20% increase in maximum tangential wind (Bister 2001). Since we were not provided with the initial temperature and humidity vertical convectively neutral profiles corresponding to SST=26.5°C, as described in RE, but with neutral profiles corresponding to SST=24.89°C, we generated, from these profiles, the initial neutral profiles correspond to SST=26.5°C. We first computed the relative humidity of these given profiles and kept it and added 1.61°C to the temperature profile at all levels and then proceeded with the procedure that RE used to remove convective instability.

Our results from repeating the RE experiments reveal that given enough elapsed time even the smallest V_m can lead to cyclogenesis. Fig. 1 show the minimum SLP (hPa) of the first 40 days in four experiments, E1 through E4, with initial V_m equal to 1, 3, 6, 12 m/s respectively. The settings of E4 are

the same as those of the RE control experiment. The experiment with initial V_m equal to 1 m/s clearly shows no development prior to day 16 and between day 16 and day 18 a TC develops. The minimal sea level pressure (not shown) drops rapidly in four days, reaches a minimum of 965 hPa around day 28 and then gradually equilibrates to around 990 hPa. Though this cyclogenesis takes longer to reach its peak than what is normally observed in nature, this experiment clearly shows that cyclogenesis occurs suddenly and before and after the transition the model is in two complete different states. The onset is earlier when the initial vortex is stronger.

Fig. 2 shows precipitation as a function of time (40 days) and radius (first 150 km) for the four experiments, E1 through E4. One prominent feature of these figures is that prior to the onset process there is very little precipitation. This is the result of using convectively neutral initial condition. Thus the model cyclogenesis is associated with the start of convection. This is distinct from the observed transition. The observed cyclogenesis evolves from a preexisting disturbance, which has precipitation for quite some time prior to the cyclogenesis.

Thus, there is the question of whether the RE model can simulate something resembling the observed pre-genesis disturbances. An additional experiment, E5, shows that this is the case. E5 is a repeat of E1 except that in the initial condition the factors of 1 and -1 are multiplied to the tangential wind field at each vertical grid column alternatively in the radial direction. The initial temperature and pressure fields are then computed using these tangential winds in the same way as described in RE.

Fig. 3 shows the minimum sea-level pressure and maximum tangential wind for 160 days in E5. Between days 20 and 23 there is a growth of the disturbance. After an apparent overshooting, the disturbance soon settles to an intensity that is comparable to that of the observed pre-genesis disturbances. Fig. 4a (not shown) shows the tangential wind at hr 0 of day 52. It shows a TC-like structure with sub-TC intensity. Further integration of this experiment reveals a spontaneous cyclogenesis process starting around day 70. It takes only three days for the TC to reach its peak. Fig. 4b (not shown) shows the tangential wind at hr 0 of day 73. It shows a TC structure with maximum winds at 20km radius. Thereafter, the TC gradually dies down and returns to a pre-genesis state. Fig. 5 (not shown) shows the precipitation field as a function of time and radius. It shows a contracting convective ring at the time of cyclogenesis around day 70 and in the subsequent dying down process the eye-wall radius reduces and eventually the precipitation is concentrated at the center of the pre-genesis disturbance. This is then followed by another cyclogenesis, which is also associated with the contraction of a convective ring. Apparently, the model state alters between a tropical cyclone state and a pre-genesis state. The transition into the tropical cyclone state, the cyclogenesis, is rapid. However the transition back to the pre-genesis state is rather slow.

In the pre-genesis stage convection develops outside of 250 km radius and then moves toward the center at a very slow speed (~0.2 m/s) as the center disturbance weakens. The spontaneous cyclogenesis is associated with the final stage of the contraction of this convection region, whose speed remains slow (~0.35 m/s). This contraction reminds one of the eye-wall replacement found in observations (Willoughby et al. 1982) and in an MM5 simulation of Hurricane Floyd (1999) (Tenerelli and Chen 2002). However, the scale and the duration of this contraction are much larger and longer and it is associated with a rapid sea-level pressure drop and a maximum tangential wind

increase of magnitudes that are found only in cyclogenesis. The eye-wall replacement in the mature tropical cyclones involves relatively little changes in these two quantities.

3. Discussion and summary

We have found that the initial vortex specified by RE leads to cyclogenesis even with weak amplitude. It only takes longer to start. Therefore for the RE finite amplitude nature interpretation to hold, it is necessary to use the specific initial vortex they prescribed and to require that cyclogenesis to occur within eight days. Our results from the RE model show that the model does support a state that resembles the observed pre-genesis disturbances. A different initial condition is required to reach this state first. And after an initial adjustment the model state transits between this pre-genesis state and the full-fledged TC state. Apparently, the initial vortex as specified by RE is quite different from these two states.

To have a realistic simulation it is necessary that the model's quasi-equilibrium trajectories match closely those in nature and that the initial state of the model is located on a trajectory in the model quasi-equilibrium evolution phase space. Granted that models are never perfect, they can only be used for a limited period and therefore the realistic initial condition become important, if one's purpose is to do a short-term realistic simulation. On the other hand, if one's purpose is to understand the physical mechanism, the requirement on the model is not that stringent (as long as it does not miss the major quasi-equilibria or the oscillation modes that one intends to study.) Also an idealized initial condition can be used in order to demonstrate a particular point. The vortex plus neutral profiles type of initial condition that RE used is for the purpose of demonstrating that convective instability in the initial profile is not necessary for cyclogenesis. Also the saturated core initial condition used by Bister and Emanuel (1997) is another example.

The answer to our question raised in the introduction is that the RE model does not have two unconnected quasi-equilibrium states. The model state transits between two regions in the phase space, one resembling the tropical cyclone state and the other the pre-genesis disturbance. Which of the two regions the model state enters into first depends on the initial conditions. The type of initial conditions that RE used leads to the tropical cyclone region first (so does the one that Bister and Emanuel (1997) used.) And a different type of initial conditions is needed for the model state to enter the pre-genesis state first. The spontaneous cyclogenesis found in E5 exhibits some characteristics which remind one of the observed eye-wall replacement. But it is clearly distinct from the eye-wall replacement.

Although the physical mechanism of the spontaneous cyclogenesis in the RE model remains to be explored, some arguments can be put forth to support the experimental results we obtained. The experimental results show that the model state transits between two states one corresponding to a TC and the other to a pre-genesis disturbance. This is much more reasonable than the case that only one of the two states exists. If only the pre-genesis disturbance existed as a quasi-equilibrium state, then the model

would not be able to simulate cyclogenesis. If only the TC state existed as a quasi-equilibrium state, then spontaneous cyclogenesis would not be simulated. The fact that spontaneous cyclogenesis occurs means these two states are not unconnected. This is also quite reasonable. This means that the TC in the model eventually has to die down (in its transition into the pre-genesis state). In that process convection in the core diminishes and convection in far field develops and strengthens so that the total rainfall does not change rapidly. So the remaining questions are why the transition into the TC state is much more rapid than the reverse transition and why the outer convection region contracts. These questions will be our future research foci.

Is the spontaneous cyclogenesis in the RE model realistic? Observations do show that sometimes pre-genesis disturbances turn into TC without obvious triggers. But, the observed cyclogenesis is not associated with the contraction of an outer convective ring. Thus the usefulness of the model results is called into question. The unrealistic contracting convective ring leads us to conclude that the axisymmetry of the RE model is a severe restriction. Due to this restriction, the RE model (and most likely all axisymmetric tropical cyclone models) should be used with caution.

In summary, the contribution of this work lies in its exploration of the long-term behavior of the RE model. Our experiments reveal that the RE model state transits between two states: one corresponding to the pre-genesis disturbance and the other to the TC. The transition from the former to the latter is fast and spontaneous, while the reverse transition is slow. Which state the model falls into first depends on the initial condition. The type of initial vortex used by RE allows the model to fall into the TC state first even with very weak amplitude. A different type of initial condition is needed for the model to fall into the pre-genesis disturbance first. However, since the spontaneous cyclogenesis has an unrealistic contracting convective ring, the RE model (and mostly likely all axisymmetric TC models) should be used with caution for studying cyclogenesis. The cause of the unrealistic simulation is attributed to the axisymmetry of the model. Finally, there is an obvious need of repeating our experiments with other tropical cyclone models, both 2-D and 3-D.

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Email: winston.c.chao@nasa.gov

